

ERRATA

Page 15: Line 7: $P \in \vec{CA}$ and $P \in \vec{CB}$

Page 16: Exercise 9: This result is true if and only if D and E are on the same side of \overleftrightarrow{AB} .

Page 16: Proposition 1.5.8: The proof works for a non-straight angle. If $\angle CAB$ is a straight angle then the bisector is the perpendicular line through A , whose existence is guaranteed by Theorem 1.5.9.

Page 45: Exercise 1(a): Let D be between B and C , and $A \dots$

Page 71: Second line of proof of Proposition 2.1.3 “ $\Rightarrow m_2 \parallel l$ and $m_2 \parallel m_1$ ”.

Page 72: Fifth line below Figure 2.3: “through P ”

Page 82: Line -5: **Proof of Theorem 2.3.3** It follows from Axiom **S**₂ of Chapter 1 that, given a positive integer number N , there exists $P_1 \in t$ such that

$$\frac{AC}{N+1} < AP_1 < \frac{AC}{N}$$

(why?) which implies

Page 83: Line 15: “where the last inequality above was implied by the fact that $K \leq N$. Since the inequality $|AB/AC - A'B'/A'C'| < 2/N$ holds for any positive integer N , we conclude that”

Page 85: Line 8: $\triangle ADE \sim \triangle ABC$.

Page 123: Line 4:

$$\frac{PA}{PP'} = \frac{P''B}{P''P'} = \frac{1}{2}.$$

Page 131: Exercise 22: such an example does not exist. I am replacing this exercise by “Show that a group of rigid motions that contains a translation is infinite.”

Page 142: Exercise 5, Line -3: Consider P' the image of P under the inversion in circle C .

Page 170: Figure 4.3: We need to draw line l_1 through P and P_2 and line l_2 through P and P_1 .

Page 171: Figure 4.4: We need to draw lines l_1 and l_2 through P .

Page 171: Line -2 (starting from the bottom of the page) “ l is perpendicular to n .”

Page 188: Last line, change $\det(u, v, w)$ to $\det(w, u, v)$.

Page 189: Line 4: $u \wedge v = (u_2v_3 - v_2u_3, -(u_1v_3 - v_1u_3), u_1v_2 - v_1u_2)$.

Page 205: Line 4: $(0, 0, 1) = g(1, 1, 0) + h(1, -1, 0) + i(0, 0, 1)$.

Page 210: Line 1: $\beta' = \{(0, 1, 1, 0), (1, 0, 1, -1), (1, -1, 0, 1), (1, 1, -1, 0)\}$.

Page 215: Line 19: $(0, 0, 1) = g(1, 1, 0) + h(-1, 1, 0) + i(0, 0, 1)$.

Page 217: Line 2: $\beta = \{(1, 1, 1), (1, 1, 0), (1, 0, 1)\}$.

Page 221: Line 11: Applying Proposition 5.3.2(b).

Page 228: Exercise 17, Line 15 (2) We claim that $F_j \neq 0, \forall j = 1, \dots, n$. In fact, suppose in search of a contradiction, that there exists a T_j that is a translation.

Since the group G is finite T_j^m will have to be a reflection, for some integer m . Recall that compositions of translations are translations. Find the contradiction.

(3) Conclude that

$$T_j(y) = y, \quad \forall j = 1, \dots, n.$$

Page 254: Exercise 7(b): Show that the area of a rhombus is half of the product of the lengths of its diagonals.

Page 254: Exercise 7(c): $v = \vec{AD}$.

Page 269: Line 3: $B' = \mathcal{P}' \cap P$.

Page 290: Line 13: $(-\cos \theta \sin^2 \varphi, -\sin \theta \sin^2 \varphi, -\sin^2 \theta \sin \varphi \cos \varphi - \cos^2 \theta \sin \varphi \cos \varphi)$,

Page 292: Line -2 and remaining of the proof of Theorem 7.4.4 should be replaced by: "Notice that the map $f: \mathbf{R}^3 \rightarrow \mathbf{R}^3$ given by $f(x, y, z) = (-x, -y, -z)$ is a rigid motion, since $\|(x, y, z)\| = \|(-x, -y, -z)\|$. Therefore

$$\text{Area}(\triangle(-A)(-B)C) = \text{Area}(\triangle AB(-C)),$$

since area is preserved by isometries (Exercise 5). Substituting above we obtain

$$\text{Area}(H_C) = \text{Area}(S_A) + \text{Area}(S_B) - \text{Area}(\triangle ABC) \text{Area}(S_C) - \text{Area}(\triangle ABC).$$

and hence

$$\begin{aligned} \text{Area}(H_C) &= \text{Area}(S_A) + \text{Area}(S_B) + \text{Area}(S_C) - \\ &\quad 2\text{Area}(\triangle ABC), \end{aligned}$$

implying

$$2\pi = 2m(\angle A) + 2m(\angle B) + 2m(\angle C) - 2\text{Area}(\triangle ABC),$$

which gives the theorem."

Page 295:

$$\pi(X) = (0, 0, 1) + \frac{1}{1-z}((x, y, z) - (0, 0, 1)) = \frac{1}{1-z}(x, y, 0).$$

Page 296: Figure 7.12: We need to draw z -axis.

Page 296:

$$\sigma'_2(t_1) = \left(\frac{x'_2(t_1)}{1-z_2(t_1)} + \frac{x_2(t_1) \cdot z'_2(t_1)}{(1-z_2(t_1))^2}, \frac{y'_2(t_1)}{1-z_2(t_1)} + \frac{y_2(t_1) \cdot z'_2(t_1)}{(1-z_2(t_1))^2} \right).$$

Page 315: Second line " $\triangle A'B'B$ and $\triangle A'BD$."

Page 323: Proposition 8.4.3, second line $\dots P'Q' \perp l'$. Page 325: Lines 3,4,5, 6, and 8: changed line l to m' .

Page 350: Line -3: "In fact, let g_1 be an isometry that maps D to the center (see Exercise 6 of this section)."

Page 350: Last line $AB = DE$.

Page 373: Proposition 10.4.4, line -2: "Notice that f_1 and f_3 are linear complex functions..."