

The Effect of Power Saturation on the Line Shapes of Nitroxide Spin Probes Under the Influence of Spin-Exchange and Dipole–Dipole Interactions Studied by CW EPR

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Abstract

The continuous-wave saturation (CWS) behavior of several measureable parameters in an EPR spectrum of a nitroxide free radical is carried out theoretically and tested experimentally with ¹⁵N-d₁₇-4-Hydroxy-2,2,6,6-tetramethylpiperidine 1-oxyl in 60% aqueous-glycerol solutions from 273 to 340 K. The theory explicitly includes spin relaxation due to electron spin exchange and dipole-dipole interactions, but no other spectral diffusion pathways of paramagnetic relaxation. A primary objective of this work was to study the CWS of the dispersion signal induced by spin exchange and dipole-dipole interactions, a signal that is superimposed upon the absorption. This was rendered possible because, using modern least-squares fitting methods, the two signals may also be separated to high precision. Using a new rigorous theory, theoretical spectra were simulated and were also separated into absorption and dispersion components. The absorption components, both experimental and theoretical, may be analyzed using the traditional Bloch equations and compared with literature results. The dispersion components may only be analyzed by direct comparison of parameters derived from the theoretical and experimental spectra. A comparison of the amplitudes of the absorption and the dispersion components provides a severe test of the theory and the experimental results are good agreement with the theory. The experimental values of T_1 both from The Bloch equations and the direct comparison of the absorption components were comparable to the limited and scattered literature results where both pulsed- and CWS methods were employed. From the theory, the same value of T_1 was found from the CWS of the Lorentzian line width and the doubly-integrated intensity; however, there were discrepancies in the values of T_1 for these two parameters experimentally.

Extended author information available on the last page of the article

1 Introduction

This is the first of a series of papers in quest of a deeper understanding of the effects of Heisenberg spin exchange (HSE) and dipole-dipole (DD) interactions on saturated EPR spectra of nitroxide free radicals (nitroxides) in solution. See Table 1 for a summary of abbreviations, notes, and acronyms. We extend further our theory [1-5] to an arbitrary value of the circularly-polarized magnetic induction of the microwave field, H_1 , and compare the theoretical predictions with experimental results obtained from the nitroxide 4-hydroxy-2,2,6,6-tetramethylpiperidine-d₁₇-1-¹⁵N-oxyl (15D-Tempol). Here, our focus is on nitroxides executing rapid rotational and translation motion yielding spectra in the motional-narrowed regime. Our goal is to understand the spin-relaxation behavior of nitroxides in solution in view of recent discoveries of interesting spectral properties of nitroxides where HSE and DD interactions which, at increasing concentration, C, (M) induce signals that are admixtures of absorptive and dispersive terms: e.g., see [6,7] and references therein. When we refer to "signals", we mean the components of the EPR spectrum observed out-of-phase with H_1 , normally observed with a modern EPR spectrometer employing automatic frequency control. Thus the designation *dispersion* in this context is distinct from its historical meaning of being the in-phase signal. Recent work offers a different viewpoint of this mixed shape of resonance lines [5]. These admixtures are a result of transfer of spin coherence by HSE, DD, or both. Thus, for ¹⁴N nitroxides, instead of three pure absorption lines observed at low C, three spin modes [2, 6, 7] result at higher C. The modes at high- and low-fields, (hf and lf) are comprised of two components, one absorption plus one dispersion while the central-line (cf) only shows only the absorption. Furthermore, as HSE increases, intensity of the absorption contributions to the lf and hf modes is transferred to the cf mode [8]. Finally, the lf and hf absorption components change from absorption to emission [6, 7]. For ^{15}N nitroxides, the lf and hf are each comprised of one absorption and one dispersion. This work will also address the complex effect of inhomogeneous broadening (IHB) due to proton (deuteron) hyperfine structure (hfs) on the saturation behavior of nitroxides in the presence or absence of HSE and/or DD. For convenience, we mostly refer to protons in the text when it is clear that we mean either isotope. There has been considerable work on all of these aspects except for the dispersion. See, for example the review by Marsh and coworkers and references therein [9]. A problem that its already complicated by hfs, HSE, and DD [6] is further complicated because of the addition of another dimension, H_1 . Fortunately, the reader may consult [9] as well as clear expositions of the various complicating factors in two recent books that detail the progress to date by Salikhov [2] (theory) and by Marsh [10] (theory and experimental methods). Both books provide a wealth of references and historical perspective.

It's been 55 years since McConnell's group at Stanford published their seminal work on nitroxides [12]. See, for example, [13] for a summary of the fundamental advances in the field replete with history and images of many of the principal contributors. The practical applications of nitroxide spin probes that have

Table 1	Definitions,	abbreviations,	notes,	and	acrony	/ms
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Nitroxide	Nitroxide free radicals. For simplicity, we refer to "nitroxides" throughout the paper; however, our procedures and results may apply to other radicals under certain conditions
Tempol	4-Hydroxy-2,2,6,6-tetramethylpiperidine-1-oxyl. To refer to per- deuterated Tempol, we use the acronym D-Tempol and to the ¹⁵ N enriched Tempol, we use ¹⁵ N Tempol or ¹⁵ N D-Tempol
Tempone	2,2,6,6-tetramethyl-4-oxopiperidine-1-oxyl. To refer to per-deuter- ated Tempone, we use the acronym pp-Tempone and to the $^{15}\mathrm{N}$ enriched Tempone, we use $^{15}\mathrm{N}$ Tempone or $^{15}\mathrm{N}$ p-Tempone
Protons	Generically refers to either protons or deuterons when there is no need to distinguish
hfs, hfc, hfp	Hyperfine structure, isotropic hyperfine coupling constant(s), hyperfine pattern
HSE, DD	Heisenberg spin exchange and dipole–dipole interactions, respec- tively; HSE/DD denotes HSE and or DD
$A_0, a_p a_d$	Nitrogen, proton, or deuteron hfc, respectively
M	Label of the <i>M</i> th nitrogen manifold. $M = $ lf, cf, and hf for ¹⁴ N or lf and hf for ¹⁵ N, denoting the low-, center-, and high-field manifolds, respectively
Manifold	Superposition of proton or deuteron spin modes corresponding to each nitrogen nuclear quantum number, <i>M</i> . Also referred to as a "line" or a "nitrogen line."
IHB	Inhomogeneous broadening of the nitrogen manifold, principally due to hfs of protons, but also due to magnetic field modulation
С	Concentration, M. $C = 0$ denotes $C = 10^{-6}$ M for calculations and 3×10^{-5} M for experiments
H_1	The magnitude of the circularly polarized magnetic flux density of the microwave field, G. $H_1 = 0$ denotes $H_1 = 0.0001$ G in the calculations
V _{sct}	Rate of spin coherence transfer
Intermediate zones	The region of HSE/DD where the transfer of spin coherence (sct) is comparable to the hyperfine spacing. For nitroxides, there are two such zones, the proton, $\gamma a_{\rm p} \approx V_{\rm sct}$ or nitrogen, $\gamma A_{\rm p} \approx V_{\rm sct}$, intermediate zone, respectively
Spectrum	The first-derivative of the EPR signal detected predominantly out- of-phase with H_1 by employing automatic frequency control
Absorption component	In the absence of transfer of spin coherence transfer, the spectrum. In the presence of HSE/DD, the antisymmetric component of the spectrum. Also referred to as the "absorption."
Instrumental dispersion	In the absence of transfer of spin coherence, a small admixture of the EPR signal in-phase with H_1 due to a slight mismatch of the cavity coupling
Dispersion component	In the presence of transfer of spin coherence, the symmetric component of the spectrum after subtracting the instrumental dispersion. Also simply referred to as the "dispersion." The signal in-phase with H_1 with or without HSE/DD is called in-phase dispersion
Voigt(s), Lorentzian(s), Gaussian(s)	First-derivative Voigt, Lorentzian, or Gaussian line shape func- tions, respectively, used as adjectives to modify dispersion or absorption. For example, we refer to a Voigt dispersion or a Lorentzian absorption, etc.

Table 1 (continued)	
CWS	Continuous wave saturation; a plot of a parameter measured from a spectrum versus H_1 in the abstract referring to any parameter or to a particular parameter. In particular, we detail CWS(ΔH_{pp}^L), CWS(I), CWS(V_{disp}), and CWS(V_{pp})
Fit	Verb, performing a non-linear least-squares fit of the spectrum or CWS to a specified fit function. Noun, the result of the fit
Eye fit	Verb, finding the best fit of the CWS of one or several parameters. Noun, the result of the fit
Map	Refers to the mapping of the measured mixing constant for the Lorentzian—Gaussian sum-function approximation to the Voigt for a particular hfp. Most maps are due to the Universal Map [11], applicable to most nitroxides under most conditions to the precision given in [11]. If unspecified, the Universal Map is assumed. For accurate representations of the theory, nitroxide- specific maps are employed and are noted
T_{10}, T_1^{eff}	Intrinsic spin–lattice relaxation time directly to the lattice, directly to the lattice and indirectly through other relaxation pathways, respectively

developed over this time span, and continue to be developed—just in biology and chemistry—is impractical to summarize because of its sheer abundance. Fortunately, a series of reviews of the advances have been available regularly: e.g., [14–16]. Useful reviews of continuous wave saturation (CWS) and other EPR techniques to study exchange processes and distances in membranes were given in [9] and [10]. Because of their practical use for studies of in vivo EPR imaging, relaxation times have been measured for a number of isotopically-substituted nitroxides [17]. Similar studies focused on the role of electron spin relaxation for Overhauser dynamic nuclear polarization [18–25].

Aside from their practical uses in chemistry and biology, nitroxides offer a unique testing ground for our understanding of interacting spins in liquids because they: (a) are stable and may be studied over wide ranges of temperatures in solvents of different viscosities and polarities; (b) have well defined hfs patterns that are precisely known [11] and variable by changing solvent polarity, nitroxide structure, and deuteron substitution; (c) afford precise variation of the spin diffusion due to HSE and DD from being negligible to one or the other being dominate; and, (d) offer two distinct regions of hfs and therefore, two intermediate zones [6]. The term "intermediate zone" refers to rates of transfer of spin coherence that are comparable to hyperfine coupling constants. Thus we refer to the proton or nitrogen intermediate zone when the rate of transfer of spin coherence is comparable to either γa_p or γA_0 , where a_p or A_0 are the hyperfine coupling constants, in gauss, due to the protons or the nitrogen, respectively.

The feature that is completely new in this line of investigation is the role of the transfer of spin coherence that provokes line shifts and dispersion components [2]. The line shifts are beyond the scope of the present work, but are potentially very interesting because they arise not only from either HSE or DD [6] but also from the interaction of H_1 [3].

See a recent publication [26] for a brief summary of the development and uses of CWS and motives for pursuing the method further. Because the dispersion and absorption components may be reproducibly and accurately separated [6, 27], the saturation behavior of each component may be studied independently by CWS. Specifically, the saturation of the dispersion component may now be studied by CWS because it is separated from the much larger absorption. It would be difficult by pulsed methods because the recovery to equilibrium of both signals would be superimposed.

It has been 67 years since Portis published his pioneering paper on spin relaxation of *F*-centers as measured by continuous-wave saturation (CWS) of EPR of IHB spectra of *F*-centers [28]. Portis studied the CWS of the maximum amplitude of the absorption and showed that its unusual saturation behavior could be understood if the signal were comprised of individual Lorentzian resonance lines distributed over many resonance fields due to hyperfine coupling to neighboring magnetic nuclei. Portis coined the term "spin packet" which refers to an individual resonance line of Lorentzian shape with full-width at half-height line width, $\Delta H_{1/2}^L$, that saturates according to the Bloch formalism, the "homogeneous case"

$$Y(H) = K_{\text{peak}} \frac{H_1}{1 + \left[\gamma \left(H - H_0\right)T_2\right]^2 + \gamma^2 H_1^2 T_1 T_2},$$
(1)

where H_1 is the effective value of the circularly-polarized magnetic induction and K_{peak} is the slope of the amplitude $Y(H_0)$ in the unsaturated region; i.e., for $H_1^2 T_1 T_2 \ll 1$ which we call "small H_1 ." $T_2 = 2/\left[\gamma\left(\Delta H_{1/2}^L\right)_0\right]$ where subscript 0 denotes $(H_1 \rightarrow 0)$. Experimental determination of H_1 depends on factors discussed in detail in [26] and references therein. In (1), γ is the gyromagnetic ratio of the free electron, H and H_0 are the swept- and resonance-magnetic fields, respectively. In Portis' model, it is assumed that T_1 and T_2 are the same for all spin packets. The spin packets are distributed over an IHB profile to form a manifold of overlapping, unresolved Lorentzian lines.

To compare with theory, Portis assumed an IHB profile of Gaussian shape (Gaussian), leading to the convolution of a Lorentzian and Gaussian, the Voigt, to represent the spectrum [11, 28].

The familiar Voigt [11], used in various fields of physics [29], is defined by the single parameter, χ as follows:

$$\chi = \frac{\Delta H_{\rm pp}^{\rm G}}{\Delta H_{\rm pp}^{\rm L}},\tag{2}$$

where ΔH_{pp}^{L} and ΔH_{pp}^{G} are the peak-to-peak Lorentzian line widths of the spin packets and of the Gaussian profile, respectively in a first-derivative presentation. Experimentally, Portis plotted the CWS of the maximum of the absorption in the center of the Voigtian line as well as the CWS of the height of the signal in-phase with H_1 , the "normal" dispersion, which showed no saturation. Schematic representations of the Voigt comprised of spin packets abound in the literature. See, for example, Fig. 2 of [28] (non-derivative) or Fig. 1 of [6] (derivative). This latter schematic also includes dispersion components due to HSE and provides a graphical definition of the peak-to-peak height of the Voigt, denoted by V_{pp} , and the peak-to-peak line width of the Voigt, ΔH_{pp}^0 . In this work, these quantities will carry an index, when needed, to refer to a particular manifold or to distinguish between HSE and DD.

Portis assumed that there were no interactions between the spin packets and that $\chi \to \infty$. He also established the fact that the spin packet was Lorentzian to high precision, justifying the use of the Lorentzian CWS, Eq. (1) [28]. The lack of interactions between the spin packets implies that transfer of spin coherence was absent.

Castner [30] studied the CWS of V_{pp} of the spectrum of the V_K center. He also assumed the Voigt and no spin diffusion, however, maintained a finite value of χ to successfully describe CWS. The two authors studied the height of the symmetric EPR absorption in its non-derivative (Portis) or derivative (Castner) presentation; neither studied the integrated intensity which is given in Eq. (17) of [30].

Wolf [31] extended the work of Portis and Castner by including an unknown mechanism of spectral diffusion only controllable over a limited range by varying the temperature. He did not include transfer of spin coherence.

These three works suffered from the lack of a detailed knowledge of the hfs and in Wolf's case, a lack of knowledge of the diffusion process and the omission of a treatment of transfer of spin coherence. Nitroxides treated with modern theories suffer from none of these deficiencies.

Modern workers have a tremendous advantage that allows us to separate the absorption and dispersion components of each line separately even if they are severely overlapping even to the extent that separate lines are not visually evident in the spectrum. The program Lowfit, which is described further below, is our method of effecting this separation. The significance of this separation is that we have a method to study the absorption component using the long established Bloch formulation of spin relaxation. The study of the dispersion components is now made possible by rigorous theories such as the one in the next section.

From the Bloch formalism, the first-derivative spectrum of a homogeneous line, the peak-to-peak line width, ΔH_{np}^{L} , varies with H_1 as follows [26, 32]:

$$\Delta H_{\rm pp}^{\rm L}(C) = \Delta H_{\rm pp}^{\rm L}(C)_0 \left(1 + H_1^2 \frac{2}{\sqrt{3} \Delta H_{\rm pp}^{\rm L}(C)_0} \gamma T_1 \right)^{\frac{1}{2}}, \tag{3}$$

...

where the subscript 0 means the limit as H_1 goes to zero. $T_2 = \lim_{C \to 0} 2/\left[\sqrt{3\gamma} \Delta H_{pp}^L(C)\right]$ while the peak-to-peak height is given by [26, 32]

$$V_{\rm pp}(C) = K_{\rm pp} \frac{H_1}{\left(1 + H_1^2 \frac{2}{\sqrt{3}\Delta H_{\rm pp}^{\rm L}(C)_0} \gamma T_1\right)^{3/2}}.$$
(4)

The CWS of V_{pp} or ΔH_{pp}^0 for an IHB manifold are not described by (3) or (4), respectively; however, provided that spin packets do not interact, the CWS for the

doubly integrated intensity of the first-derivative spectrum, I, does have the same form as that for a homogeneous line (Eq. 11 of [26]) as follows:

$$I(C) = K_{\rm I} \frac{H_{\rm I}}{\left(1 + H_{\rm I}^2 \frac{2}{\sqrt{3} \Delta H_{\rm pp}^{\rm L}(C)_0} \gamma T_{\rm I}\right)^{\frac{1}{2}}},$$
(5)

where $K_{\rm I}$ is the slope of I at small $H_{\rm I}$.

Equations (3–5) are appropriate to the absorption components, only. A priori, Eqs. (3–5) are not expected to describe the CWS of real nitroxides except at $C \rightarrow 0$.

Let us summarize the argument in [26] that (5) applies to IHB spectra for $C \rightarrow 0$. Because each spin packet is independent of the others, it saturates as (5). *I* is the sum of the doubly-integrated intensities of all of spin packets, thus *I* also saturates according to (5). This same conclusion has been reach by others [9] based on the Voigt convolution [9]. The simpler argument given here shows that the assumption of a Voigt is unnecessary for $C \rightarrow 0$; it is true for any IHB profile, indeed for resolved or powder spectra.

A similar argument applies to fitting a CWS of ΔH_{pp}^{L} to (3) for $C \rightarrow 0$ even for IHB spectra. We assume that all of the spin packets in a given manifold have the same line width at $C \rightarrow 0$. Each spin packet broadens according to (3) so each spin packet continues to have the same width; thus the average width extracted from fit to a Voigt also follows (3). Here, the requirement of a Voigt line is explicit and therefore less general than the application of (5) which is valid for any line shape.

In the literature, it is generally accepted that for C > 0, in the presence of HSE, that the forms of CWS Eqs. (3) and (5) may be correctly applied to IHB spectra and give effective values of T_1 , T_1^{eff} , [9]. The implicit use of (3) for the CWS of ΔH_{pp}^L for IHB nitroxides in refs [33, 34] are examples; however, those authors used a different approach to obtain ΔH_{pp}^L . In other work, the CWS of *I* is used to obtain T_1^{eff} [9]. Whether these approaches to obtain T_1^{eff} are born out experimentally in the context of a rigorous theory is beyond the scope of this paper, but is obviously an important conjecture worthy of study. We shall see that under the assumptions of our theory, T_1^{eff} obtained from the absorption component of theoretical spectra shows that this conjecture is reasonable except in proton intermediate zones. See Table 4 below. In the theory developed here, the only relaxation pathways that are specifically included are due to HSE and/or DD.

A straightforward method to obtain *I* is to numerically integrate the spectrum twice, a necessary procedure for spectra not describable by an analytic line shape, for example slow motion or powder spectra. However, for fast motion nitroxide spectra such as those in Fig. S4 that are accurate Voigts, the accuracy is improved by at least an order of magnitude by using the parameters χ , V_{pp} and ΔH_{pp}^{0} to compute *I* employing Eq. (35) of [11]. For noisy spectra the improvement is even greater. For a dramatic demonstration of this latter point, see Fig. 11 of [35].

In a comprehensive experimental and theoretical treatment of CWS in liquids that included the effects of HSE, Eastman et al. [34] studied the tetracyanoethylene anion radical (TCNE-) under conditions in which DD was negligible. Earlier studies of

HSE of radicals in solution at low H_1 are cited in refs. 1–7 of [34]. At low concentrations, where HSE was negligible, they observed the expected nine well separated narrow lines of relative intensities near 1:4:10:16:19:16:10:4:1 spaced by A_0 . Defining the spin exchange rate constant K_{ex} such that the frequency of spin exchange, ω_{ex} , is $\omega_{ex} = K_{ex}C$, those authors showed that for slow exchange, $K_{ex}C \ll \gamma A_0$, the effective spin–lattice relaxation time of the *k*th line with statistical weight of the ϕ_k was as follows:

$$T_{1k}^{\rm eff} = T_{10} \left[\frac{1 + T_{10} K_{\rm ex} C \phi_k}{1 + T_{10} K_{\rm ex} C} \right].$$
(6)

Here k labels the projection of the nitrogen nuclear quantum numbers. T_{1k}^{eff} governs the CWS of each well separated Lorentzian line according to Eqs. (3)–(5) and depends on k if ϕ_k varies with k as was the case with TCNE-. In this example, $\phi_k = 1:4:10:16:19:16:10:4:1$, each divided by 81. T_{10} is the spin–lattice relaxation time directly to the lattice of each line, assumed to be independent of k.

For nitroxides without protons, labelling the lines with the projection of the nitrogen spin quantum number, M, $\phi_M = 1/(2I + 1)$ yields

$$T_{1M}^{\text{eff}} = T_{10} \left[\frac{1 + T_{10} K_{\text{ex}} C (2I+1)^{-1}}{1 + T_{10} K_{\text{ex}} C} \right].$$
(7)

Equations (6) and (7) have the simple physical interpretation that T_{1M}^{eff} is reduced by HSE from T_{10} through the relaxation pathways provided by the non-resonant lines. The application of (7) to Fremy's salt, which contains no protons, was carried out in [36] assuming that the spectrum was approximately Lorentzian using the CWS of the linewidth, (3), to obtain T_{1cf}^{eff} . Except for Fremy's salt, all nitroxides are IHB.

To simplify the presentation, we discuss *N* equivalent protons which applies directly to radicals such as di-tert-butylnitroxide (DTBN) and 2,2,6,6-tetramethyl-4-oxopiperidine-1-oxyl (Tempone). For small H_1 , this simplified hfs yields spectra that are excellent approximations to those derived from the true hfs for most nitroxides for $\chi < 2$ [11]. We demonstrate below that the same holds for saturated spectra by comparing CWS of Tempone vs. 4-hydroxy-2,2,6,6-tetramethylpiperidine 1-oxyl (Tempol). The advantage of this restriction is that a concrete, clearer exposition may be presented, maintaining the essential physical content. Our calculations are applicable to any hfs, so this simplified presentation does not affect the results for other hfs.

The IHB (ΔH_{pp}^{G}) of spectra obtained with a modern EPR spectrometer is dominated by field modulation and hfs due to protons [37]. The former is treated in [37] and the latter by Eq. (2) of [11] from which, for *N* equivalent protons (deuterons),

$$\Delta H_{\rm pp}^{\rm G} = a_{\rm p} \sqrt{\alpha N} = a_{\rm d} \sqrt{8\alpha N/3},\tag{8}$$

where α is a constant, near unity, to account for the small difference between the hyperfine pattern and the Gaussian. For Tempol, $\sqrt{\alpha} = 1.04$ [11].

The studies of the saturation of nitroxide spectra leading to (6) and (7) were limited to the effects of HSE on ΔH_{pp}^L , using the square of (3) to fit the data to a

straight line [36]. Those studies, and almost all others until 1997, dealt only with the line width until a paper appeared [38] that fundamentally changed the way we approached the studies of HSE and DD. In [38], an HSE-induced dispersion signal that is superimposed upon the traditionally studied absorption signal [39–42], was demonstrated to be capable of independently finding $K_{ex}C$ to a precision rivalling that of line width studies.

This opened the door to the separation of HSE and DD [27, 43]. Another independent method to separate HSE and DD by comparing the concentration broadening of ¹⁴N versus ¹⁵N nitroxides was developed in [44].

The use of Lowfit to obtain ΔH_{pp}^{L} , *I*, V_{pp} and V_{disp} , and *I* is rather involved, thus we provide a detailed example involving an experimental spectrum in the Supplemental Information. We highlight one technical problem due to a mismatch of the cavity often encountered with lossy solvents [45]. This mismatch, introduces some normal in-phase dispersion signal into the normally detected out-of-phase signal. V_{disp}/V_{pp} due to the mismatch, which we term "instrumental dispersion," has the same sign and magnitude for all three (two) manifolds, either positive or negative depending on the conditions. This allows us to correct for the instrumental dispersion for ¹⁴N by subtracting $V_{disp}^{cf}/V_{pp}^{cf}$ from the other two ratios yielding two independent values of corrected $V_{disp}^{man}/V_{pp}^{man}$, giving us a means to assess the systematic errors.

Unfortunately, for ¹⁵N, we only have two such ratios giving us just one corrected value, denoted simply as V_{disp} , as follows:

$$V_{\rm disp} = V_{\rm pp}^{\rm hf} \left[\frac{V_{\rm disp}^{\rm hf}}{V_{\rm pp}^{\rm hf}} - \frac{1}{2} \left(\frac{V_{\rm disp}^{\rm lf}}{V_{\rm pp}^{\rm lf}} + \frac{V_{\rm disp}^{\rm hf}}{V_{\rm pp}^{\rm hf}} \right) \right].$$
(9)

Our summary thus far has considered dominate HSE. Now, let us consider the case of dominant DD. The spectra are qualitatively similar to those in Fig. 1 except that the dispersion is negative; i.e., corrected $V_{disp}^{lf} < 0$ and $V_{disp}^{hf} > 0$. The reason for this difference in sign is that the transfer of phase coherence occurs without a phase change for HSE while for DD there is a change of phase of 180° [2]. Because they are of opposite sign, $V_{disp}^{DD} + V_{disp}^{HSE}$ can vanish over a (narrow) range of diffusion coefficients, *D*. This interesting effect has been observed experimentally with 14pD-Tempone at approximately 180 K and with 15pD-Tempone at approximately 283 K in 70 wt% aqueous glycerol, see Fig. 13 of [27]. Line shifts toward the center from HSE, which have proved to be a valuable resource for separating HSE and DD and for studying re-collision during one encounter can be large, especially when $K_{ex}C \cong \gamma A_o$. See Table 2 of [7]. For DD, these shifts are outward, but they are marginally measureable and have not yet proved to be of quantitative use. See Fig. 12 of [43] where just a hint of outward shift is discernable near $V_{disp}^{DD} + V_{disp}^{HSE} = 0$ before being overcome by the inward shift due to HSE.

Taking into account the sign change upon transfer of spin coherence, HSE and DD are treated theoretically on a similar footing at low H_1 . Within this framework we are able to think about the two interactions in broad terms but must keep in

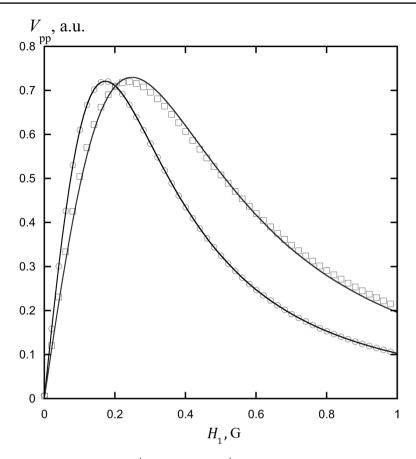


Fig. 1 CWS of V_{pp} for $\gamma T_1 = 10 \text{ G}^{-1}$ and $\gamma T_2 = 1.67 \text{ G}^{-1}$. Tempol pattern (squares) and Tempol pattern with $a_p = 0$ (circles); i.e., a Lorentzian. The two CWS are normalized to the same V_{pp} and the solid lines are fits to Eq. (4)

mind that DD shows very much smaller identifiable changes in the spectra. It's important to keep in mind that the extent of line broadening provoked by DD is limited by the solid state, closely packed value of 49 G/M [43] while only about one-half of this value has been found experimentally [27]. Thus, in varying D over a wide range from where HSE vs. DD is predominate, most measureable effects are dominated by HSE, see Fig. 2a of [44] and Fig. 7 of [27]. Finally, in comparing three methods mentioned above to obtain the relative contribution of HSE versus DD, the results were different for the three methods, outside of experimental error, although the broad features were reasonable, see Figs. 4, 6, and 7 of [44].

Another complication in studying DD arose when corrected values of $V_{\text{disp}}^{\text{lf}}/V_{\text{pp}}^{\text{lf}}$ and $-V_{\text{disp}}^{\text{hf}}/V_{\text{pp}}^{\text{hf}}$ were linear and equal to each other as functions of *C* up to about 30 mM, but they did not extrapolate to the origin [27]. The negative intercept [27] was nicely explained by Marsh [46] who showed that the pseudosecular electron-nuclear dipolar interaction also induced transfer of spin coherence for isolated nitroxides, albeit small and over a limited range of the diffusion coefficient.

In summary, at low H_1 , the theory of HSE has been amply confirmed by experiment, including the effect of re-collisions of the same pair during one encounter [47, 48]. We felt modestly confident of our understanding of HSE at small H_1 [6] and anticipated gaining a deeper understanding of the behavior of the absorption and dispersion components due to HSE under saturating conditions. On the other hand, our understanding of DD is not yet complete, either at low H_1 or under saturating conditions.

To recap the motivation for this work, we strive to learn how to study spin relaxation in systems where transfer of spin coherence is significant using continuous wave EPR with a typical standard CW spectrometer. To achieve this goal, we separate the absorption and dispersion components of experimental or theoretical spectra. We study the absorption components with the long established Bloch expressions (3)–(5) to permit comparison with literature results. We then study these same absorption components with the rigorous theory (17) and, in addition, study the saturation of the dispersion components.

A guide to procedures in this paper is as follows: all theoretical spectra are simulated using (17), next section. These spectra are then fit with Lowfit to obtain the theoretical parameters ΔH_{pp}^{L} , *I*, *V*_{pp} and *V*_{disp}. These same parameters are then obtained from the experimental spectra. The CWS of the absorption components ΔH_{pp}^{L} and *I* are then analyzed with the Bloch formulation utilizing (3) and (5), respectively, after establishing that the CWS of *V*_{pp} yields poor values of *T*₁. All four parameters ΔH_{pp}^{L} , *I*, *V*_{pp}, and *V*_{disp} are analyzed by direct comparison with (17). *T*₁ derived from the absorption parameters obtained from ΔH_{pp}^{L} and *I* using the Bloch approach and the direct comparison may be compared with each other and with the literature. *V*_{disp} may only be obtained with a rigorous theory such as (17) and there are no literature values.

2 Theory

2.1 General Formulation of the Spectral Manifestations of HSE and DD Interactions

The shape of the EPR spectrum of a radical with hyperfine structure due to an arbitrary number of magnetic nuclei in a relatively dilute solution is given by the following kinetic equations (e.g., [4] and references therein:

$$\frac{\partial M_k^-}{\partial t} = -i\left(\omega_k + \delta_k - \omega\right)M_k^- - \frac{M_k^-}{T_{2k}} - W_{sd}M_k^- + \varphi_k V_{sct}M^- - i\gamma H_1M_{kz}$$

$$\frac{\partial M_{kz}}{\partial t} = -\frac{M_{kz} - M_k^0}{T_1} - VM_{kz} + \varphi_k VM_z - \gamma H_1M_{ky};$$
(10)

here $M_k^- = M_{kx} - iM_{ky}$, $M^- = \sum M_k^-$, $M_z = \sum M_{kz}$ and,

$$V_{\text{sct}} = K_{\text{ex,sct}} C - \frac{1}{T_{\text{dd,sct}}}$$

$$W_{sd} = K_{\text{ex,sd}} C + \frac{1}{T_{\text{dd,sd}}},$$

$$V = K_{\text{ex,set}} C + \frac{1}{T_{\text{dd,set}}}$$
(11)

where

$$\frac{1}{T_{\rm dd,sd}} = \frac{1}{8} \gamma^4 \hbar^2 C \left(\frac{5}{4} J^{(0)}(0) + \frac{27}{2} J^{(1)}(\omega) + \frac{9}{4} J^{(2)}(2\omega)\right),\tag{12}$$

$$\frac{1}{T_{\rm dd,sct}} = \frac{1}{8} \gamma^4 \hbar^2 C \left(J^{(0)}(0) + 9 J^{(1)}(\omega) \right), \tag{13}$$

$$\frac{1}{T_{\rm dd,set}} = \frac{1}{16} \gamma^4 \hbar^2 C \left(J^{(0)}(0) - 9J^{(2)}(2\omega) \right), \tag{14}$$

where $\omega = \gamma H_0$ and $J^{(n)}(x)$ are spectral densities of the correlation functions for the dipole–dipole interaction, chapter 8 [49].

The expressions (12) - (14) are obtained under the assumption that $\omega \ge 10^{11}$ s^{-1} to satisfy the condition that $\omega \tau_D \gg 1$ and at the same time, $a_p \tau_D \ll 1$; here the characteristic time $\tau_D = b^2/2D$, with *b* the distance of closest approach between colliding paramagnetic radicals and *D* the diffusion coefficient of a single radical. Under these conditions the dipole–dipole interaction contribution terms practically do not depend on the index (*k*) of the hyperfine structure line (see Eq. (4.21) [50]).

In (10), the subscript k refers to the kth hyperfine component (e.g., for nitroxides: the nitrogen or one line in the proton superhyperfine structure); M_k^- is the transverse magnetization, φ_k is the statistical weight, T_{2k} is the transverse relaxation time when $C \rightarrow 0$, and ω_k is the resonance frequency of that component. The three rate constants in (11) are: spin dephasing, $K_{\text{ex,sd}}$; spin coherence transfer to the observed spin from the colliding spin, $K_{\text{ex,sct}}$; and spin excitation transfer during the bimolecular collision, $K_{\text{ex,set}}$, respectively. Frequency shifts due to the same interacting pair colliding multiple times during a single encounter [47, 48, 50, 51] are denoted by δ_k .

In general, the rate constants $K_{\text{ex,sd}}$, $K_{\text{ex,sct}}$, and $K_{\text{ex,set}}$ may be different; however, if during the bimolecular collisions all spin dependent interactions of paramagnetic particles can be neglected except HSE, the three are equal [41], a condition known as equivalent HSE. HSE between nitroxides is known to fulfill this requisite [2]; thus, the following assumes that $K_{\text{ex,sd}} = K_{\text{ex,set}} = K_{\text{ex}}$.

The intrinsic longitudinal spin lattice relaxation time is given by

$$\frac{1}{T_1} = \frac{1}{T_{10}} + \frac{1}{T_{1d}},\tag{15}$$

where

$$\frac{1}{T_{1d}} = \frac{9}{8} \gamma^4 \hbar^2 C \left[J^{(1)}(\omega) + J^{(2)}(2\omega) \right].$$
(16)

Note that the definition of T_1 (15) describes the direct relaxation to the lattice of a spin in the excited state. Other relaxation pathways are limited to those offered by HSE and/or DD. Often the same symbol is used in the literature to denote an effective relaxation rate. In the present theory, at $C \rightarrow 0.1/T_{1d} = 0$; however, calculations show that $1/T_{1d}$ is small for all C under the conditions of this experiment. Therefore, in practice, $T_1 = T_{10}$. Note that the present theory does not include other relaxation mechanisms at $C \rightarrow 0$, for example nitrogen nuclear spin flips of rate T_n^{-1} [52]. In the event that these relaxation pathways and perhaps others become important, then a relaxation rate measured at $C \rightarrow 0$ would not be equal to a relaxation directly to the lattice. Within the context of the present theory, T_1 is expected to remain constant as functions of C and T.

The details of the solution of Eq. (10) in the steady state, $\partial M_k/\partial t = 0$, (10) for equivalent HSE are solved in the Supplemental Information.

2.2 Solutions of the Kinetic Equations for Nitroxides

The spectra predicted by Eqs. (S6) and (S7) in the Supplementary Information are quite general encompassing hyperfine interactions due to any set of magnetic nuclei. For nitroxides, these nuclei are ¹⁵N (¹⁴N), protons (deuterons), ¹³C and occasionally others. Here, we specialize to the most common spin probe that is composed of only one nitrogen nucleus, a number of the order of 12 or more protons and/or deuterons and ignore all others.

The familiar EPR spectrum consists of 2I + 1 manifolds inhomogeneously broadened by protons (deuterons), spaced by the isotropic coupling constant, γA_0 where *I* is the nuclear spin of the nitroxide.

Solutions of Eq. (10) are presented via the values of S_i Eqs. (S6, S7) of the Supplemental Information which have the form:

$$S_i = \frac{1}{2I+1} \sum_{M=-I}^{I} \sum_m \phi_m P_{iMm} / F_{Mm}; \sum_m \phi_m = 1, i = 1, \dots, 5$$
(17)

where

$$P_{1Mm} = 1,$$

$$P_{2Mm} = (\omega - \omega_0 - \gamma A_0 M - \omega_m),$$

$$P_{3Mm} = (\omega - \omega_0 - \gamma A_0 M - \omega_m)^2,$$

$$P_{4Mm} = (1/T_{2M} + W_{sd}),$$

$$P_{5Mm} = (1/T_{2M} + W_{sd})^2,$$

$$F_{Mm} = \gamma^2 H_1^2 (1/T_{2M} + W_{sd})^2 + W_{1M} \left(\frac{1}{T_{2M}} + W_{sd}\right)^2 + W_{1M} (\omega - \omega_0 - aM - \omega_m)^2.$$
(18)

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In (17), *M* is summed over the nitrogen manifolds and *m* over the proton hfs. Note that, in writing $W_{1k} = W_{1M}$, we have assumed that all of the proton lines in manifold *M* have the same value of T_1 .

For the case of N equivalent protons, the resonance frequency of the *m*th proton line with respect to the center of each nitrogen manifold is given by

$$\omega_m = (m - N/2)\gamma a_p,\tag{19}$$

and the statistical weight is given by the binomial coefficients:

$$\phi_m = \frac{1}{2I+1} \frac{1}{2^N} \frac{N!}{(N-m)!m!}.$$
(20)

For the general case,

$$\omega_m = \sum_{\{k\}} \gamma a_k m_k. \tag{21}$$

For deuterons or other magnetic nuclei, (21) is carried out by the computer by constructing a "stick" diagram beginning with the 1st nucleus and placing $2I_1 + 1$ sticks spaced by a_1 . Then for each successive nucleus the next layer of sticks is imposed on the previous layer, etc. For *N* equivalent protons, for example, each successive layer results in a stick overlaying previous ones and leads to (19) and (20). In this work, (21) is used for the Tempol pattern and for deuterated nitroxides to demonstrate the validity of using the simpler pattern under the conditions of our experiment.

All calculations in this paper are performed with the rigorous theory, (10, 17). The resulting spectra are fit with Lowfit which yields the parameters to plot the CWS.

2.3 Notation

It is instructive to compare CWS found from the rigorous results from (17) to those assuming $a_p = 0$, the homogeneous case.

The notation has changed twice since the work in 2010 [1]. The first change, in 2016, [53] was noted in [6]. The original notation was preserved in [6, 27, 44]. The second change is in this work as follows:

$${}^{A}W_{\rm dd}C = \frac{1}{T_{\rm dd,sd}} + \frac{1}{2I+1}\frac{1}{T_{\rm dd,sct}},$$
(22)

and

$${}^{A}V_{\rm dd}C = -\frac{1}{2I+1}\frac{1}{T_{\rm dd,sct}},$$
(23)

where the left-hand side (LHS) is the notation of [6, 27, 44, 53] and the quantities in the right-hand side are defined in (12) and (13). Note that, unlike previous notations, $T_{dd set}^{-1}$ is a rate, not a rate constant; i.e., the concentration *C* is included in this rate.

2.4 Measureable Parameters at $H_1 \rightarrow 0$

For $H_1 \rightarrow 0$, in the absence of protons, the measureable parameters ΔH_{pp}^L and V_{disp}/V_{pp} are given in this notation as follows:

$$\Delta H_{\rm pp}^{\rm L}(C)_0 - \Delta H_{\rm pp}^{\rm L}(0)_0 = \frac{2}{\sqrt{3}} \left(\frac{1}{T_{\rm dd,sd}} + \frac{1}{2I+1} \frac{1}{T_{\rm dd,sct}} + \frac{2I}{2I+1} K_{\rm ex}C \right), \quad (24)$$

and

$$\pm \left(\frac{V_{\rm disp}}{V_{\rm pp}}\right) = \frac{4}{3\sqrt{3\gamma}A_0} \left(K_{\rm ex}C - \frac{1}{T_{\rm dd,sct}}\right),\tag{25}$$

where the + or – sign refers to the lf or hf, respectively. For saturated spectra, the effective spin–lattice relaxation time is the new measureable parameter. Foreseeing our experimental results that show that $T_{11f} \neq T_{1hf}$, we have extended Eq. (7) in the Supplemental Information for the case of ¹⁵N as follows:

$$T_{11f}^{eff} = T_{11f} \frac{1 + \frac{1}{2} \left(K_{ex} C + \frac{1}{T_{dd,set}} \right) T_{1hf}}{1 + \left(K_{ex} C + \frac{1}{T_{dd,set}} \right) \overline{T_1}},$$
(26)

where the factor 1/2 gives the statistical weight of one of the ¹⁵N manifolds and $\overline{T_1} = [T_{1lf} + T_{lf}]/2$. Interchange of the lf and hf gives the other relationship. Generalization of (15) yields

$$\frac{1}{T_{1M}} = \frac{1}{T_{10M}} + \frac{1}{T_{1d}}.$$
(27)

2.4.1 Approximations

The rates in (24)–(26) may be simplified in two limits. In the high-viscosity limit (HVL), [49] where $J^{(1)}(\omega_0) = J^{(2)}(2\omega_0) = 0$, $(T_{dd,sd})^{-1} = 5(T_{dd})^{-1}$, $(T_{dd,sct})^{-1} = 4(T_{dd})^{-1}$, and $(T_{dd,set})^{-1} = 2(T_{dd})^{-1}$. In the low-viscosity limit (LVL), $J^{(0)}(0):J^{(1)}(\omega_0):J^{(2)}(2\omega_0) = 6:1:4$; see after (VIII. 79) of [49]. We have argued the HVL is more appropriate and have shown that the difference in the HVL and LVL is rather small. See Fig. 5 of [44].

Thus, for the HVL, the important measurable parameters become

$$\Delta H_{\rm pp}^{\rm L}(C)_0 - \Delta H_{\rm pp}^{\rm L}(0)_0 = \frac{2}{\sqrt{3\gamma}} \left(\frac{5}{T_{dd}} + \frac{1}{2I+1} \frac{4}{T_{dd}} + \frac{2I}{2I+1} K_{ex}C \right), \quad (28)$$

$$\pm \left(\frac{V_{disp}}{V_{pp}}\right) = \frac{4}{3\sqrt{3\gamma}A_0} \left(K_{ex}C - \frac{4}{T_{dd}}\right).$$
(29)

For small H_1 , Eq. (29) is in accord with simulations for C = 0 and $C \gg \gamma a_p/K_{ex}$, outside of the proton intermediate zone. In the HVL, (26) becomes

$$T_{\rm llf}^{\rm eff} = T_{\rm 10lf} \frac{1 + \frac{1}{2} \left(K_{\rm ex} C + \frac{2}{T_{\rm dd}} \right) T_{\rm 10hf}}{1 + \left(K_{\rm ex} C + \frac{2}{T_{\rm dd}} \right) \overline{T_{\rm 1}}}.$$
(30)

where plus or minus sign in (29) corresponds to lf or hf, respectively.

2.5 Theoretical Spectra and CWS Curves

2.5.1 Negligible HSE and DD

To illustrate the content of our theory, we present some results and conclusions from the theory by way of simulations using (17) for $C \rightarrow 0$, approximated by $C = 10^{-6}$ M. These simulations of spectra are then fit with Lowfit to obtain the pertinent parameters. We call these the theoretical parameters with the understanding that they represent the content of Eq. (17) only to the precision afforded by the fits. All of the simulated spectra in this subsection share the following parameters ¹⁵ N; $A_0 = 23.7$ G, $\gamma T_1 = 10, 3.33$, and 1.67G⁻¹; $\gamma T_2 = 1.67$ G⁻¹; $K_{ex}C$ and $W_{dd}C$ negligible.

The validity of our approach rests upon the fidelity of the theoretical spectrum shape to the Voigt. It is well known that at small H_1 , the Voigt shape is insensitive to the particular hyperfine pattern for most nitroxides unless $\chi > 2$ [11]. Is this property maintained throughout the saturated region? We may answer this question by comparing spectra with the same Voigt shape and width; i.e., the same values of T_2 and χ but different hfi. As a test, we simulate two patterns. Pattern 1: H-Tempone with 12 equivalent protons, $a_p = 0.40$ G. For small H_1 this is the same spectrum treated in Fig. 1 of [6]. Pattern 2: 10 inequivalent protons with, $a_p = 0.44$ G (6H), 0.36 G (2H), and 0.48 G (2H), where the integers in the parentheses are the number of equivalent protons. We term this latter pattern "Tempol" for convenience because it encompasses the major values of a_p and gives the correct value of $\Delta H_{nn}^{G} = 1.4 \text{ G}$ for Tempol in water [11]. From Eq. (2) of [11], adopting the values of $\sqrt{\alpha} = 1.04$ for Tempol pattern and 1.03 for Tempone, the same value of $\Delta H_{pp}^{G} = 1.4$ G is obtained for the two nitroxides and therefore, the same value of $\chi = 2.0$, somewhat below the value of $\chi_{incip} = 2.3$ where proton structure may begin to be perceived [11]. Thus, the treatment of this pattern here and in [6] tests the theory for significant IHB.

The output of Lowfit is by default based on χ derived from the Universal Nitroxide pattern given in Table 5 of [11]. To correct to other patterns, Eqs. (11) and (7a) of [11] are used. A summary of the values of T_1 and T_2 obtained by the fits are given in Table 2. The maximum discrepancy in T_2 , 1.6%, occurs for $\gamma T_1 = 1.67 \text{ G}^{-1}$ which is a factor of more than 13 shorter than our experimental values. At $\gamma T_1 = 10$ G⁻¹, still a factor of 2 faster than experiment, the error is negligible. The maximum

Hyperfine pattern	γT_2 , G ⁻¹ Input	γT_1 , G ⁻¹ Input	$\gamma T_2, \mathbf{G}^{-1}$ $(\Delta \mathbf{H}_{\mathrm{pp}}^{\mathrm{L}})$	$\gamma T_1, \mathbf{G}^{-1}$ $(\Delta \mathbf{H}_{\mathrm{pp}}^{\mathrm{L}})$	$\gamma T_1, \mathbf{G}^{-1}$ (I)	$\gamma T_1, \mathbf{G}^{-1}$ (V_{pp})
Tempol	1.67	1.67	1.64	1.71	1.62	0.806
	1.67	3.33	1.65	3.41	3.25	1.60
	1.67	10	1.66	10.1	9.90	4.76
Tempone	1.67	1.67	1.67	1.68	1.63	0.806
	1.67	3.33	1.67	3.36	3.28	1.59
	1.67	10	1.65	10	10	4.75

 Table 2
 Relaxation times deduced from theoretical CWS by fitting to the parameter in the parentheses

Negligible HSE and DD

discrepancies in T_1 from the CWS of either ΔH_{pp}^L or I are 2–3%, which occur for short values of input $\gamma T_1 = 1.67 \text{ G}^{-1}$. For a more realistic value of $\gamma T_1 = 10 \text{ G}^{-1}$ the discrepancies are negligible. As expected, the values of T_1 from the CWS of V_{pp} are very poor. In summary, fit values of the relaxation times in the absence of spin diffusion for typical experimental conditions are negligibly different than the theoretical values and for faster times, are different by a few percent.

Plots of the CWS of ΔH_{pp}^{L} , *I*, and V_{pp} for Tempone and Tempol are exhibited in Fig. S1 of the Supplemental Information.

It is instructive to compare the CWS of V_{pp} for a Lorentzian line and an IHB line as shown in Fig. 1 which corresponds to $\gamma T_1 = 10 \text{ G}^{-1}$. The squares are for the Tempol pattern and circles for the same pattern except $a_p = 0$; i.e., a Lorentzian. The two CWS are normalized to the same maximum V_{pp} , V_{pp}^{max} , and the lines are fits to Eq. (4). The fit to the $a_p = 0$ case shows a maximum discrepancy of $1.6 \times 10^{-9} V_{pp}^{max}$ demonstrating that Eq. (9) is very accurate in the limit of $a_p = 0$. Let us define H_1^{max} as the value of H_1 at V_{pp}^{max} . It is clear that H_1^{max} increases due to IHB; i.e., it gives a first impression that T_1 is shorter due to IHB when in fact they have the same values of T_1 and T_2 . The CWS of V_{pp} yields the correct values for the homogeneous case but not for the IHB. Note that this effect is not due to a greater number of relaxation pathways for the IHB spectrum because there is no spin diffusion. We see that the fit of the IHB case is visually rather a good fit; however, the output value T_1 is more than a factor of two too short. In short, a reasonable fit to a CWS and/or the values H_1^{max} do not necessarily reveal a difference in spin relaxation.

Note that for nitroxides in liquids of low viscosity, Eq. 4 is expected to give a reasonable visual fit, because the values of χ are relatively small for unresolved lines [11]. Contrast this with CWS in solids or high-viscosity fluids where unresolved lines with values of χ much larger are often encountered, [9, 28, 30, 31, 54], and fits to Eq. (4) are very poor.

2.5.2 Appreciable HSE and/or DD

Some very interesting effects on the CWS are predicted by Eq. (17) at large values of $K_{ex}C$ and H_1 [2, 3] that we shall detail in future publications. In this work,

we confine our theoretical presentation to values of $K_{\rm ex}C/\gamma < 1.6$ G and $W_{\rm dd}C/\gamma < 0.40$ G, comparable to our experimental conditions.

Spectra were simulated as a function of H_1 by (17) for ¹⁵N with $A_0 = 23.74$ G employing typical parameters, $K_{\rm ex}/\gamma = 100$ G/M and $W_{\rm dd}/\gamma = 25$ G/M at C = 0, 0.5, and 16 mM. Input parameters of T_2 and T_1 , similar to the values observed in the experiment, different for If and hf, are given in Table 3. These spectra are IHB by 12 equivalent deuterons (nuclear spin 1, 25 lines) with $a_d = 0.061$ G, similar to the experiment, which yields, $\Delta H_{pp}^{G} = 0.359$ G, Eq. (8). Spectra were also simulated with 12 equivalent protons (nuclear spin 1/2, 13 lines) with $a_p = 0.0996$ G which yields the same value of ΔH_{pp}^{G} , Eq. (8). The maximum value of χ is $\chi = 2.4$. Under all conditions, the spectra and the parameters extracted from the CWS are negligibly different for the two isotopes; thus, for the purpose of simulating theoretical spectra either pattern may be used. Note that C = 0.5 and 16 mM yield $K_{ex}C/\gamma = 0.05$ and 1.6 G, respectively compared with $\gamma a_{p} = 0.0992$ G; i.e., just below and above the proton intermediate zone, respectively. Note that for $C \rightarrow 0$, these results are examples of negligible spin coherence transfer presented in the previous section; nevertheless, they are included in Tables 4 and 5 for comparison. The simulation assumed different T_1 values for low-, T_{11f} , and high-field, $T_{\rm lhf}$, lines. The kinetic Eq. (10) can be easily generalized to the case of different spin-lattice relaxation times of spins belonging to different components of the spectrum. Their solution in stationary conditions is found by standard methods. In the case of different T_1 , this solution is more cumbersome than Eqs. (17, 18). Thus, we do not give it here.

Figure 2 shows the effects of saturation on the absorption and dispersion components for C = 16 mM: i.e., $W_{dd}C/\gamma = 0.40$ G (**a** and **b**) and $K_{ex}C/\gamma = 1.6$ G (**c** and **d**). The unsaturated components at small H_1 are shown for **a** DD and for **c** HSE. The saturated components ($H_1 = 0.49$ G) are shown in **b** and **d** respectively. In Fig. 2, the observed spectra (not shown) would be the sums of the two components. In **b** and **d**, both the absorptions and the dispersions are saturated, but the dispersions less so, as may be judged by the relative heights of the two components. For clarity, the dispersion components are amplified relative to the absorption components as indicated and the baselines are truncated.

The broadening of all components by saturation may be appreciated comparing **a** with **b** and **c** with **d**. Furthermore, it is evident that the hf components are saturated less by comparing the relative heights of the lf and hf absorption components in **a** vs. **b** and **c** vs. **d**. This is due to the fact that $T_{1hf}T_{2hf} < T_{1lf}T_{2lf}$ for both the HSE and DD series.

Table 3 Input parameters	Series	$\gamma T_{1\mathrm{lf}}, \mathrm{G}^{-1}$	$\gamma T_{\rm 2lf},{ m G}^{-1}$	$\gamma T_{\rm 1hf},{\rm G}^{-1}$	$\gamma T_{\rm 2hf},{\rm G}^{-1}$
	HSE	29.4	7.75	21.7	6.10
	DD	43.5	2.72	38.5	1.10

 $K_{\rm ex}/\gamma = 100$ G/M or $W_{\rm dd}/\gamma = 25$ G/M

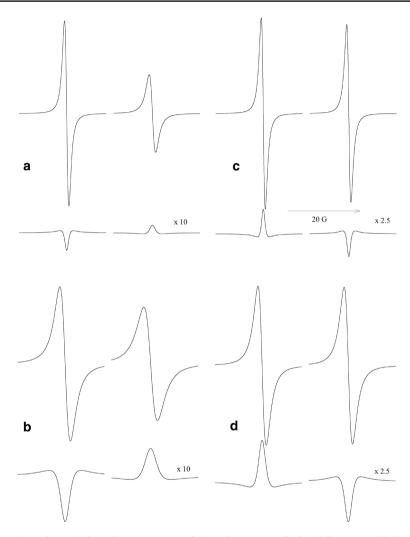


Fig. 2 Absorption and dispersion components of theoretical spectra of 16 mM Tempone with dominate DD, **a** and **b** and with dominate HSE, **c** and **d**. The spectra from which these components were derived (not shown) are the sum of the two components. Parts **a** and **c** are simulated at low H_1 and **b** and **d** at a saturating $H_1 = 0.49$ G. The baselines are truncated for clarity. The dispersions are amplified relative to the absorptions as indicated near their baselines. At high $H_1 = 0.49$ G, both the absorptions and the dispersions are saturated; however, the dispersion component less so. Compare the relative heights of the two components in **b** and **d** with those in **a** and **b**

2.5.2.1 CWS of \Delta H_{pp}^{L} Typical CWS of the lf of $\Delta H_{pp}^{L}(C)$ are presented in the Supplemental Information. The theoretical values of $\Delta H_{pp}^{L}(C)_{0}$ obtained from fitting simulated spectra are tabulated in columns 3 and 4 of Table 4. From Table 3, employing $\Delta H_{pp}^{L}(0)_{0} = 2/\gamma \sqrt{3}T_{2}$, we may calculate the input values of $\Delta H_{pplf}^{L}(0)_{0} = 0.149$ G and $\Delta H_{pplf}^{L}(0)_{0} = 0.189$ G for the HSE series and $\Delta H_{pplf}^{L}(0)_{0} = 0.425$ G

Series	<i>C</i> , mM	$\Delta H_{\rm pplf}^{\rm L}(C)_0$ Theory ^a	$\frac{\Delta H^{\rm L}_{\rm pphf}(C)_0}{\rm Theory^a}$	$\Delta H^{\rm L}_{\rm pplf}(C)_0$ Intercept ^b	$\Delta H^{\rm L}_{\rm pphf}(C)_0$ Intercept ^b	$\Delta H^L_{pplf}(C)_0$ No protons ^c	$\Delta H^{\rm L}_{\rm pphf}(C)_0$ No protons ^c
HSE	0	0.149	0.189	0.149	0.189	0.149	0.189
	0.5	0.203	0.239	0.183 (-10%)	0.224(-6%)	0.178 (-12%)	0.218 (-9%)
	16	1.09	1.13	1.10 (+1%)	1.14	1.07 (-2%)	1.11 (-2%)
DD	0	0.424	1.05	0.420	1.05	0.425	1.05
	0.5	0.442	1.07	0.438	1.07	0.445	1.07
	16	1.05	1.69	1.04 (-1%)	1.69	1.07	1.70

Table 4 Lorentzian line widths, G in the limit of $H_1 \rightarrow 0$

^aTrue values fit from simulations of (17)

^bFrom intercept of fits to (3)

^cFrom Eq. (28), assuming no protons

	-r		, / - _{11f} , _				
Series	C, mM	$ \begin{array}{c} T_{\rm llf}^{\rm eff} \left(\Delta H_{pp}^L \right) \\ {\rm Theory}^{\rm a} \end{array} $	$\gamma T_{\rm 1hf}^{\rm eff} \left(\Delta H_{pp}^L \right)$ Theory ^a	$\gamma T_{1lf}^{eff}(I)$ Theory ^b	$\gamma T_{1\mathrm{hf}}^{\mathrm{eff}}(I)$ Theory ^b	γT_{1lf}^{effc} No protons	$\gamma T_{\rm 1hf}^{\rm effc}$ No protons
HSE	0	29.2	21.6	29.4	21.6	29.4	21.7
	0.50	17.6	14.9	22.9	18.4	19.9	16.6
	16	12.2	12.0	14.7	14.4	12.9	12.7
DD	0	43.7	38.8	43.5	37.8	43.5	38.5
	0.50	40.0	35.6	39.3	34.9	39.6	35.4
	16	23.0	22.4	23.4	23.0	23.5	22.8

Table 5 spin–lattice relaxation times, γT_{11f}^{eff} , G⁻¹

For $C \rightarrow 0$, $T_{11f}^{eff} = T_1$

^aCWS of theoretical values fit to Eq. (3)

^bCWS of theoretical values fit to Eq. (5)

^cApproximation assuming no protons, (30)

and $\Delta H_{pplf}^{L}(0)_{0} = 1.05$ G for the DD series. Comparing these input values with those in columns 3 and 4 for $C \rightarrow 0$, the first row of the HSE or DD series, we see that the output (theoretical) and input values are identical. This verifies that our method of simulating and fitting to a Voigt produces accurate values of T_{2} . The final two columns of Table 4 show the approximate values assuming no protons. The values in Table 4 derived from the Universal and the correct map are within 1% of one another.

In Table 4, the discrepancies between the theoretical values and the other two methods are shown when they are > 1%; otherwise, the absence of parenthetical values indicates that the discrepancies are less than 1%. For the two non-zero values of *C*, significant discrepancies are noted between the true and approximate values as computed from Eq. (28). This is fully expected because Eq. (28) assumes no protons. Nevertheless, apart from the proton intermediate zone, where 6–10% discrepancies in the HSE series are incurred, the discrepancies are

very small. For the 16-mM results in the HSE series, they amount to only 1-2% and in the DD series they are negligible.

The fits of ΔH_{pp}^{L} also yield values of T_{1M}^{eff} which are denoted by $T_{1M}^{eff} \left(\Delta H_{pp}^{L} \right)$ and tabulated in columns 3 and 4 of Table 5. For C = 0, the errors are negligible when the correct map is employed; use of the Universal map leads to errors of 6 and 8% for lf or hf, respectively. The fits to Eq. (3) of all CWS are excellent except for those for C = 0.5 mM, HSE where $K_{ex}C/\gamma = 0.05$ G. Note that values of T_{1}^{eff} are available from the Bloch formulation but not the rigorous theory, (10, 17), because they are not an input (true) parameter. Results in the first and third rows and from Sect. 2.5.1 show that the Bloch and rigorous theory are the same for $C \rightarrow 0$. For C > 0, no comparison between the two theories is possible. Comparison of the CWS generated by (10, 17) and the fit to the Bloch Eq. (3), shown visually in Fig. S2 shows that, outside the intermediate proton zone, C = 0.5 mM, the curves are essentially identical. The discrepancies between the rigorous theory and the fit to (3) is less than 1% for both HSE and DD.

Similarly, the discrepancies between the CWS of I, shown in Fig. 3e, f below, are very small, less than 2% in the intermediate proton zone, and 1.2% elsewhere.

In summary, CWS of the absorption components calculated from (10, 17) are fit to high precision by the Bloch formulations, yielding values of T_{11f} and T_{1hf} that are same for $C \rightarrow 0$. Estimates of the values of T_1^{eff} observed in an experiment are only available from the Bloch formulation, unless simulations using (10, 17) of the CWS are found that are within about 2% of the observed values. We have not found such simulations for this first experiment because both C and I are rather small and lack the interesting effects alluded to in the first sentence of Sect. 2.5.2. Thus, in the following sections through Sect. 4.2, we develop in detail T_1^{eff} . In Sect. 4.3, we demonstrate the direct use of (10, 17) to analyze the same experimental data.

2.5.2.2 CWS of V_{pp} , V_{disp} , and I Figure 3 displays CWS of the lf of V_{pp} (**a** and **b**), V_{disp} (**c** and **d**), and I (**e** and **f**). The HSE series is depicted in **a**, **c**, and **e**; the DD in **b**, **d**, and **f**. All of the parameters are in arbitrary units; however, their relative values are indicated. In **b**, for example, Gain $\mathbf{a} \times 6$, means that the amplification is 6 times that in **a**. For clarity, the values are normalized to the same C; i.e., the increase in intensity due to an increase in C that would be observed in the experiment is discounted. In Fig. 3 only every other computed point is displayed; also, the line through the V_{disp} data is interpolated to guide the eye. The symbols are the theoretical values and the solid lines are fits of V_{pp} to Eq. (4) and I to Eq. (5). The parameters $\Delta H_{pp}^{L}(0)_{0}$ in these fits are taken from columns 5 and 6 of Table 4. It is important to be able to use the intercepts because they yield more precise values of $\Delta H_{pp}^{eff}(I)$, respectively, where the parameter in the parentheses indicates the CWS that is fit. The values of $\gamma T_{1lf}^{eff}(I)$ are tabulated in columns 5 and 6 of Table 5; the values of $\gamma T_{1lf}^{eff}(V_{pp})$ are in error by about a factor of 2 and are not reported. Approximate values of γT_{1lf}^{eff} were computed from Eq. (30), which assumes no protons, employing the input values given in Table 3. These are reported in columns

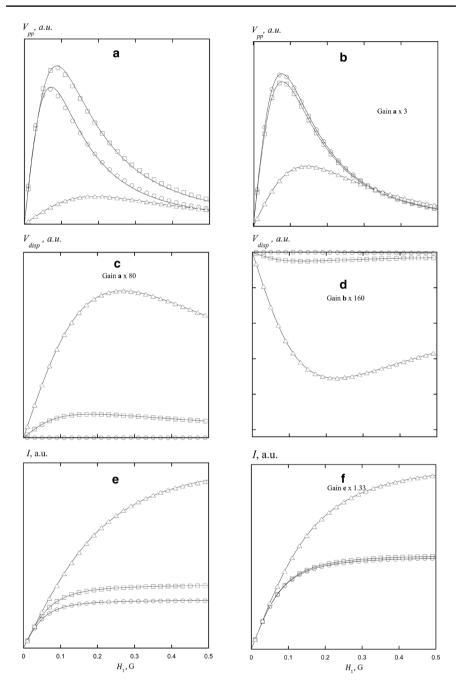


Fig. 3 CWS of the If of $V_{pp}(\mathbf{a}, \mathbf{b})$, $V_{disp}(\mathbf{c}, \mathbf{d})$, and $I(\mathbf{e}, \mathbf{f})$. The HSE series is depicted in $\mathbf{a}, \mathbf{c}, \mathbf{e}$; the DD in \mathbf{b}, \mathbf{d} , and $\mathbf{f}. C = 0$, circles; 0.5, squares; and 16 mM, triangles. All of the parameters are in arbitrary units; however, their relative values are indicated. In \mathbf{b} , for example, Gain $\mathbf{a} \times 6$, means that the amplification is 6 times that in \mathbf{a} . For clarity, the values are normalized to the same C; i.e., the increase in intensity due to an increase in C, which would be observed in the experiment, is discounted

7 and 8 of Table 5. Columns 3 and 4 report values of $T_1^{\text{eff}}\left(\Delta H_{\text{pp}}^{\text{L}}\right)$, which were alluded to in the previous section.

In Fig. 3 it is apparent that the dispersion component saturates less readily than the absorption component which we have already noted in Fig. 2. Figure 3 depicts the behavior of the lf lines; for hf, the sign of each of the dispersion components is the opposite and the results are similar.

In Table 5, at C = 0, the input values (Table 3), those from CWS(ΔH_{pp}^{L}), CWS(I), and the no-proton approximation are all negligibly different which shows that the simulations, the fits, and Eq. (30) are consistent. For DD, only small differences are noted for all C, however, for HSE, the theoretical values obtained from CWS(ΔH_{pp}^{L}) and CWS(I) for C = 0.5 mM are significantly different (19–23%) which is expected because $K_{ex}C = 0.05$ impinges on $\gamma a_p = 0.0992$ G. At C = 16 mM they are also different (17%) where $K_{ex}C = 1.6$ G. Interestingly, the no-proton estimates in this intermediate proton zone are about half-way between the CWS(ΔH_{pp}^{L}) and CWS(I) results.

In contemplating Fig. 3, note that the range of H_1 , up to 0.49 G, is more than three times what we were able to achieve while maintaining critical coupling of the cavity in this study of a lossy solvent. Therefore, much of the detail seen in Fig. 3 is not available in the present experiment. Under ideal conditions, our spectrometer is capable of producing values H_1 , up to 0.9 G.

3 Materials and Methods

4-Hydroxy-2,2,6,6-tetramethylpiperidine- d_{17} -1-¹⁵N-oxyl (purity 95%) was prepared from isotope-enriched triacetonamine-¹⁵N- d_{17} according to literature procedures [55]. Triacetonamine-¹⁵N was prepared from ¹⁵NH₄Cl (isotope enrichment 99.9%) according to the method by Pirrwitz and Schwarz [56] with minor modifications [57]. Glycerol (98%) and distilled water were used to prepare 60 wt% aqueous glycerol (60%AG). Samples from [6] stored in a refrigerator at 3 °C were used. As detailed in [6], a stock nitroxide solution with C = 50 mM was prepared gravimetrically and serially diluted. Non-degassed samples were drawn into 50-µL disposable pipettes and sealed at both ends with a flame. The samples extended through the entire cavity as described in [26]. References to H_1 mean effective values for a line sample in this configuration [26]. Only concentrations 0.03, 0.5, 5.0, 9.0, and 16.0 mM were used in this work.

EPR spectra were obtained at X-band at temperatures of 273, 298, 315, 340 K using a Bruker EMX Plus spectrometer equipped with a SHQ 4122 cavity and a standard temperature controller from Oxford, which had an accuracy of 0.1 K. Recording parameters of the CW EPR spectra are: modulation amplitude $a_{\rm m} = 0.1$ G, modulation frequency $f_{\rm m} = 100$ or 10 kHz, time constant 5.12 ms, conversion time 40 ms, field sweep 50 G, and resolution 50 mG. The CWS were obtained up

to 31.7 mW while preserving the critical coupling of the resonator. The conversion from the power incident on the critically coupled cavity, *P*, to H_1 was detailed in [26] using a standard sample of Fremy's salt. By measuring the Q-value with the present samples in the cavity, the conversion is given by $H_1 = 1.1\sqrt{P}$ with *P* in W and H_1 in G.

4 Experimental Results

Figure 4 displays typical experimental spectra for C = 16 mM obtained at 315 K: at $\mathbf{a} H_1 = 6.2$ mG and $\mathbf{b} 200$ mG. The amplification of the low-power spectrum \mathbf{a} relative to the higher-power spectrum \mathbf{b} is × 17 as indicated. The amplitudes of the dispersion components are amplified × 3 to show these components more clearly. In \mathbf{a} we see that instrumental dispersion, with a positive amplitude is superimposed upon the dispersion due to HSE and DD because $V_{\text{disp}}^{\text{lf}}/V_{\text{pp}}^{\text{lf}} > -V_{\text{disp}}^{\text{hf}}/V_{\text{pp}}^{\text{hf}}$ for these components. In \mathbf{b} we note an even more severe instrumental dispersion yielding a positive value of $V_{\text{disp}}^{\text{hf}}/V_{\text{pp}}^{\text{hf}}$ where it ought to be negative. The corrected values, by use of Eq. (9), yields $V_{\text{disp}}^{\text{lf}}/V_{\text{pp}}^{\text{lf}} = -V_{\text{disp}}^{\text{hf}}/V_{\text{pp}}^{\text{hf}}$ for both lines in \mathbf{a} as well as in \mathbf{b} . We observe

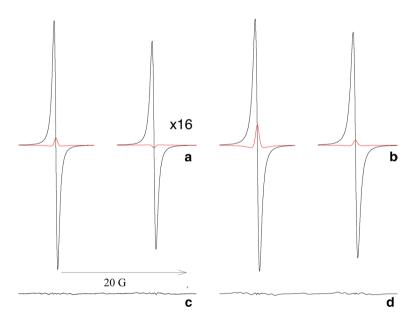


Fig. 4 Experimental absorption and overlaying dispersion component of 16-mM 15D-Tempol in 60 wt% aqueous glycerol at 315 K. **a** $H_1 = 6.2$ mG; **b** $H_1 = 200$ mG. **c**, **d** are the respective residuals. The base-lines are truncated for clarity. For clarity, the spectrum is not shown: it is the sum of the two components and the residual. Note that V_{disp}^{hf} for hf at the higher power is positive due to the larger instrumental dispersion; i.e., the cavity mismatch is more severe at the higher power. The corrected value, by use of Eq. (9), for both lines would be the normal $V_{disp}^{hf} < 0$ as is expected for this HSE-dominated spectrum. The amplification of the low-power spectrum **a** relative to the higher-power spectrum **b** is × 16 as indicated

that V_{disp} saturates less readily than V_{pp} in agreement with the theory, Figs. 3 and 4. Although it is not readily apparent on the scale of 4, the line widths in **b** are larger than those in **a** as expected. Similarly, it is not apparent that the nitrogen hyperfine spacing is larger in **a** than in **b** because the difference is less that the width of the printed line, but it is readily measureable.

The experiments were performed with modulation frequency, $f_m = 100$ kHz; however, one brief experiment compared the CWS of C = 0.05 mM at 10 kHz to assure that slow passage was maintained. See [26] and references therein. The most sensitive comparison is made with V_{pp} despite the fact that we do not expect accurate results for T_1 from the CWS of this parameter. The values of $\Delta H_{pp}^L(C)_0$ are the same to within 1 mG at the two frequencies, thus a difference in H_1^{max} is due to a difference in T_1 . Figure 5 shows the results for the lf; the hf results are similar. The solid lines are fits to Eq. (3) of the 100-kHz data and the dashed lines to the 10-kHz data. These fits are approximate because the lines are IHB; however, they serve to guide the eye. Our conclusion is that the 273 K CWS appears to saturate less readily at 100 kHz most likely due to the lack of time to respond to the saturation H_1 at the higher frequency. At the other temperatures, the coincidence at the two frequencies is satisfactory. This same conclusion applies to the hf.

For unsaturated spectra, the well documented procedures [6, 27, 43, 44] to separate HSE and DD were employed to find the rate constants given in Table 6. In earlier studies, we employed a single value of small H_1 , whereas here, we improved the precision of the measurements by measuring the intercepts of CWS as described in [26]. As an example, Fig. 6 illustrates the improvement in precision for $\Delta H_{pp}^{L}(C)_{0}$. The rate constants tabulated in Table 6 are within experimental uncertainty of the fit values in [6] for the three coincident temperatures. Values obtained from the "two-point method" [6] are consistently somewhat above these values. The uncertainties are larger here due to a smaller number of concentrations studied.

For experimental CWS results given in Tables 7, 8, 9, 10 and 11, the output from Lowfit was corrected using the correct Tempol map [11].

4.1 Negligible HSE and DD

These results were obtained from the sample at C = 0.03 mM approximating $C \rightarrow 0$. We use the notation $C \rightarrow 0$ to refer to these results. As expected, the dispersion amplitudes were negligible. Figures 7 and 8 show the CWS of ΔH_{pp}^{L} and *I*, the doubly-integrated intensity, respectively. The correlation coefficients, *r*, are given in the captions, showing that the fits of ΔH_{pp}^{L} are good and those of *I*, are excellent. From Fig. 6, we obtain values of $\Delta H_{pplf}^{L}(0)_{0}$, Table 7, from which values of T_{2} are obtained, Table 8.

From Fig. 7, we see that values of the product T_2T_1 are different for lf and hf, at all temperatures. The fits of ΔH_{pp}^{L} to (2) yield T_{10lf} , T_{10hf} , and $\Delta H_{pp}^{L}(0)_0$ from which $T_2 = 2/\left[\sqrt{3\gamma}\Delta H_{pp}^{L}(0)_0\right]$. The fits of *I* to (5), after fixing the values of the values of T_2 obtained from Fig. 5, yield another set of T_{10lf} , T_{10hf} , and the

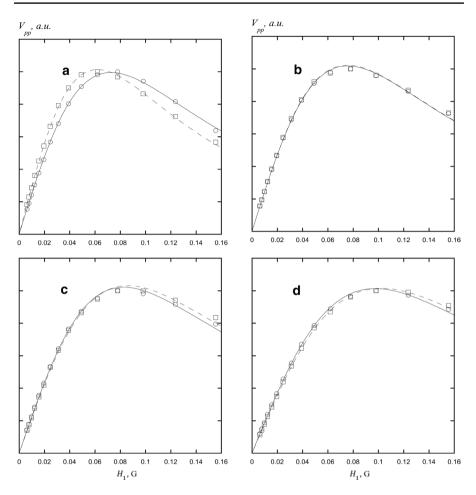


Fig. 5 CWS of V_{pp} of the *lf* of C = 0.5 mM normalized to unity, taken with modulation frequency 100 kHz, circles and 10 kHz, squares at 273 K, **a**; 298 K, **b**; 315 K, **c**; and 340 K, **d**, respectively. The solid lines are fits to (3) for $f_m = 100$ kHz and the dashed for 10 kHz, where f_m is the modulation frequency. The fits are approximate for these IHB spectra; however, they serve to guide the eye. The values of $\Delta H_{n}^{L}(C)_{0}$ are independent of f_m to high precision, ~ 1 mG. The hf show similar behavior

parameter K_I which is proportional to the doubly-integrated intensity for the unsaturated spectra. Table 9 tabulates the results from the CWS of *I*. Details of the variation of K_I with temperature are not presented; however, it is near that predicted by the Boltzmann factor.

We observe that values of T_1 are very different when derived from the CWS of ΔH_{pp}^{L} or *I*, in stark contrast to the results in Table 2. Observe that these differences may not be attributed to complications near the deuteron intermediate zone which is $a_d = 0.06$ G compared with the largest value of $K_{ex}C/\gamma = 0.003$ G.

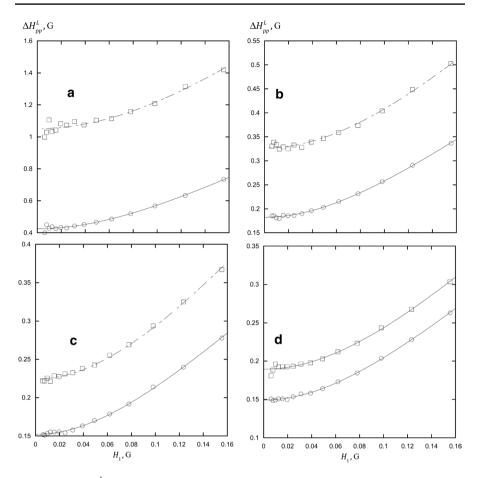


Fig. 6 CWS of ΔH_{pp}^{L} for C = 0.03 mM at **a** 273 K, **b** 298 K, **c** 315 K, and **d** 340 K; circles, If and squares, hf. These fits were good with r = 0.976 (273 K, hf), 0.994 (273 K, lf), 0.996 (298 and 340 K, hf), and 0.999 for all other temperatures and lines. Note the gain in precision from finding the intercepts, $\Delta H_{pp}^{L}(0)_{o}$, from which to calculate values of T_{2} rather than relying on the value at one small H_{1}

Т, К	k	<i>B</i> ′, G/M	$K_{\rm ex}/\gamma, {\rm G/M}$	$W_{\rm dd}\gamma,{ m G/M}$
273	0.03 ± 0.09	34.9 ± 3.2	14.3 ± 2.6	23.1±3.7
298	0.60 ± 0.03	33.4 ± 2.3	33.0 ± 3.3	12.4 ± 1.4
315	0.90 ± 0.04	39.3 ± 1.9	51.0 ± 4.4	8.53 ± 1.2
340	1.15 ± 0.04	56.7 ± 2.6	87.9 ± 7.5	5.12 ± 1.4

4.2 Appreciable HSE and DD

Table 6 Rate constants

0.03 mM

The experimental CWS for ΔH_{pp}^{L} and *I* for C = 0.5, 5, 9, and 16 mM are plotted in Fig. 9, symbols. Except for one outlier, the Bloch fits to those data are even better

Table 7 Intercepts of the CWS of $\Delta H^{\rm L}_{\rm pplf}(0)$	Т, К	$\Delta H^{\rm L}_{\rm pplf}(0)_0$	$\Delta H^{\rm L}_{\rm pphf}(0)_0$
	273	0.445 ± 0.004	1.084 ± 0.007
	298	0.183 ± 0.001	0.342 ± 0.002
	315	0.149 ± 0.001	0.231 ± 0.001
	340	0.146 ± 0.001	0.193 ± 0.001

Units, G, C = 0.03 mM

Table 8	Spin relaxation	times
from CV	VS of ΔH_{pp}^{L}	

Table 9Spin relaxation timeand K_I, from CWS of I

Т, К	γT_{2lf}^{a}	$\gamma T_{2\mathrm{hf}}{}^{\mathrm{a}}$	γT_{10lf}^{a}	$\gamma T_{10\mathrm{hf}}{}^{\mathrm{a}}$
273	2.59	1.07	31 ± 1	31 ± 2
298	6.30	3.38	17.9 ± 0.3	16.7 ± 0.5
315	7.76	5.01	15.0 ± 0.2	15.1 ± 0.3
340	7.89	6.00	13.2 ± 0.2	11.9 ± 1

^aUnits, G^{-1} , C = 0.03 mM

C, mM	Т, К	$\gamma T_{\rm 10lf},{\rm G}^{-1}$	$\gamma T_{\rm 10hf},{\rm G}^{-1}$	K _I ^a
0.03	273	46 ± 1	43 ± 1	1.00 ± 0.01
0.03	298	39 ± 1	31.2 ± 0.7	0.876 ± 0.04
0.03	315	35 ± 1	25.7 ± 0.6	0.818 ± 0.03
0.03	340	25.8 ± 0.4	20.7 ± 0.2	0.771 ± 0.01

C = 0.03 mM. Uncertainties, propagated fit errors

^aRelative values of the slope of I at small H_1 . These initial slopes give relative values of the intensity which are similar to the expected change in the Boltzmann factor

than these quantities for $C \rightarrow 0$ in Figs. 7 and 8 respectively, with *r* near 0.999 for ΔH_{pp}^{L} and 0.9999 for *I* over all concentrations. There was one outlier at $H_1 = 0.062$ where Lowfit did not find a fit to a Voigt and thus is invalid. Eliminating this point in the fit to the CWS resulted in r = 0.999; including it, r = 0.993. These Bloch fits are not shown because the differences in the fits and the data are imperceptible on this scale, but the results are given in Tables 10 and 11.

The solid lines are direct comparisons with the rigorous theory which are described in the following section.

4.3 Direct Comparison of the CWS with the Rigorous Theory

This approach allows us to directly compare experimental CWS and rigorous CWS from Eqs. (10, 17) for any parameter that we wish to measure, not being constrained to just ΔH_{pp}^{L} and *I*. In Figs. 9, 10, 11, the solid lines are obtained by simulating spec-

The Effect of Power Saturation of	n the Line Shapes of Nitroxide
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Table 10 T_1^{eff} from Bloch fitCWS of I	C, mM	Т, К	$\gamma T_{11f}^{eff}(I)$	$\gamma T_{\rm 1hf}^{\rm eff}(I)$	K _I ^b
	0.50	273	52 ± 1	44.4 ± 0.7	1.00 ± 0.027
	0.50	298	36.2 ± 0.8	30.0 ± 0.7	0.730 ± 0.013
	0.50	315	27.6 ± 0.5	22.4 ± 0.2	0.630 ± 0.008
	0.50	340	18.4 ± 0.3	15.9 ± 0.2	0.602 ± 0.003
	5.0	273	58.2 ± 0.9	53.6 ± 0.8	1.000 ± 0.016
	5.0	298	31.9 ± 0.7	28.1 ± 0.5	0.671 ± 0.014
	5.0	315	21.9 ± 0.4	19.6 ± 0.3	0.607 ± 0.010
	5.0	340	13.3 ± 0.2	12.0 ± 0.1	0.581 ± 0.006
	9.0	273	50.7 ± 0.4	51.6 ± 0.6	1.000 ± 0.006
	9.0	298	22.3 ± 0.2	21.0 ± 0.3	0.589 ± 0.006
	9.0	315	14.3 ± 0.2	13.4 ± 0.2	0.517 ± 0.005
	9.0	340	8.9 ± 0.2	8.5 ± 0.1	0.521 ± 0.002
	16	273	48 ± 3	44 ± 5	1.000 ± 0.023
	16	298	26.9 ± 0.2	27.6 ± 0.5	0.856 ± 0.004
	16	315	11.5 ± 0.1	11.8 ± 0.2	0.600 ± 0.004
	16	340	7.1 ± 0.2	7.2 ± 0.3	0.578 ± 0.004

Fits to (3), Units, G⁻¹

^aRelative values of the slope of the CWS at small H_1

Table 11 $\Delta H_{pp}^{L}(C)_{0}$, G, and γT_{1}^{eff} , G⁻¹, from Bloch fits of CWS of ΔH_{pp}^{L}

<i>C</i> , mM	<u>рр 7, К</u>	$\gamma T_{1\mathrm{lf}}^{\mathrm{eff}}$	$\gamma T_{1\mathrm{hf}}^{\mathrm{eff}}$	$\frac{\Delta H^{\rm L}_{\rm pplf}(C)}{\Delta D^{\rm L}_{\rm pplf}(C)}$	$\Delta H^{\rm L}_{\rm pphf}(C)_0$
0.50	273	34.3 ± 0.7	36.5 ± 0.7	0.357 ± 0.002	0.824 ± 0.002
0.50	298	16.4 ± 0.2	15.4 ± 0.4	0.174 ± 0.000	0.295 ± 0.001
0.50	315	12.6 ± 0.3	11.3 ± 0.2	0.159 ± 0.001	0.226 ± 0.001
0.50	340	10.0 ± 0.2	8.9 ± 0.1	0.180 ± 0.001	0.216 ± 0.001
5.0	273	40.7 ± 0.8	44.4 ± 0.4	0.459 ± 0.003	0.960 ± 0.002
5.0	298	13.1 ± 0.2	14.1 ± 0.2	0.299 ± 0.001	0.416 ± 0.001
5.0	315	9.07 ± 0.09	9.3 ± 0.2	0.317 ± 0.000	0.378 ± 0.001
5.0	340	7.4 ± 0.1	7.5 ± 0.1	0.401 ± 0.001	0.431 ± 0.001
9.0	273	39.8 ± 0.7	44.4 ± 0.4	0.591 ± 0.002	1.12 ± 0.001
9.0	298	11.9 ± 0.1	12.8 ± 0.1	0.443 ± 0.001	0.564 ± 0.001
9.0	315	8.68 ± 0.09	8.8 ± 0.2	0.485 ± 0.000	0.549 ± 0.001
9.0	340	8.2 ± 0.2	8.1 ± 0.1	0.633 ± 0.001	0.671 ± 0.001
16	273	26.8 ± 0.4	25 ± 1	0.822 ± 0.001	1.375 ± 0.004
16	298	21.0 ± 0.2	21.1 ± 0.2	0.697 ± 0.001	0.856 ± 0.001
16	315	10.1 ± 0.2	9.9 ± 0.2	0.776 ± 0.001	0.852 ± 0.001
16	340	8.4 ± 0.3	8.3 ± 0.2	1.06 ± 0.002	1.096 ± 0.001

Fits to (5)

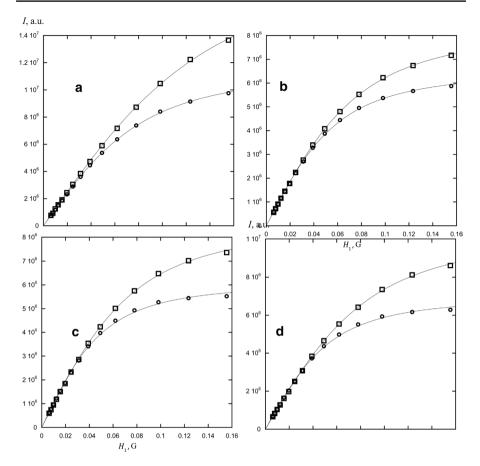


Fig. 7 CWS of *I* for C = 0.03 mM at a 273 K, b 298 K, c 315 K, and d 340 K; circles, lf and squares, hf. These fits were excellent with r = 0.9994 (315 K, lf), 0.9995 (298 K, lf), 0.9999 (340 K, *lf*), and 0.9999 for all other temperatures and lines

tra using (10, 17), fitting them with Lowfit, and constructing the CWS. The parameters T_{10} and T_2 for lf and hf, and K_{ex} , and W_{dd} were varied to find the best overall fit to all of the data according to our judgement. To obtain the eye fits, we begin with the parameters in Table 6. We were able to constrain T_{10} and T_2 to constant values independent of *C*. The direct comparison offers the advantage of exploiting V_{pp} and V_{disp} which are more rapidly varying functions of $T_1T_2H_1^2$ than ΔH_{pp}^L or *I*, therefore, more sensitive to global fitting. Note that for most concentrations and temperatures, V_{pp} attains a maximum or nearly a maximum, whereas for ΔH_{pp}^L or *I* we must rely on less definitive regions of H_1 . We have not yet attempted the type of curve-fitting analysis in Sect. 4.2 for V_{disp} . Note that a severe test of the theory, is the CWS of V_{disp} . The ratio V_{disp}/V_{pp} relies not only on the correct dependence on H_1 , but also the correct values of K_{ex} and W_{dd} . Counterbalancing these advantages is that the uncertainties are more difficult to estimate.

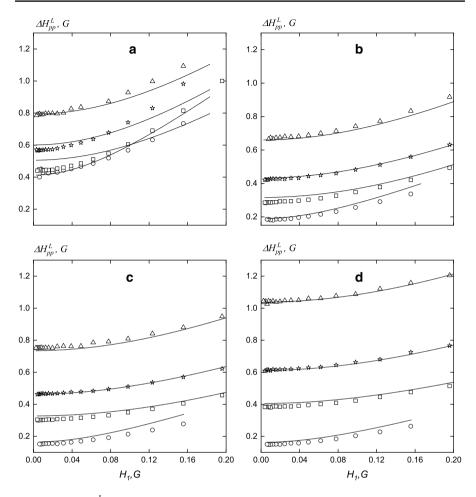


Fig. 8 CWS of ΔH_{pp}^{L} at **a** 273, **b** 298, **c**, 315, and **d**, 340 K. Circles, 0.03; squares, 5; stars, 9; and triangles, 16 mM. The solid lines are eye-fit theoretical curves, Eq. (17), with the parameters given in Table 12. At each temperature, T_{10} , T_2 , K_{ex} , and W_{dd} are maintained constant. Fits to the Bloch approach, Eq. (3), pass through data well within the size of the symbols and therefore are not shown

The parameters obtained by direct comparison are tabulated in Table 12.

Figures 10, 11, 12 are in arbitrary units; in Fig. 9, the quantities are all on the same scale and the same is true in Fig. 10. In Fig. 11, the results for V_{disp} are amplified relative to those in Fig. 10 by the factors shown as Gains. For example, at 273 K, the values of V_{disp} , Fig. 11a, are about 100 times less intense than the corresponding values of V_{pp} , Fig. 10a. It is astonishing that such small signals may be separated from the overall signal, but that fact is at the heart of being able to use the dispersion signal effectively.

The eye fits to $V_{\rm pp}$ are rather impressive, considering the constraints, rivaling those in Fig. 5, except at 273 K. More impressive, in view of the fact that it's the first time that it has been studied, the eye fits to $V_{\rm disp}$, again with the exception of 273 K,

are remarkably good, showing that the theory predicts the ratio $V_{\text{disp}}/V_{\text{pp}}$ both as functions of T_{10} , T_2 , K_{ex} , and W_{dd} , as well as H_1 .

A criticism of the measurements at 100 kHz at 273 K, is that Fig. 5a shows that H_1^{max} is larger at 100 kHz than at 10 kHz. Measurements at 5 kHz, not shown, are the same as those at 10 kHz. In Fig. 10a, we expect that a small part of the discrepancies in H_1^{max} is due to passage effects; however, correction of these discrepancies would move the experimental points to even lower H_1^{max} by a small amount and would increase the true discrepancies. Thus the discrepancies in Fig. 10a demand an explanation that we cannot yet provide.

5 Discussion

This project to investigate each component of a spectrum separately, with or without HSE/DD interactions, is feasible because all of the lines, experimental and theoretical, are excellent Voigts which may be fit to high precision. Fortunately, in extending the theory and experiments to saturating values of H_1 the lines continue to be excellent Voigts. This is not to say that an analysis would be impossible by other means, only that a rapid, automated procedure to deal with large numbers of samples and spectra opens the door to feasible extensive investigations. Furthermore, because the absorption and dispersion components are orthogonal functions, they may be separated to high precision, even when the latter is very much smaller that the former.

Equipped with values of $\Delta H_{\rm pp}^{\rm L}$, I, $V_{\rm pp}$, and $V_{\rm disp}$, we employ two approaches to estimate T_2 and T_1 from the CWS. Approach 1 employs fitting the CWS of ΔH_{pp}^L and I, theoretical and experimental, to the Bloch Eqs. (3) and (5). This procedure is justified because, when applied to theoretical spectra, the results are the same as the known input values to Eq. (10, 17) for $C \rightarrow 0$, Table 2. This approach offers the advantage of objective and consistent estimates of T_2 and T_1 together with objective estimates of the errors in the usual manner [58]. Because V_{pp} from the Bloch approach yields values of T_1 that are in error by about a factor of two is a significant disadvantage. Approach 2 compares the CWS, experimental (symbols) and theoretical (lines), Eq. (17), of all four parameters searching for a global fit, by eye. An advantage is that V_{pp} is directly measureable from the spectrum with good precision at small rates of transfer of coherence transfer (small C). Because V_{pp} is a more rapidly varying function of H_1 than ΔH_{pp}^L and I leading to more confidence in the fits. Perhaps more importantly, approach 2 affords the only way to study the CWS of dispersion. The significantly lower precision in finding correct eye fits and no objective way to access the uncertainties in T_{10} will make it difficult to distinguish different models of spin relaxation; i.e., different spin relaxation mechanisms in the kinetic equations.

In applications where only relative values of T_1^{eff} are needed, the Bloch approach for V_{pp} may be useful; however, one would need the relative values of T_2 because $T_1^{\text{eff}} \cdot T_2$ determines the saturation.

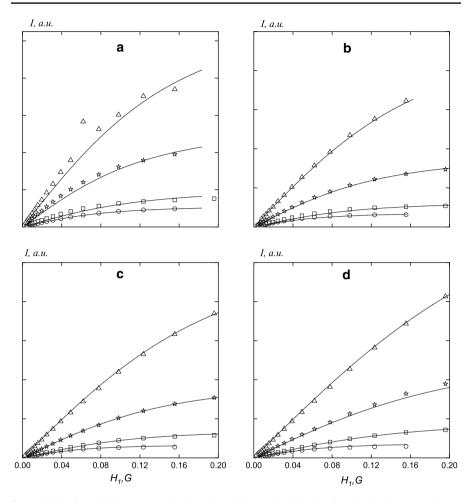


Fig. 9 CWS of I with the same symbols and conditions as in Fig. 8. After eliminating the outlier at 273 K (see text), fits to the Bloch approach, Eq. (5), pass through data well within the size of the symbols and therefore are not shown

The ability to study the CWS of $V_{\rm disp}$ was our primary motive to revive the CWS method to study T_{10} . In contemplating studies of $V_{\rm disp}$, we frankly did not know what to expect in light of Portis' observation that the in-phase dispersion showed no saturation while the absorption saturated readily [28]. We wondered if the relatively small values of H_1 available from a standard commercial spectrometer, especially with low Q-values due to lossy samples, would be sufficient to observe the saturation? Preliminary studies and this work (Fig. 11) proves the viability of this approach; however, we observe that at higher values of C and/or less viscous solvents where shorter values of T_{10} are expected, it may be more difficult. We currently do not have a physical view of the saturation of the dispersion, much less an appropriate trial fit function. However, the theory, Eqs. (10, 17), predicts its behavior

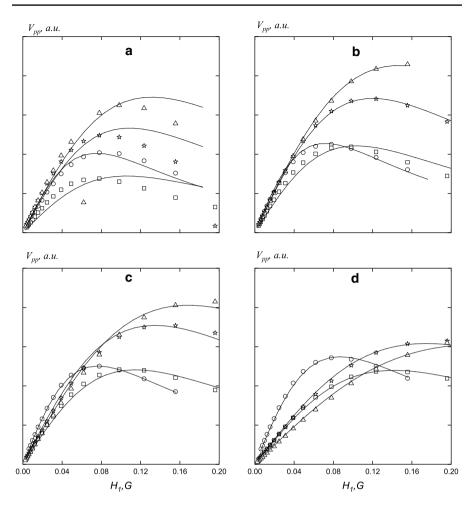


Fig. 10 CWS of V_{pp} with the same symbols and conditions as in Fig. 8. Fits to the Bloch approach, Eq. (4), yield rather good fits, but result in invalid values of T_1

with surprising accuracy keeping in mind that the eye fits that reproduce the CWS of $V_{\rm pp}$ yield the fits to $V_{\rm disp}$ without any further adjustment. Stated differently, the same value of T_1 describes the saturation of both the absorption and the dispersion. Even at 273 K, Fig. 11a, which shows poor fits at higher values of H_1 , are intriguingly similar at lower values.

5.1 Predictions of the Theory

5.1.1 Values of T_{10}

From the theory, we have learned that Eqs. (3) and (5), which are derived assuming Lorentzian lines, may be used to fit IHB spectral lines in the limit of $C \rightarrow 0$; i.e., in

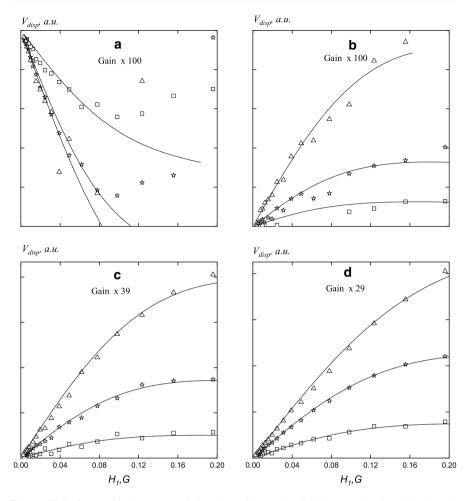


Fig. 11 CWS of V_{disp} with the same symbols and conditions as in Fig. 8 except that, for clarity, the values are amplified relative to Fig. 10 by the factors indicated. Importantly, the solid lines are given by the same values of the parameters in Table 12 as the fits to the other parameters. In particular, the experimentally accessible parameters $V_{\text{disp}}/V_{\text{pp}}$ are predicted by (17) rather well

Т, К	$K_{\rm ex}/\gamma,{ m G/M}$	$W_{\rm dd}\gamma,{ m G/M}$	$\gamma T_{\rm 10lf},{\rm G}^{-1}$	$\gamma T_{10\mathrm{hf}},\mathrm{G}^{-1}$	$\gamma T_{\rm 2lf},{ m G}^{-1}$	$\gamma T_{\rm 2hf},{ m G}^{-1}$
273	8	13	42	39	2.7	1.1
298	30	7.5	29	24	6.33	3.53
315	51	3.8	23	21	7.58	5.15
340	95	0	18	15	7.75	6.10

Table 12 Parameters from eye fits

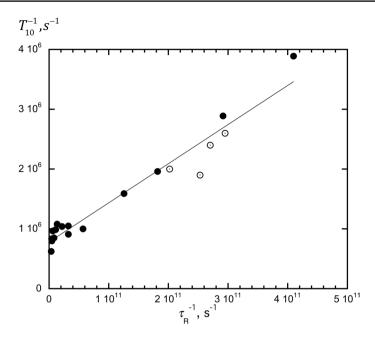


Fig. 12 Comparing spin-lattice relaxation rates from the literature for pD-Tempone in toluene. Open circles, IR [60] and closed circles, CWS [33]. Solid line, fit to combined data

the absence of HSE or DD. Thus, T_1 derived from the CWS of ΔH_{pp} or from *I* for $C \rightarrow 0$ is the same theoretically. See Table 2 and the first rows of the HSE or DD series, Table 5. This result was expected from the simple arguments given in the Introduction. This validates our approach of presenting theoretical results from fitting theoretical simulations and encourages us to take theoretical results for C > 0 to be valid.

5.1.2 Values of T_1

Except for the intermediate proton zone for HSE the theoretical values of $T_1^{\text{eff}}(\Delta H_{\text{pp}}^{\text{L}}) \approx T_1^{\text{eff}}(I)$, Table 5. Fig. S3 of the Supplemental Information is a plot of these theoretical results. Note that T_1^{eff} decreases very rapidly at low *C*. For DD, $T_1^{\text{eff}}(\Delta H_{\text{pp}}^L) \approx T_1^{\text{eff}}(I)$ for all *C*; however, keep in mind that the rates of transfer of spin coherence are significantly smaller. For HSE in the intermediate proton zone, perhaps just by numerical accident, the no-proton approximation lies about midway between the other two.

Both CWS(ΔH_{pp}^{L}), e.g. [33] and CWS(*I*) e.g. [59] have been proposed as methods to obtain T_{1}^{eff} . Which, if either, is correct under the rather simple assumptions of Eq. (17)? The no-proton approximation is expected to yield values of T_{1}^{eff} that are longer than if protons are included because the latter provides more relaxation pathways. This expectation argues against using CWS(*I*); however, we do not yet have enough information to exclude it.

The theory offers us the opportunity to carry out global fits under conditions that we may specify. For example, the eye fits in Figs. 9, 10, 11 and 12, which assume that, at a given temperature, the same values of T_{10} , T_2 , K_{ex} , and W_{dd} govern the CWS of all four parameters, ΔH_{pp}^{L} , I, V_{pp} , and V_{disp} are not perfect, but promising. One could relax any one of these in search of a better fit, or introduce a new parameter in the future to test. These eye fits are tedious and subjective, but may provide clues to improve the theory or the experimental design.

5.2 Results from the Experiments for Absorption

5.2.1 Values from Pulse vs. CWS Measurements

Our literature search did not find results where both CWS and pulsed EPR measurements of Tempol in the same solvent carried out by the same lab. In fact, although our search was not as rigorous for other nitroxides, we did not come across any such data for any spin probe-solvent pair. The only data that we found employing the two approaches for Tempol were in toluene which are displayed in Fig. 12. The solid circles show values of T_1^{-1} derived from CWS (ΔH_{pp}^L) and the open circles derived from IR. The straight line is a fit to the combined data. Note that Figs. 13 are presented on linear scales permitting a better visual comparison of the data than log scales which are often used. Figures 13 do not yet show that pulsed and CWS data are the same because more data is required to assess the matter. They only show that the results from CWS are reasonable.

5.2.2 Values of T₁₀

Reducing $C \to 0$ yields T_{10} provided that relaxation pathways other than HSE/DD are not effective; however, [52] has provided evidence that nitrogen nuclear spin flips at rate T_{1n}^{-1} begin to compete with T_{10}^{-1} for $\tau_{\rm R} > 0.1$ ns. Taken at face value, Fig. 3 of [52] shows that $T_1^{\rm eff} \to T_{10}$ only at 340 K; at lower temperatures, T_{10} would be longer after taking into account T_{1n} . In other words, because our present theory does not include T_{1n} , as T decreases, our values of T_1^{-1} may be increasingly smaller than the data points in Fig. 13.

Figure 13 compares the values of T_{10} from the present work with some from the literature: **a** CWS and **b** time domain. Rotational correlation times were computed from the data collected in [6] maintaining the full spectral densities; e.g., Eq. (5.61) of [10]. The results were averaged over 5 concentrations 0.2–40 mM. The value of τ_R for 315 K was found by interpolation between 298 and 323 K.

In considering Fig. 13a, we note that we used a standard sample of Fremy's salt to calibrate our values of H_1 , as described in detail in [26] which employs the same values of T_{10} used in Hwang's work, [33]. The estimated relative accuracy between our values of T_{10} and those of Hwang is about 5%. Therefore, despite the fact that the accuracy of T_{10} was estimated to be 20–30% [61], the relative values are comparable within 5%. We observe that at low values of τ_{R}^{-1} , our values

(circles) of $T_{10}^{-1}(\Delta H_{pp}^{L})$ are in excellent agreement with those of [33] but, as the relaxation rate increases above about 1 µs⁻¹, the literature values are more in line with our values of $T_{10}^{-1}(I)$. Note that in Fig. 13a, the difference in $T_{10}^{-1}(\Delta H_{pp}^{L})$ for lf and hf is minimal while for $T_{10}^{-1}(I)$ it is significant and increasing with rotational rate. While Fig. 13 shows that the relaxation rates of pp-Tempone in toluene and of pp-Tempol in 60%AG are comparable, they cannot definitively support the reliability of either $T_{10}^{-1}(\Delta H_{pp}^{L})$ or $T_{10}^{-1}(I)$.

Figure 13b compares the present results those of [52] derived from combined time-domain measurements of saturation recovery-EPR and saturation recovery-ELDOR in a series of water/glycerol mixture, triangles. The dashed lines are smooth curves to guide the eye through the data of [52] as well as our data for $T_1^{-1}(\Delta H_{pp}^L)$, circles. Here, the full 20–30% uncertainty in H_1 in our measurements comes into play. Nevertheless, the overall agreement is reasonable keeping in mind that the ordinate is a linear scale, unlike the majority of literature data that are presented on a log scale. A preliminary observation is that time-domain data have more straightforward interpretations but that CWS data are more reproducible. Of course, reproducibility and accuracy can be quite different. This point is amply demonstrated by the difference between $T_1^{-1}(\Delta H_{pp}^L)$ and $T_1^{-1}(I)$ which are derived from the same sample and both from high quality fits to the CWS. We understand that the interpretation of $T_1^{-1}(\Delta H_{pp}^L)$ or $T_1^{-1}(I)$ even at C = 0.03 mM depends critically on a detailed understanding of possible relaxation pathways other than HSE/DD; however, we do not yet understand why the two modes of measurement would lead to different results.

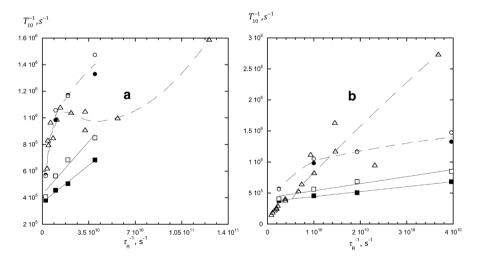


Fig. 13 Spin–lattice relaxation rates derived from $\text{CWS}(\Delta H_{pp}^L)$, circles, and from CWS(I), squares. The straight lines are linear fits; closed symbols If, open, hf. **a** compares the present results those of [33], who employed $\text{CWS}(\Delta H_{pp}^L)$ of pp-Tempone in toluene-d₈ as a function of temperature. **b** compares the present results with those of [52] derived from combined measurements of SR-EPR and SR-ELDOR, triangles, in a series of water and glycerol. The dashed lines are smooth curves to guide the eye

5.2.3 Values of $T_{11f}^{eff}/T_{1hf}^{eff}$

In early work [62], T_1^{eff} was measured using the saturation-recovery technique (SR) for all three lines of 0.16 mM Tempol in sec-butyl benzene as a function of temperature. The values of $T_{\text{llf}}^{\text{eff}}/T_{\text{lhf}}^{\text{eff}}$ showed no correlation with *T*, yielding a mean value of 1.1 ± 0.2 . In the same work, no significant difference in T_1^{eff} was reported for Tempone and pD-Tempone. For ¹⁵N Tempone, $T_{\text{llf}}^{\text{eff}}/T_{\text{lhf}}^{\text{eff}} = 1.0 \pm 0.2$. We are unaware of other work, employing either CWS or pulsed measurements

We are unaware of other work, employing either CWS or pulsed measurements that have reported $T_{\rm llf}^{\rm eff}/T_{\rm lhf}^{\rm eff}$ in Tempol; however, more modern work using SR or IR revealed small but significant differences in three other nitroxides [17]. From IR, differences in $T_{\rm llf}/T_{\rm lhf}$ were found that were not significantly different from rather different nitroxide structure, deuteration, or ¹⁵N enrichment. See column 4 of Table 3 in [17]. Combining all of their room temperature data, we find from those data, $T_{\rm llf}/T_{\rm lhf} = 1.22 \pm 0.03$.

In this work, forming $T_{\rm llf}^{\rm eff}/T_{\rm lhf}^{\rm eff}$ from Tables 8, 9, 10 and 11, one finds minor variations with T and C. Furthermore, there is no correlation with $f_{\rm m}$. Combining all data, $T_{\rm llf}^{\rm eff}/T_{\rm lhf}^{\rm eff} = 1.01 \pm 0.05$ from CWS($\Delta H_{\rm pp}^{\rm L}$), 1.3 ± 0.2 from CWS(I), and 1.15 ± 0.07 from the eye fits. This aspect supports the validity of CWS(I).

In summary, the pulsed EPR measurements [17] and various approaches to analyzing CWS in this work both show small, systematic departures of $T_{\rm llf}/T_{\rm lhf}$ from unity of similar magnitude.

6 Conclusions

A theory was presented that allows the study of the CWS of any parameter derived from the EPR spectrum. The parameters readily available experimentally without fitting are ΔH_{pp}^{spc} , the line width of the combined absorption and the dispersion and V_{pp}^{spc} , the amplitude of the combination, neither of which is very useful as the lines become broader. With fitting, ΔH_{pp}^{L} , I, V_{pp} , and V_{disp} may be studied. We have shown that the Bloch fits to CWS of V_{pp} are rather good, but yield values of T_1 that are wrong by 100% or more in the examples considered here. Furthermore, as exemplified by Fig. 1, comparison of empirical parameters based on a percentage change in V_{pp}^{spc} from the linear behavior at small H_1 must be done with great care. Experimentally, at C = 0.03 mM where HSE or DD are negligible, T_{10} is comparable with literature values, but the values derived from CWS of I or ΔH_{pp} are different from one another. For C > 0, using fits to the Bloch Eqs. (3) or (5) to obtain values of T_{1hf}^{eff} as has been proposed in the literature [33, 59], yield values that are reasonable, but the values derived from I or of ΔH_{pp}^{L} are different. From eye fits, the CWS of V_{disp} may be estimated and is in reasonable agreement with theory except at 273 K at higher values of H_1 .

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