

# Evaluating the Occupational Environment – Particle Behavior

EOH 466B  
Spring 2008

## Particle Behavior

- Excellent reference: Aerosol Technology. Properties, behavior and measurement of airborne particles, Second Edition by William C. Hinds, Wiley-Interscience, 1999

## Particle Behavior

- The physical diameter and density of a particle are important factors affecting behavior of an aerosol. It is convenient to consider particles as spherical.

## Particle Behavior

- Stokes diameter is the diameter of a sphere that has the same density and settling velocity as the particle.

## Particle Behavior

- Aerodynamic diameter is the diameter of the unit density sphere that has the same settling velocity as the particle.

## Particle Behavior

- Terminal settling velocity: can be determined if the size and density of a particle is known. Stokes' law allows an estimation of  $V_{ts}$ , for particles between 1 and 100  $\mu$

$$V_{ts} = \frac{gd^2(\rho - \rho_a)}{18\eta}$$

- $g$  = gravitational acceleration,  $9.8 \times 10^2$  cm / sec
- $d$  = diameter of particle in cm
- $\rho$  = density (air =  $1.17 \times 10^{-3}$  g/cm<sup>3</sup>)
- $\eta$  = coefficient of viscosity of air  $1.828 \times 10^{-3}$  g / cm-sec

## Particle Behavior

- This can be simplified to
  - $V_{ts} = 0.003 \times SG \times d^2$  at NTP.
  - This equation gives  $V_{ts}$  in cm/sec using  $d$  in microns.

## Compare Physical Diameter and Aerodynamic Diameter

**Table 2. Aerodynamic Diameters of Particles with Different Densities**

|                                                                                     |                         |                                                                  |                                    |
|-------------------------------------------------------------------------------------|-------------------------|------------------------------------------------------------------|------------------------------------|
|  | Low-density particle    | $\rho_p = 1 \text{ gm/cm}^3$<br>$d_{ps} = 2 \text{ }\mu\text{m}$ | $d_{pa} = 2.0 \text{ }\mu\text{m}$ |
|  | Medium-density particle | $\rho_p = 2 \text{ gm/cm}^3$<br>$d_{ps} = 2 \text{ }\mu\text{m}$ | $d_{pa} = 2.8 \text{ }\mu\text{m}$ |
|  | High-density particle   | $\rho_p = 3 \text{ gm/cm}^3$<br>$d_{ps} = 2 \text{ }\mu\text{m}$ | $d_{pa} = 3.5 \text{ }\mu\text{m}$ |

Note:  $\rho_p$  = Particle density  
 $d_{ps}$  = Stokes particle diameter  
 $d_{pa}$  = Aerodynamic diameter

## Particle Behavior

- The equation should be adjusted by the Cunningham slip correction factor,  $C_c$  to provide accurate prediction of  $V_{ts}$  for particles smaller than 1 micron.

$$V_{ts} = \frac{gd^2(\rho - \rho_a)C_c}{18\eta}$$

Table 1. Cunningham Slip Correction Factors for Air (298°K, 1.0 atm)

| $d_{pa}(\mu m)$ | $C_c$ | $d_{pa}(\mu m)$ | $C_c$ |
|-----------------|-------|-----------------|-------|
| 0.001           | 221.6 | 0.1             | 2.911 |
| 0.002           | 111.1 | 0.2             | 1.890 |
| 0.003           | 74.25 | 0.3             | 1.574 |
| 0.004           | 55.83 | 0.4             | 1.424 |
| 0.005           | 44.76 | 0.5             | 1.337 |
| 0.006           | 37.41 | 0.6             | 1.280 |
| 0.007           | 32.15 | 0.7             | 1.240 |
| 0.008           | 28.20 | 0.8             | 1.210 |
| 0.009           | 25.14 | 0.9             | 1.186 |
| 0.01            | 22.66 | 1.0             | 1.166 |
| 0.02            | 11.65 | 2.0             | 1.064 |
| 0.03            | 7.878 | 3.0             | 1.056 |
| 0.04            | 6.151 | 4.0             | 1.042 |
| 0.05            | 5.060 | 5.0             | 1.034 |
| 0.06            | 4.337 | 6.0             | 1.028 |
| 0.07            | 3.823 | 7.0             | 1.024 |
| 0.08            | 3.441 | 8.0             | 1.021 |
| 0.09            | 3.145 | 9.0             | 1.019 |
|                 |       | 10.0            | 1.017 |

## Particle Behavior

- For non spherical particles,  $V_{ts}$  must be calculated using a dynamic shape factor,  $\chi$ , for particle sizes described by the equivalent volume diameter,  $d_e$

$$V_{ts} = \frac{gd^2(\rho - \rho_a)C_c}{18\eta\chi}$$

## Compare Different Shape and Aerodynamic Diameter

| Table 1. Aerodynamic Diameters of Differently Shaped Particles                      |                 |                                                                      |                                  |
|-------------------------------------------------------------------------------------|-----------------|----------------------------------------------------------------------|----------------------------------|
|  | Solid sphere    | $\rho_p = 2.0 \text{ gm/cm}^3$<br>$d_{ps} = 1.4 \text{ }\mu\text{m}$ | $d_{pa} = 2 \text{ }\mu\text{m}$ |
|  | Hollow sphere   | $\rho_p = 0.5 \text{ gm/cm}^3$<br>$d_{ps} = 2.8 \text{ }\mu\text{m}$ |                                  |
|  | Irregular shape | $\rho_p = 2.4 \text{ gm/cm}^3$<br>$d_{ps} = 1.3 \text{ }\mu\text{m}$ |                                  |

Note:  $\rho_p$  = Particle density  
 $d_{ps}$  = Stokes particle diameter  
 $d_{pa}$  = Aerodynamic diameter

## Particle Behavior

- Stopping distance: when a particle is released at high speed, how far will it travel?
  - This can be calculated, and is related to resistance to travel experienced by the particle. For small particles, generally this is less than 1 cm. Can be significant for denser and larger particles.

## Particle Behavior

- Particle size selective samplers apply the principles in  $V_{ts}$  to remove particles from an air stream.
  - Cyclones (centrifugal force)
  - Vertical Elutriators (settling velocity)
  - Cascade Impactor (stopping distance)
  - Horizontal Elutriators (settling velocity)

## Particle Behavior

- Particle amount: how much material is present: most often mass, but can be number of particles, radioactivity, surface area, volume or chemical content. Choice of unit depends on application.

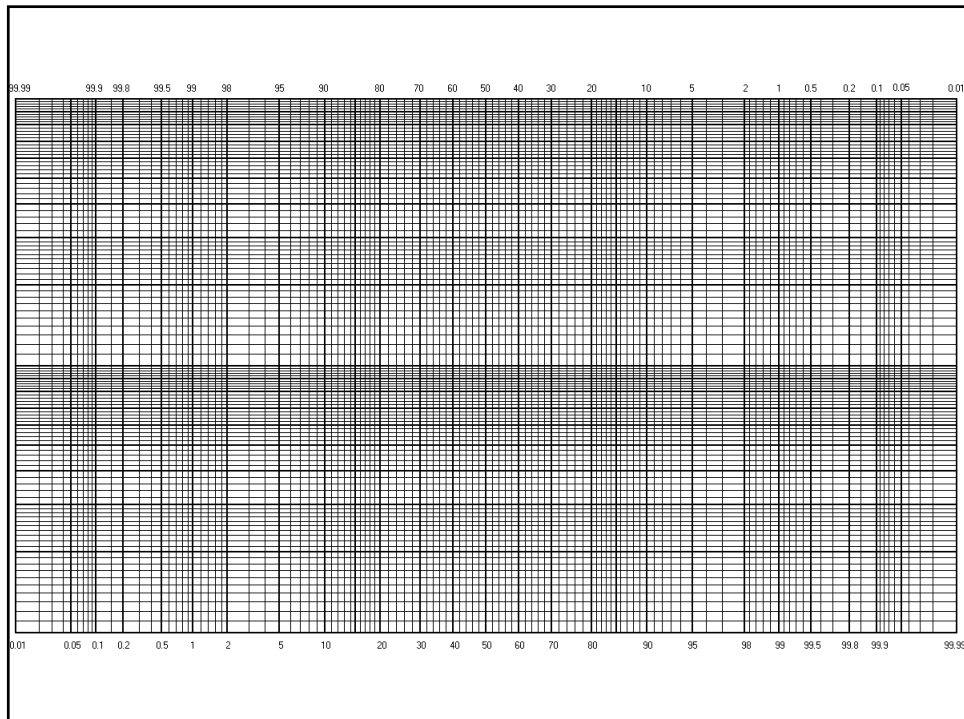
## Presentation of Particle Size Information

- Cumulative probability plots.
  - Calculate the fraction of total amount in each size class, and sum this fraction from the small to large size classes.
    - Graph this on 'log-probability' paper: a straight line will indicate a lognormal distribution.



## Analysis of Particle Count Data

| Lower Interval<br>( $\mu\text{m}$ ) | Upper Interval<br>( $\mu\text{m}$ ) | Midpoint Interval<br>$d_i$ ( $\mu\text{m}$ ) | Number in Interval<br>$n_i$ | Fraction Interval<br>(%) | Cumulative Fraction less Than $d_i$ (%) |
|-------------------------------------|-------------------------------------|----------------------------------------------|-----------------------------|--------------------------|-----------------------------------------|
| 0.46                                | 0.54                                | 0.50                                         | 3770                        | 0.74                     | 0.74                                    |
| 0.54                                | 0.63                                | 0.585                                        | 13,000                      | 2.56                     | 3.30                                    |
| 0.66                                | 0.74                                | 0.685                                        | 55,100                      | 10.84                    | 14.14                                   |
| 0.74                                | 0.86                                | 0.80                                         | 62,900                      | 12.38                    | 26.52                                   |
| 0.86                                | 1.0                                 | 0.93                                         | 98,800                      | 19.44                    | 45.96                                   |
| 1.0                                 | 1.2                                 | 1.1                                          | 109,000                     | 21.45                    | 67.41                                   |
| 1.2                                 | 1.4                                 | 1.3                                          | 98,800                      | 19.44                    | 86.85                                   |
| 1.4                                 | 1.6                                 | 1.5                                          | 37,200                      | 7.32                     | 94.17                                   |
| 1.6                                 | 1.8                                 | 1.7                                          | 17,000                      | 3.35                     | 97.52                                   |
| 1.8                                 | 2.2                                 | 2.0                                          | 9710                        | 1.91                     | 99.43                                   |
| 2.2                                 | 2.5                                 | 2.35                                         | 2850                        | 0.56                     | 99.99                                   |
| 2.5                                 | 2.9                                 | 2.7                                          | 52                          | 0.01                     | 100                                     |
|                                     |                                     |                                              | 508,182                     |                          |                                         |



## Sample method development

- NIOSH Applet is important to review.
- Concepts:
  - Precision, bias, accuracy
  - Detection limit
  - 95 % accuracy
  - Sample stability
  - Walk through the applet