Consider an isosceles triangle $ABC$ with $AB = AC$. Let $D$ be the midpoint of segment $BC$, $E$ a point on the side $AC$ such that $DE$ is perpendicular to $AC$, and $F$ the midpoint of segment $DE$.

Prove that the segments $AF$ and $BE$ are perpendicular.