

Introduction to MATLAB

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 Mechanical Engineering 309
**Numerical Analysis of
 Engineering Systems**

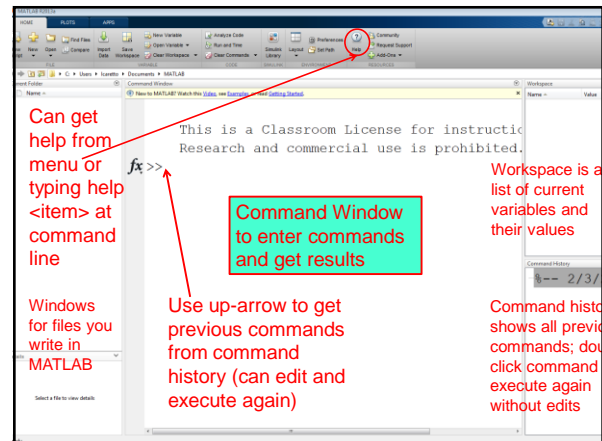
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Outline

- MATLAB windows and Help
- Commands from command window
 - Formatting data and command window
 - Functions in MATLAB
 - Entering and using arrays of numbers
 - Introduction to plotting in MATLAB
 - Saving the workspace and diary files
 - Starting, saving, and opening m-files
 - Script files and MATLAB functions

Starting MATLAB

- During class we will start working on the next programming assignment
- Start MATLAB and Word on your computers
 - Save Word file as <lastName>_pa2.docx
- Download second programming assignment from home page of course web site
 - www.csun.edu/~lcaretto/me309/pa2.pdf



MATLAB Exercise

- Type format compact at MATLAB command prompt (>>)
- Use a wide command window to get as many results as possible on one line
- From time to time copy MATLAB commands, results, plots, and files to Word file
- Word file with MATLAB information and your discussion is only file required

MATLAB Basics

- Variables are introduced without declaration of types or array size
- In general any variable can be an array of complex numbers
 - Can also be a simple number like 3
- Variables are case sensitive (A is not a)
- Type commands at >> prompt
- Results echoed after command unless you end command with semicolon (;)

Command Window

- Examples of commands (following >>) and resulting output given below
- Copied from actual MATLAB session, but edited to eliminate blank rows
- Press **Enter** key after each command

```
>> %This is a comment
>> %Assign values to variables
>> x = 2
x = 2
>> y = 3
y = 3
>> %Default result is ans
>> x + y
ans = 5

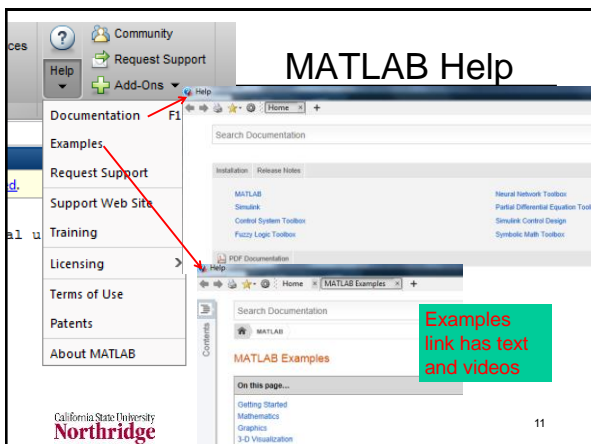
>> %Assign result to variable
>> z = x/y
z = 0.6667
>> %Change output format
>> format ('long')
>> %Print value of z
>> z
z = 0.6666666666666667
```

Formatting Output

- **format** command sets output
- **format compact** and **format loose** set line spacing as narrow or wide
- Decimal display is controlled by format
 - **format short** gives five significant figures
 - **format long** gives fifteen significant figures
 - Enter **help format** for other choices
- All calculations done with ~15 significant figures regardless of format

Functions and Complex Numbers

- MATLAB has large number of functions
- Simple ones similar to other languages
 - Partial list: sin, **sin_d**, cos, tan, sqrt, asin, atan, sinh, tanh, log (natural log), log₁₀, etc.
 - >> log(10) gives ans = 2.3026 Returns sine of argument in degrees
- Can also have complex numbers
 - >> 2 + 3i gives ans = 2.0000 + 3.0000i
 - Can also use j in place of i for $\sqrt{-1}$
 - MATLAB does complex arithmetic and more



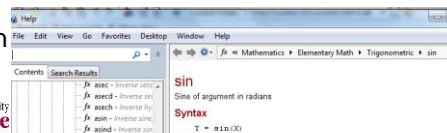
More on Help

- Help example at right
- Click on [doc sin](#) for full html help on sine

```
>> help sin
SIN Sine of argument in radians.
SIN(X) is the sine of the elements of X.

See also asin, sind.

Reference page in Help browser
doc sin
```



Arrays of Numbers

- We will say more about the following definitions when we cover matrix analysis
- An array of numbers in a row is called a row vector, e.g. $r = [1 \ 5 \ -4 \ 10 \ 3]$
- An array of numbers in a column is called a column vector (see next slide)
- An two-dimensional array is called a matrix (see next slide)

– Row/column vectors special case of matrix

Matrix Examples

Row vector: $r = [1 \ 5 \ -4 \ 10 \ 3]$

Column vector:

$$c = \begin{bmatrix} 8 \\ 17 \\ -21 \\ 14 \\ -3 \end{bmatrix}$$

A matrix with 3 rows and 5 columns is called a 3 by 5 (3 x 5) matrix

$$A = \begin{bmatrix} 12 & 8 & -9 & 0 & 45 \\ -7 & -16 & 23 & 87 & -12 \\ 0 & 3 & 5 & 6 & 16 \end{bmatrix}$$

The row vector above is a 1 by 5 matrix and the column vector is a 5 by 1 matrix

Entering Arrays

- Enter a row vector by enclosing data in [] separated by a space
`>> row = [12 -3 5 7 0]`
- Enter a column vector by enclosing data, separated by a semicolon (;) in []
`>> col = [-3; 6; 0; 4]`

Entering a Matrix

- Enter matrix data row by row
`>> A=[1 2; 3 4]`
- Put spaces between data in the same row
- Put a semicolon to start data on next row
`>> B = [1 2 3; 4... 5 6; 7 8... 9]`
- MATLAB uses the ... as a continuation signal
- After the ... hit Enter and continue input of same command on a new line

Entering a Matrix II

- Pressing enter after each row of data can be used to enter a matrix
- Using semicolons, all data can be placed on one row (see below)
- Continuation is only needed to start new line in the middle of data entry

$$B = \begin{matrix} \text{(Result)} \\ 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{matrix}$$

```
>> B = [1 2 3
        4 5 6
        7 8 9]
>> B = [1 2 3; 4...
        5 6; 7 8 9]
>> B = [1 2 3; 4 5 6; 7 8 9]
```

Command History

- Can use up-arrow key to get old commands
- Can edit old commands
 - Use left- and right-arrow keys to move backward and forwards in command
 - Backspace or delete removes characters
 - Type new characters as desired
 - Hit enter to execute edited command
 - Repeat editing if second command is wrong

Addressing Matrix Elements

- For row matrix, r, or column matrix, c, r(k) or c(k) is kth element in matrix
- If A is a matrix, A(m,n) is element at row m and column n
- If A is a matrix A(r1:r2,c1:c2) is a submatrix that includes all rows between r1 and r2 and all columns between c1 and c2
- If you want all columns or all rows enter A(r1:r2,:) or A(:,c1:c2), respectively

Exercise: Enter the following

Row vector: $r = [1 \ 5 \ -4]$

(3 x 2) matrix

$$B = \begin{bmatrix} 5 & 4 \\ 1 & 4 \\ 2 & 8 \end{bmatrix}$$

(3 x 3) matrix

$$A = \begin{bmatrix} 12 & 8 & 0 \\ -7 & -16 & 4 \\ 0 & 3 & 2 \end{bmatrix}$$

Column vector:

$$c = \begin{bmatrix} 8 \\ 3 \\ -2 \end{bmatrix}$$

Ask yourself, "what will the result of the following formulas be?" before entering them

Note that for any matrix, A, A' gives A^T, the transpose of A (the matrix A with rows and columns exchanged)

D = [A B] E = [B A] ct = c' F = [r; ct] G = [c A ct']

Exercise: Saving the Workspace

- Select **File | Save Workspace As**
 - Use default file name (matlab.mat) or enter one of your own and click **Save**
 - Exit and restart MATLAB
 - Select **File | Open**, click on saved file name (matlab.mat) in dialog, and click **Open**
 - Type **whos** at command line to see that all your previous variables are there
 - Type H, then type H(2,3) at the command line. Is the result for H(2,3) correct?

Exercise: SubArrays

- Recall that A(r1:r2,c1:c2) is a submatrix of A that includes all rows between r1 and r2 and all columns between c1 and c2
- Type the following and make sure that you believe the results (use <Enter>)
 - H(2:4,3:5) Type H(2:4,3) = [-1; -2; -3] at the command line then type H
 - H(:,2:4)
 - H(1,:)
 - H(2:4,3) Are the results what you expected?

Other Array Definitions

- Use <variable> = <lower bound> : <increment> : <upper bound>
 - Can also use <lower bound> : <upper bound> with default <increment> = 1
 - Example creates array t

```
>> t = 0:pi/4:2*pi
t =
Columns 1 through 7
    0    0.7854    1.5708    2.3562    3.1416    3.927    4.7124
Columns 8 through 9
    5.4978    6.2832
```

Array Functions

- If A is an array, a function like sin(A) is also an array giving the value of the sine for each element in the array, A

```
>> s=sin(t)
s =
    0    0.7071    1.0000    0.7071    0.0000   -0.7071   -1.0000   -0.7071   -0.0000
```

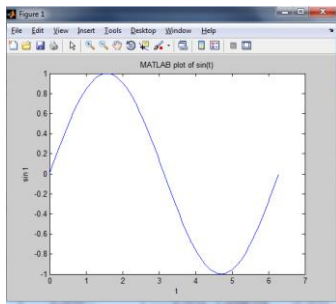
- We can use arrays like these to generate plots
 - Redo t and s to have more data points using $t = 0:\pi/100:2*\pi$;

MATLAB Plotting

– Commands for t and s below use semi-colon at end of line to suppress output

```
>> t=0:pi/100:2*pi;
>> s=sin(t);
>> plot(t,s)
>> ylabel('sin t')
>> xlabel('t')
>> title('MATLAB plot of sin(t)')
```

Single quotes define string constant



Script Files

- MATLAB script files are like Excel macros: they are a set of commands that are executed by a single command
 - Type file name at command line to execute
- To start script file select **New** from home tab then select **Script** in submenu
- Copy the previous commands for sine plot from the command window to a file
- Can change sine to cosine

Script File

```
%cosinePlot -- a script file
% to plot the cosine
%Larry Caretto 31 Jan 14
%-----
t=0:pi/100:2*pi;
s=cos(t);
plot(t,s)
ylabel('cos t')
xlabel('t')
title('MATLAB plot of cos(t)')
```

File must be saved as cosinePlot.m

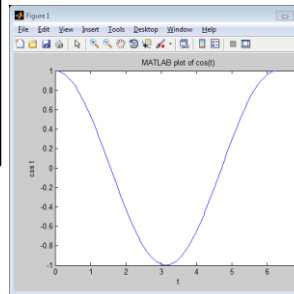
- Script file shown in box at left
 - Name is first entry after %
- First four lines are comments
 - Will show by help command
- Type file name at >> to execute

Using Script File

```
>> help cosinePlot
cosinePlot -- a script file
to plot the cosine
Larry Caretto 31 Jan 14
```

```
>> cosinePlot
>>
```

- Commands above show results of help command and execution command



Array Operations

- Can do mathematical operations on arrays providing they are compatible
- Two kinds of operations
 - Term-by-term operations act on each term in an array
 - Arrays must be same size (rows and columns)
 - Matrix operations will be covered after discussion of matrix analysis
 - Addition and subtraction are same for both types of operation

Addition and Subtraction

$$D = \begin{bmatrix} 12 & 8 & 0 & 5 & 4 \\ -7 & -16 & 4 & 1 & 4 \\ 0 & 3 & 2 & 2 & 8 \end{bmatrix} \quad E = \begin{bmatrix} 5 & 4 & 12 & 8 & 0 \\ 1 & 4 & -7 & -16 & 4 \\ 2 & 8 & 0 & 3 & 2 \end{bmatrix}$$

$$D + E = \begin{bmatrix} 17 & 12 & 12 & 1 & 4 \\ -6 & -12 & -3 & -15 & 8 \\ 2 & 11 & 2 & 5 & 10 \end{bmatrix}$$

$$D - E = \begin{bmatrix} 7 & 4 & -12 & -3 & 4 \\ -8 & -20 & 11 & 17 & 0 \\ -2 & -5 & 2 & -1 & 6 \end{bmatrix}$$

D and E are shown on slide 18

Array Times a Scalar

- A single number, $a = 3$, is a scalar
- When an array is multiplied (or divided) by a scalar each term in the array is multiplied (or divided) by the scalar
- For $r = [6 \ 3 \ -1]$, $3r = [18 \ 9 \ -3]$
- For the A array defined previously, what is $4A$? What is $A/2$?

$$A = \begin{bmatrix} 12 & 8 & 0 \\ -7 & -16 & 4 \\ 0 & 3 & 2 \end{bmatrix} \quad 4A = \begin{bmatrix} 48 & 36 & 0 \\ -28 & -64 & 16 \\ 0 & 12 & 8 \end{bmatrix} \quad \frac{A}{2} = \begin{bmatrix} 6 & 4 & 0 \\ -3.5 & -8 & 2 \\ 0 & 1.5 & 1 \end{bmatrix}$$

Term-by-term Operations

- Have seen addition and subtraction
- Term-by-term multiplication and division of arrays use operators `.*` and `./`
 - The period (.) distinguishes these from matrix operations to be covered later
- For term by term operations the arrays must be the same size
 - Same number of rows and same number of columns

Term-by-term Multiplication

$$D = \begin{bmatrix} 12 & 8 & 0 & 5 & 4 \\ -7 & -16 & 4 & 1 & 4 \\ 0 & 3 & 2 & 2 & 8 \end{bmatrix} \quad E = \begin{bmatrix} 5 & 4 & 12 & 8 & 0 \\ 1 & 4 & -7 & -16 & 4 \\ 2 & 8 & 0 & 3 & 2 \end{bmatrix}$$

$$D .* E = \begin{bmatrix} 60 & 32 & 0 & 40 & 0 \\ -7 & -64 & -28 & -16 & 16 \\ 0 & 24 & 0 & 6 & 16 \end{bmatrix}$$

Term-by-term Division

$$D = \begin{bmatrix} 12 & 8 & 0 & 5 & 4 \\ -7 & -16 & 4 & 1 & 4 \\ 0 & 3 & 2 & 2 & 8 \end{bmatrix} \quad E = \begin{bmatrix} 5 & 4 & 12 & 8 & 0 \\ 1 & 4 & -7 & -16 & 4 \\ 2 & 8 & 0 & 3 & 2 \end{bmatrix}$$

$$D ./ E = \begin{bmatrix} 2.400 & 2.000 & 0 & 0.6250 & \text{Inf} \\ -7.000 & -4.000 & -0.5714 & -0.0625 & 1.000 \\ 0 & 0.375 & \text{Inf} & 0.6667 & 4.000 \end{bmatrix}$$

Operations on Formulas

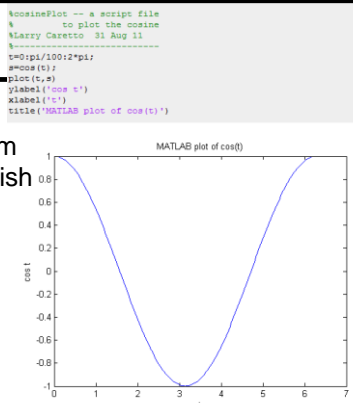
- How do you compute $e^{ax}\sin(bx)$ for an x array between 0 and 2 with $\Delta x = .01$?
 - Set the x array: `>>x = 0:0.01:2;`
 - Define constants, e.g.: `>> a = -1 >>b = 12`
 - Use term by term multiplication for arrays of exponential and sine terms:
 - `>> y = exp(a*x).*sin(b*x);`
 - Do these steps yourself then execute command `plot(x,y)` Use the `.*` operator for term-by-term array operations

The publish Command

- Used to publish reports in various formats: html, Word, Power Point, etc.
- Type `help publish` for full information
- Sample for cosinePlot script
- `>>publish('cosinePlot', 'html')`
- Result is `ans= <path to html document>`
 - `C:/Users/lcaretto/Documents/MATLAB/html/cosinePlot.html`
- Copy this path and paste it into the URL box of your web browser

Result

- File that results from using publish command shown on previous slide



MATLAB File Locations

- Stored as file in MATLAB subdirectory of your Documents folder
 - C:\Users\lcaretto\Documents\MATLAB
- Need to use the same computer in lab to have access to old files
 - Can use Save As command in MATLAB to save files to memory stick (or copy from your MATLAB directory)
 - Possible to save in other directories
- Type **help userpath** to see how to do this

Saving Files to Z: Drive

- Create matlab subdirectory on Z: drive (or U: drive) using Windows
 - Choose subdirectory appropriate for you
 - This slide assumes matlab subdirectory
- At MATLAB command prompt, enter the command: `userpath('z:\matlab')`
- To check that this worked, enter the command: `userpath`
 - Should get: `ans = z:\matlab;`

The diary Command

- Keeps a record of your commands and MATLAB responses in a text file
 - Use **diary <filename>** to start and **diary off** to stop
 - E.g. `diary 20140203.out` will start recording
 - Can stop and restart in same session
 - Use command **diary on** to append new commands to previous ones
 - This command does not copy figures
 - Can edit diary file in text editor

More About Plotting

- The plot command is `plot(x, y, 'options')`
 - x,y are variables to be plotted on x,y axes
 - Options is a **string** that can combine several options (color, line style, marker)
 - Default (no options) plot is solid blue line with no markers
 - Colors are blue(b), green(g), red(r), cyan(y), magenta(m), yellow(y), black(b), white(w)
 - Line styles: solid(-), dotted(:), dash-dot(-.), dashed(--), and no line(none)
 - Example: dashed red line option is 'r--'

More Plot Options

- Marker options: point(.), circle(o), x-mark(x), plus(+), star(*), square('s'), etc.
 - What options does 'g:s' specify
- `xlabel('time')` writes time as label on x axis
- `ylabel('function')` for function as y axis label
- `title('Chart Title')`
 - Note use of character constants by placing text inside single quotation marks('')
 - See **help plot** or **doc plot** for more options including multiple lines on one plot, formatting, and mathematical symbols in labels

Still More Plot Options

- Four plot commands: plot, semilogx, semilogy, and loglog
 - Give linear, semilog (x or y) or log-log plots
 - Place one or more lines on each plot
 - All commands have similar syntax with following arguments (x1, y1, options1, x2, y2, options2, ... , xN, yN, optionsN)
 - xK and yK are arrays plotted on x and y axes
 - optionsK describe colors, line style, etc. for data set K

Plot Legend and Axes

- Legend for multiple lines on one plot
 - legend ('title1', 'title2', ... , 'titleN')
 - Provides title for each line in same order that lines are specified in plot commands
 - Legend in upper-right-hand corner
 - Shows line color and marker next to title provided in legend command
- axis command sets limits as array
 - axis([xMin, xMax, yMin, yMax])
 - Default limits show all data

MATLAB Functions

- Contrast with script files that use any defined variable in the current session
- Function files receive inputs through argument list like other languages
- MATLAB functions can return more than one variable
- Function <name> (<argument list>)
- Each variable returned by a MATLAB function can be a scalar or an array

Trajectory Function

```
function [x, y] = traj(v0, theta, N)
%Computes frictionless trajectory Use file
%Uses SI units (meters, seconds) names the
%v0 is initial speed in m/s same as the
%theta is initial angle in degrees function
%N is number of points computed names (e.g.
g = 9.80665; %gravity in m/s^2 traj.m) to
tMax = 2 * v0 * sind(theta) / g; save
t = 0:tMax/(N-1):tMax; functions
x = v0*cosd(theta) * t;
y = v0*sind(theta) * t - g * t.^2/2; Array
plot(x,y); Use semicolons to avoid operation
end intermediate output from
function code
```

Using Your MATLAB Functions

- Used as any MATLAB Function


```
>>v0 = 10;
>>theta = 60;
>>N = 100;
>>[x, y] = traj(v0, theta, N);
```
- Can use only part of return variables
 - >>= traj(v0,theta,N) returns x values in ans
 - >>x = traj(V0,theta,N) returns x values in x
 - >>[x y] = traj(V0,theta,N) for x and y values

MATLAB if Statements

- Use the following format


```
if <expression1>
    <statements1>
elseif <expression2>
    <statements2>
<other elseif's here>
else %optional
    <statements>
end
```
- Same structure as VBA but "Then" not used
- All keywords (if, else, elseif) in lower case
- Final statement is end, not endif

While Statement

- MATLAB has only one conditional looping command with a test before


```
while <condition>
    <statements>
end
```

MATLAB keywords (while and end) must be lower case
- The <statements> in the while loop continue to execute while the <condition> is true

for Statement

- Similar to VBA For statement, but loop limits are a MATLAB array specification


```
for <index> = <MATLAB array>
    <statements>
end
```
- Examples of for statements


```
for τ = [300, 500, 1000, 5000]
for x = 0 : 0.01 : 2
for k = 1 : 25 (Same as 1:1:25)
```

Convert 2D Array to Column

- Convert two-dimensional array, x, to one-dimensional array, y, in MATLAB
- Can enter following lines from command prompt or write as script
 - Used in second programming exercise

```
n = size(x); %n(1) = rows; n(2) = columns
y = x(:,1); %copy first x column into y
%copy remaining x columns into y
for k = 2:n(2) y = [y; x(:,k)]; end
```

Publishing to Word

```
% Define the structure, options_doc_nocode,
% to include code in the output
% and publish to Microsoft word format:
options_doc_nocode.format='doc'
options_doc_nocode.showCode=true
% Publish sine_wave.m:(put m-file name here)
publish('sine_wave.m',options_doc_nocode)
% view the published output file in word:
winopen('html/sine_wave.doc')
```

Matlab creates *.doc name with same first part as m-file (cannot use docx)

MATLAB Review 1/2

- User interface, command window, help
 - Commands echoed unless followed by ;
 - Use `format compact` for small spacing
 - Conventional mathematical expressions and functions
 - To enter arrays separate items on one row by spaces and separate rows by semicolon
 - Combine smaller arrays to get larger ones only if arrays are compatible

MATLAB Review 2/2

- Get array components, A(row,column), or subarrays, A(r1:r2,c1:c2), A(:,c1:c2), A(:,c1), A(r1,:), A(r1:r2,c1), A(r1,c1:c1)
- Set array components equal to some values as in A(3,2:4) = [4 9 6] (or is it [4; 9; 6]?)
- Define array as <start>:<increment>:<last>
- Functions of arrays
- Term-by-term operations (+ - .* ./ .^)
- Plot commands
- Scripts and publish command