

Introduction to One-Dimensional Arrays

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Computer Science 106

Computing in Engineering and Science

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Outline

- Quiz Two and Midterm Results
- Why do we need arrays
- Declaring and using arrays
- Array indexing and size of arrays
- Code use with arrays
- Using for loops where the loop index is an array subscript to process elements in an array

Quiz Two Results

- Number of students: 8
- Maximum score: 25
- Average: 10.6
- Median: 6.5
- Standard deviation: 7.27
- Grade distribution
5 5 5 5 8 15 20 22

Quiz Two Solution

```
#include <iostream>
#include <fstream>
using namespace std;
int main()
{ fstream in( "input.dat" ) ;
  int countTotal = 0;
  int countPositive = 0;
  int countNegative = 0;
  int countZero = 0;
  double sumTotal = 0;
  double sumPositive = 0;
  double sumNegative = 0;
```

Quiz Two Solution II

```
double x;  in >> x;
while ( x != -999.999 ) {
  countTotal++;
  sumTotal += x;
  if ( x > 0 ) {
    countPositive++;
    sumPositive += x;
  }
  else if ( x < 0 ) {
    countNegative++;
    sumNegative += x;
  }
}
```

Quiz Two Solution III

```
else
  countZero++;
in >> x;
} // end while
if ( countTotal == 0 )
  cout << "No data read";
else
  cout << "\nThere are "
    << countPositive <<
    << " positive numbers, "
    << "whose average is "
    << sumPositive /
    << countPositive <<
```

Quiz Two Solution IV

```
<< ".\nThere are "
<< countNegative
<< " negative numbers "
<< "whose average is "
<< sumNegative /
countNegative
<< ".\nThere are " << countZero
<< " zeros " << ".\nThere are "
<< countTotal << " total data "
<< "points whose average is "
<< sumTotal / countTotal << ".\n";
```

Midterm

- Number of students: 9
- Maximum score: 110
- Average: 76.1
- Median: **74**
- Standard deviation: 16.19
- Grade distribution
52 58 65 70 **74** 85 91 93 97

First Problem

```
const double g = 9.808
double mDot, height, efficiency;
cout << "Enter the mass flow rate in kg/s: ";
cin >> mDot;
cout << "Enter the efficiency as a fraction: ";
cin >> efficiency;
cout << "Enter the water height in meters: ";
cin >> height;
double power = efficiency * mDot * g * height
* 1e-6;
cout << "\nFor your input data: "
<< "\n Mass flow rate = " << mDot
<< "kg/s" << "\n Efficiency = "
<< efficiency << "\n Height of water = "
<< height << "m\n" << "\nPower output = "
<< power << "MW."
```

Second Problem

- Trace code through loop
- Read data from file, left to right to exhaust data on one line then move to next line
- Exit while loop when a = -9999
- Gives only three cases
Two real roots: -1 and -1
Two real roots: 3 and -2
Complex roots
Real part = 0, Imaginary part = 2

Third Problem

```
cin >> n >> a >> b;
while ( n != -999.999 ) {
cout << "\nFor your inputs a = " << a
<< ", b = " << b << ", and n = "
<< n << ", the integral is ";
if ( n == -1 && ab > 0 )
cout << log( b / a );
else if ( n == -1 )
cout << "not defined.";
else
cout << ( pow( b, n - 1 ) -
pow( a, n - 1 ) ) / ( n - 1 );
cout << "Enter n a b: ";
cin >> n >> a >> b;
}
```

Representing Data

Run	Data
1	12.3
2	14.4
3	11.8
4	12.5
5	13.2
6	14.1

- Consider a set of experimental data with several runs
- How do we represent the data in such a way that we can process these data and similar data sets with more values?

Representing Data II

Run, i	x data
1	x_1
2	x_2
3	x_3
4	x_4
5	x_5
6	x_6

- x_i is mathematical notation for several cases of similar data
- Use this formula to find the mean of N data items

$$\bar{x} = \frac{1}{N} \sum_{i=1}^N x_i$$

Representing Data III

- When we have a set of N data items like x_i it will occupy N memory locations
- A variable like x, declared as double x, occupies only one memory location
- For our data on x_i
 - We want to call it by its name, x
 - We want to have N memory locations
 - We want to compute formulas like average x
 - We want to refer to a specific x, say x_3

Arrays Represent Data

- An array is a way that we can represent the mathematical notation for x_i
- We use the programming notation $x[i]$ to represent the general data element x_i
- When we declare a variable as an array, we reserve the memory locations that we will need for the data
 - Regular variable: double x;
 - Array variable: double x[200];

How to represent x_i

- An array has a single variable name, like x, augmented by a subscript to identify the particular data item
- Example $x[3]$ or $x[k]$
- Power of array structure is use of **variable subscript as loop index** to refer to different elements
- Arrays must be declared with maximum size

One-dimensional C++ Array

Math	C++
x_0	$x[0]$
x_1	$x[1]$
x_2	$x[2]$
x_3	$x[3]$
x_4	$x[4]$
x_5	$x[5]$

- View one-dimensional arrays as a column (or row) of cells
- Start with zero subscript
- Array shown here has 6 elements with subscripts from 0 to 5

Maximum Array Subscript

```
double w[4]; // 4 elements
const int MAX_SIZE = 10;
double x[MAX_SIZE]; // 10 elements
```

- Minimum subscript is zero
- Maximum subscript is one less than the number of elements
- $w[0]$, $w[1]$, $w[2]$, and $w[3]$ are the four elements of the w array
- Note different meanings of $w[N]$

Array Size Declarations

- Can be any expression that evaluates to a constant
- ```
const int MAX_SIZE = 100;
int count[MAX_SIZE];
double current[2*MAX_SIZE];
```
- Symbolic constant is preferred style
    - Allows subsequent reference to array dimension in code with ability to change all occurrences of this value with one edit

## Declaring and Using Arrays

- In a declaration statement like `double x[20]`, the 20 is the maximum array size
  - This must be a literal or symbolic constant
- When using arrays in statements like `z = x[3]` or `x[k] = w * q` the “3” or “k” refers to a particular element of the x array
  - Here we can use a variable or a constant, but the variable must be assigned a value before it is used as a subscript

## Initializing Arrays

- We can declare and initialize ordinary variables, e. g., `int x = 10;`
  - We can also do this for arrays by giving a value for each element
- ```
double x[5] = { 1, 3, 5, 18, 1 };
```
- Array size not required
- ```
double y[] = { 3, 8, 33, 7 };
```
- What is maximum subscript for y? **3**
  - What is the value of y[1]? **8**

## Two Uses of [] for C++ Arrays

| Math  | C++               |
|-------|-------------------|
| $x_0$ | <code>x[0]</code> |
| $x_1$ | <code>x[1]</code> |
| $x_2$ | <code>x[2]</code> |
| $x_3$ | <code>x[3]</code> |
| $x_4$ | <code>x[4]</code> |
| $x_5$ | <code>x[5]</code> |

- Declare this array for six elements total: `double x[6]`
- Refer to a particular element as in following examples
  - `x[2] = 3.5;`
  - `x[k+2] = x[0] + x[1];`

## Maximum Array Subscript

- Array elements are stored in contiguous memory locations
- Program computes memory location from subscript
- **C++ does not check to see if an array subscript is in bounds**
- An incorrect subscript could affect some other memory location

## Subscript out of Range

|      |
|------|
| y    |
| x[0] |
| x[1] |
| x[2] |
| x[3] |
| x[4] |
| z    |

- Cells show memory locations for y, x[] array, and z
- The x array has five elements stored in the locations shown
- `x[-1]` would give the same location as the variable y
- `x[5]` would give the same location as the variable z

## Using Arrays

- Individual components of arrays, such as `x[3]` or `y[k]`, are used in the same way as ordinary variables
- Variable subscripts must be assigned a value before use as in examples below

```
int k = 3, m = 5;
double x[5] = { 1, 3, 5, 18, 143 }, z[50], r = 1;
x[k] = 4; x[3] = 4 => { 1, 3, 5, 4, 143 }
z[2*k+3] = x[k-2] - 5 * r * x[3]; // = ???
```

```
z[2*3+3] = x[3-2] - 5 * r * x[3]; or z[9] = x[1] - 5 * r * x[3]
= 3 - 5 * 1 * 4 = -17
```

## Examples of Use

- `cin >> x[k];`
- `cout << "y[" << k << "]" = " << y[k];`
- `data[3] = <expression>`
- `result = 3 + voltage * current[m]`
- `position[m] = position[m+1]`
- `for ( int k = 0; k < N; k++ ) x[k] = 0;`
- `r = pow( y[3], 2);`
- `power[i] = current[i] * voltage[i];`

## Array Questions

| Array             | Values |
|-------------------|--------|
| <code>x[0]</code> | 32     |
| <code>x[1]</code> | 180    |
| <code>x[2]</code> | 20     |
| <code>x[3]</code> | 20     |
| <code>x[4]</code> | 40     |
| <code>x[5]</code> | 60     |

- What is array size? 6
- What are results of code below?

```
x[3] = 20;
int k = 3;
x[k+1] = 2 * x[k];
x[6-2*k] = 32;
x[k-1] = x[4] - x[3];
x[5] = x[k] + x[k+1];
x[k-2] = 3 * x[k+2];
```

## More Array Questions

- Write statements to do the following
  - to declare a double array, `x`, that can have 20 elements `double x[20];`
  - to set element 3 of the slide array equal to the value of element 2 of the same array

```
slide[3] = slide[2];
```

- Assign element `k` of the power array a value of the product of element `k` of the current array times element `k` of the voltage array

```
power[k] = current[k] * voltage[k];
```

## Arrays and for Loops

- Perhaps the most important array code uses a for loop where the loop index becomes the array subscript

```
Example: sum of all elements in array
const int MAX = 10;
double x[MAX], sum = 0;
// code to input x array goes here
for (int k = 0; k < MAX; k++)
 sum += x[k];
```

## General Array Processing

- To process each element in an array with `N` elements, starting with the initial element, use a for loop with index `k`
  - `k` starts at zero
  - The continuation condition, `k < N`, will process elements 0, 1, 2, ..., `N-1`
  - Increment `k` by 1
- `for ( int k = 0; k < N; k++ )`

## General Array Processing II

- On the previous chart N means the number of elements defined, not the total number of elements that can be stored in the array
- Sometimes it is more convenient to refer to the subscripts than to the number of elements
- E. g., array whose first and last defined elements have subscripts F and L
- `for ( k = F, k <= L; k++ )`

## General Array Processing III

- In the examples that follow, we will generally assume that an array has N elements, whose first subscript is zero
- The for loop command to process each element in such an array is  
`for ( k = 0; k < N; k++ )`
- We can use different increments (e.g. `k += 3`) to skip elements

## File Input Screen Output

```
const int MAX_SIZE = 100;
double z[MAX_SIZE];
ifstream inFile("array.dat");
for (int i = 0; i < MAX_SIZE; i++)
{
 inFile >> z[i];
 cout << "\nz[" << i << "] = "
 << z[i];
}
```

## Console Input File Output

```
const int MAX_SIZE = 100;
double z[MAX_SIZE];
ofstream outFile("array.dat");
for (int i = 0; i < MAX_SIZE; i++)
{
 cout << "\nEnter z[" << i
 << "]: ";
 cin >> x[i];
 outFile << z[i] << endl;
}
```

## Defined Elements

- The number of elements defined may be less than the array size
- You may declare an array to be the maximum size expected but actually specify a value for fewer elements

```
double x[10];
for (int j = 1; j < 5; j++)
 x[j] = 1 / double(j);
```

## Computing Array Sums

- Use previous tool of running sum variable along with for loop to include all array elements in the sum
- Application to mean on next chart

```
sum = 0;
for(i = 0; i < N; i++) {} not
{ sum += x[i]; } needed here
cout << "Array sum = " << sum
```

## Computing the Mean

$$\bar{x} = \frac{1}{N} \sum_{i=1}^N x_i = \frac{1}{N} \sum_{i=0}^{N-1} x_i$$

```
sum = 0;
```

```
for(i = 0; i < N; i++)
```

```
{ sum += x[i]; }
```

```
average = sum / N;
```

- N data items to average
- Subscripts starts at 0
- Last data item is element N-1 in array
- {} not needed

## Assignments

- Reading pages in text
  - Today: Pages 397–413
  - Thursday: Pages 413–423
  - Tuesday, April 27: None
- This week's homework problems
  - Page 425, checkpoint 7.13 and page 473, program 1
- Project one due today and project two due Tuesday, April 25