Consider an arbitrary collection of six irrational numbers. Show that there are always three of them whose sums by pairs are also irrational. That is, show that there are always three numbers \(x, y, z\) from the original six, such that \(x + y, x + z, y + z\) are all irrational.