

NAME: \_\_\_\_\_

&lt;KEY&gt;

I. Translate the following arguments into the language of statement logic (SL) using the suggested capital letters to represent simple statements. In your translation, make sure you indicate which of the statements is the conclusion. (20 points)

1. American foreign policy is bankrupt unless it is based on clear *m*oral principles. American foreign policy is not based on clear moral principles just in case it is based primarily on the *n*ational interest. Unfortunately, American foreign policy is based primarily on the national interest. We may conclude that American foreign policy is bankrupt. (A, M, N)

$$A \vee M$$

$$\sim M \leftrightarrow N$$

$$N$$


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$$\therefore A$$

2. If the equatorial rain forests produce oxygen used by Americans, then either Americans ought to *p*ay for the oxygen, or they ought to stop complaining about the destruction of the rain forests. But either it is false that Americans ought to pay for the oxygen, or it is false that Americans ought to stop complaining about the destruction of the rain forests. Therefore, it is false that the equatorial rain forests produce oxygen used by Americans. (E, P, S)

$$E \rightarrow (P \vee S)$$

$$\sim P \vee \sim S$$


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$$\therefore \sim E$$

II. Using a full truth table, determine whether the following statement is a TAUTOLOGY, SELF-CONTRADICTION, or CONTINGENT. (14 points)

3.  $(G \& H) \& (G \rightarrow \sim H)$

G	H	$(G \& H)$	$(G \rightarrow \sim H)$
T	T	T	F
T	F	F	T
F	T	F	T
F	F	F	T

SELF-CONTRADICTION

III. Using a full truth table, determine whether the following statements are EQUIVALENT, MUTUALLY CONTRADICTION, or NEITHER. (14 points)

4.  $I \rightarrow (I \rightarrow \sim J)$        $(I \rightarrow \sim J) \vee \sim I$

I	J	$I \rightarrow (I \rightarrow \sim J)$	$(I \rightarrow \sim J) \vee \sim I$
T	T	F	F
T	F	T	T
F	T	T	T
F	F	T	T

EQUIVALENT

IV. Using a full truth table, determine whether the following statements are CONSISTENT or INCONSISTENT. (14 points)

5.  $K \& \sim L$                        $\sim(K \rightarrow L)$

K	L	$K \& \sim L$	$\sim(K \rightarrow L)$
T	T	T (F) F	(F) T
T	F	T (T) T	(T) F ✓
F	T	F (F) F	(F) T
F	F	F (F) T	(F) T

CONSISTENT

V. Using a full truth table, determine whether the following argument is VALID or INVALID. (14 points)

6.  $\sim M \vee \sim N$   
 $\sim N \& \sim M$   
 $\therefore N \rightarrow M$

M	N	$\sim M \vee \sim N$	$\sim N \& \sim M$	$N \rightarrow M$
T	T	(F)	(F)	T (T) T
T	F	(T)	(F)	F (T) T
F	T	(T)	(F)	T (F) F ←
F	F	(T)	(T)	F (T) F

VALID

VI. Using a brief truth table, determine whether the following argument is VALID or INVALID. (12 points)

7.  $(D \vee E) \rightarrow \sim B$   
 $G \vee \sim F$   
 $O \& (D \leftrightarrow G)$   
 $\therefore F \rightarrow \sim(B \& O)$

$(D \vee E) \rightarrow \sim B$	$G \vee \sim F$	$O \& (D \leftrightarrow G)$	$F \rightarrow \sim(B \& O)$
T (F) F	T (T) F	T (T) T T	T (F) F T T

VALID

VII. Using a brief truth table, determine whether the following statement is a TAUTOLOGY. (12 points)

8.  $S \rightarrow [\sim(Y \& S) \rightarrow Y]$

$S \rightarrow [\sim(Y \& S) \rightarrow Y]$
T (F) T F F F

NOT A TAUTOLOGY