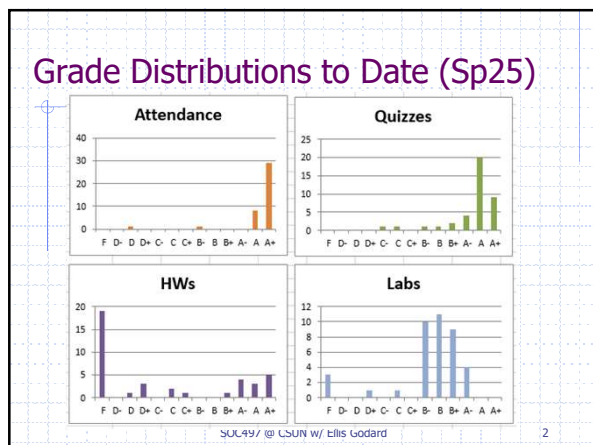


Admin Review Chi-square PREs Choices Summary

SOC497/L: SOCIOLOGY RESEARCH METHODS

## Proportional Reduction in Error & Measures of Association

Ellis Godard

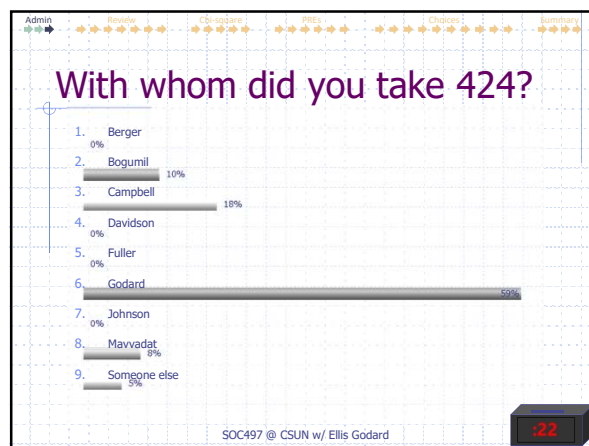
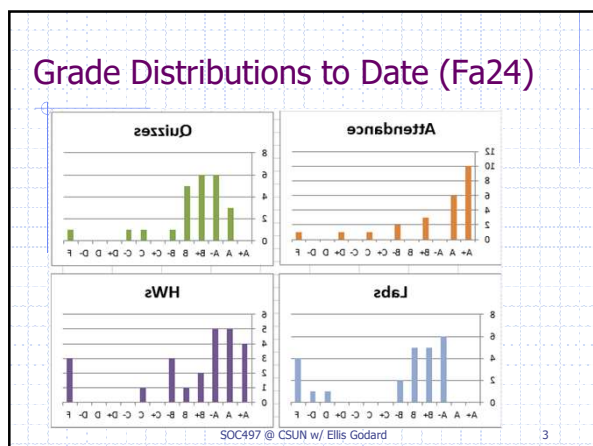


Admin Review Chi-square PREs Choices Summary

### Outline

- Review
  - Univariate, Bivariate Tests, Relationships
- Chi-square Issues
- What "PRE" means
- PRE Choices – esp Gamma & Lambda
- Demo and Lab

SOC497 @ CSUN w/ Ellis Godard 6



## Testing Your Research Project

- ◆ You each need a **bivariate research hypothesis** you'll test w/ data from our survey
- ◆ You each need at **least 2 survey questions**, to measure your DV and IV (extra credit for 2<sup>nd</sup> DV or IV, a CV, an index, etc. – but penalty for unused Qs)
- ◆ **Need to figure out which test to use**, given the measurements you've chosen and the respondent data that we collect
  - For HW6, HW9, & presentation (& paper?)
  - To *inform* your choice of the measurements
  - This lecture is another part of that review...

SOC497 @ CSUN w/ Ellis Godard 8

## Relationships

- ◆ Definition = distribution of DV varies by IV
  - I.e. conditional distributions differ
- ◆ Could look at different DVs:
  - e.g. accounting for attitudes about abortion
- ◆ Could look at different IVs:
  - What accounts for partyid best (polyviews, educ, relig, or income)?


SOC497 @ CSUN w/ Ellis Godard 11

## Operations Constrain Analysis

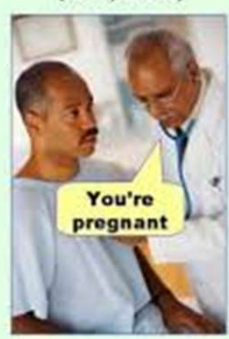
- ◆ **Level of Measurements**
  - Can the values be *out of order*?
    - If no, then it's Nominal.
    - If yes, can you *meaningfully* subtract the values from each other?
      - If No, then it's Ordinal.
        - If the values have labels, the answer is probably No.
        - If the values are labeled with ranges, it's definitely No.
      - If Yes (values can be out of order AND subtracted), it's Interval.
- ◆ **Univariate Analysis**
  - Shape (bell? Skew? Unimodal? Bimodal? Etc...)
  - Central tendency (mean, median, mode)
  - Dispersion (standard deviation, range/IQR, variation ratio)

SOC497 @ CSUN w/ Ellis Godard 9

## Type II error (false negative)



**Type I error (false positive)**



## Four Basic Statistical Tests

- ◆ **Also depend on LOM, BUT all also follow common pattern:**
  - All compare a sample measurement to a "null hypothesized" number
  - All standardize that difference based on some sort of standard error
    - Estimate of how much the sample stat (e.g. mean) differs across all possible samples
  - All ask for chance of getting a difference larger than the one observed
    - A probability (e.g. "right-hand tail") – the "p-value" – what we usually want to be < .05
  - All follow the same 5 steps, and result in a p-value
- ◆ **Four main tests in Sociology:**
  - "T-test" for 1 interval and 1 categorical variable
  - ANOVA ("F test") for several categories & 1 interval
  - Regression ("r" correlation) for several interval variables
  - "Chi-square" for 2 categorical (ordinal or nominal) variables

Next  
Last time

SOC497 @ CSUN w/ Ellis Godard 10

## 1. A relationship exists when...

- The DV changes among values of the IV  
93%
- The IV changes among values of the DV  
5%
- The CV changes among values of the DV  
2%
- The IV changes among values of the CV  
0%
- The DV changes among values of the CV  
0%

SOC497 @ CSUN w/ Ellis Godard

2. Which is NOT one of the three things you should do in any crosstab?

- A. Compare % across  
20%
- B. Compare % up/down  
15%
- C. Look for modal %s  
0%
- D. Look for main diagonal  
56%
- E. Look for chi-square's p-value  
10%

SOC497 @ CSUN w/ Ellis Godard

### Problems w/ Chi-square

- ◆ Varies w/ size of sample & of crosstab
  - Sometimes use alternative chi-square-based measurements
- ◆ Only significance, *not* strength (NOT)
  - Can eyeball (compare across, modal %s)
  - Or can use other stats: PREs/MOAs

SOC364 @ CSUN - Ellis Godard

### Reminder: Crosstabs & $\chi^2$

If they cross the line, can you still remain friends? \*What is your gender? Crosstabulation

		What is your gender?		Total
		Male	Female	
If they cross the line, can you still remain friends?	Yes	Count 71	Count 167	Count 238
	% within What is your gender?	91.0%	78.0%	81.5%
No	Count 7	Count 47	Count 54	
	% within What is your gender?	9.0%	22.0%	18.5%
Total		Count 78	Count 214	Count 292
		% within What is your gender?	100.0%	100.0%

Here, females are more than twice as likely to say they can't still remain friends (22% vs. 9%); males are more likely to say they can, and modal percentages fall along the "main diagonal"; & the difference is statistically significant ( $p < .05$ ).

Chi-Square Tests

	Value	df	Asymp. Sig. (2-sided)	Exact Sig. (2-sided)	Exact Sig. (1-sided)
Pearson Chi-Square	6.398 <sup>a</sup>	1	.011		
Continuity Correction <sup>a</sup>	5.565	1	.018		
Likelihood Ratio	7.196	1	.007		
Fisher's Exact Test				.011	.007
Linear-by-Linear Association	6.376	1	.012		
N of Valid Cases	292				

### Chi-square-based measures

- ◆  $\chi^2$ , varies with df of  $(r-1)*(c-1): \sum \frac{(f_o - f_e)^2}{f_e}$
- ◆  $\chi^2$  also varies with sample size, so Phi =  $\sqrt{\frac{\chi^2}{n}}$ 
  - Pearson's contingency coefficient  $C = \sqrt{\frac{\chi^2}{\chi^2 + n}}$
- ◆ And, it varies w/ table size, so Cramer's V =  $\sqrt{\frac{\chi^2}{\min(r, c) - 1}}$

SOC364 @ CSUN - Ellis Godard

### 3. Chi-square tests...

- A. Association  
88%
- B. Dependence  
10%
- C. Prowess  
0%
- D. Robustness  
0%
- E. Strength  
2%

SOC497 @ CSUN w/ Ellis Godard

### Chi-square = only part of picture

- ◆ All questions ask: Is there a relationship?
  - Compare Column%s across; Modal %s; Chi-square's p
- ◆ But three key questions for crosstabs
  - Dependent relationship? (chi-square)
  - Size/Strength? (% comparisons, plus PREs)
  - Direction? (% comparisons, or gamma...)
- ◆ Three key questions for intervals, too (corr/reg)
  - Strength? – weak or strong?
  - Form? – linear? Curvilinear?
  - Direction? – positive? negative?
    - Remember valence!!

SOC364 w/ Dr. Ellis Godard -- Slide



Admin Review Chi-square PREs Choices Summary

## Proportional Reduction in Error (PRE)

- ◆ By what percentage do we reduce our error in predicting values of the *dependent* variable by knowing values of the *independent* variable?
- ◆ Imagine that I want to guess which students hadn't finished an exam.
  - By how much is my guesswork improved if I know how early or late you submit homework?
  - If I know you're usually early, I might guess that you're already done with the exam.

SOC364 @ CSUN - Ellis Godard 20

Admin Review Chi-square PREs Choices Summary

## PRE Formula

- ◆ All PREs follow same basic formula  

$$(E1 - E2) / E1$$

where E1 is the errors made (in predicting values of the dependent variable) when nothing is known about the independent,

and E2 is the number of errors when the value of the dependent variable is known

SOC364 @ CSUN - Ellis Godard 23

Admin Review Chi-square PREs Choices Summary

## Illustration of the Idea

- ◆ Univariate guess
  - If I know 60% of you are Catholic, but not who is or isn't...
  - Then, for each of you, every time, I would guess you're Catholic
  - That's most likely each time... *but* I'd be *wrong* 40% of the time.
- ◆ Bivariate guess
  - If Latinos/Latinos in the class are more likely to be Catholic...
  - Then, I'd make *fewer* errors men predicting whether or not you're Catholic, if I knew your race/ethnicity.
  - For every Latino/Latina, I'd guess "yes"; for others, "no".
  - I'd still be wrong some % of the time, but less often.
  - The difference is the *proportional reduction in error*.

SOC497 @ CSUN w/ Ellis Godard 21

Admin Review Chi-square PREs Choices Summary

## All PREs have a p value

- ◆ Most have a distribution that matters; others are involved in a test statistic
- ◆ All p's are interpreted basically the same:
  - The null = that there's no relationship – e.g. the statistic, such as gamma, is zero in the population
  - P = probability we'd be wrong *if* we rejected the null
  - ~ = risk in saying the statistic is what SPSS says it is
  - We want that risk to be lower than 5% (.05) so we can reject the null & find support for our claim
    - Remember: p never *is* zero, though might be close
    - If SPSS says .000, it's <.001; if it says .00000, it's <.00001

SOC497 @ CSUN w/ Ellis Godard 24

Admin Review Chi-square PREs Choices Summary

## Distinguishing PREs

- ◆ Proportional Reduction in Error measures
- ◆ Not same as strength, or significance
- ◆ Not *necessarily* a "measure of association"... but some overlap
  - Not all MOAs have a PRE interpretation
  - Some other statistics ( $r^2$ ) *do* have a PRE interpretation but aren't technically MOAs
  - I'll focus on stats that are *both* PREs *and* MOAs

SOC364 @ CSUN - Ellis Godard 22

Admin Review Chi-square PREs Choices Summary

## 4. A p value is the probability of being wrong if we...

- ☺ A. Reject the null 95%
- B. Accept the null 5%
- C. Reject the alternative 0%
- D. Accept the alternative 0%
- E. Give up 0%

SOC497 @ CSUN w/ Ellis Godard

## Nominal Variables: Lambda

- ◆ Based on ability to guess values on one of the variables
  - PRE achieved through knowledge of values on the other variable
  - Represents reduction in errors as a proportion of the errors that would have been made on the basis of the overall distribution.
- ◆ Example: if we make 600 fewer errors predicting employment status, for a sample of 900, when we know the gender,  $\lambda = 600/900 = .67$ 
  - Measures the statistical association between gender and employment status. It indicates a strong relationship.
- ◆ Rough guideline: above 0.5 is strong? below is weak?
- ◆ Always positive; can't be negative

SOC497 @ CSUN w/ Ellis Godard

26

## C vs. D vs. "ties"

Note: these are NOT cross-tabs!!

- ◆ Concordant pair:

	John	Mary
Educ	Higher	Lower
Pay	Higher	Lower

- ◆ Discordant pair:

	John	Mary
Educ	Higher	Lower
Pay	Lower	Higher

- ◆ Tied pairs:

	J	M
Educ	H	H
Pay	?	?

	J	M
Educ	?	?
Pay	L	L

SOC364 @ CSUN - Ellis Godard

29

## Ordinal variables: Gamma

- ◆ = PRE (guess values on one variable w/ values of another) **BUT** considers order of values
  - So cannot use with nominals – i.e. if *either* is nominal
- ◆ Example: Religiosity and political conservatism.
  - If we know there is a strong relation between the two & they're each ordinal (v. strong, strong, neutral, weak, v. weak), then
  - Knowing that someone is very strong in political conservatism would lead us to guess they're very strong in religiosity.
- ◆ Guesses that a higher value on one variable connects w/ higher value on the other, for every possible pair of cases
- ◆ Allows us to guess direction as well as magnitude ("strength") of an association

SOC497 @ CSUN w/ Ellis Godard

27

## Interpreting Gamma 1: Direction

- ◆ If gamma > 0, relationship is positive
  - predict that a higher value on one probably *does* mean a higher value on the other
- ◆ If gamma < 0, relationship is negative
  - predict that a higher value on one probably means a *lower* value on the other
- ◆ In above example:
  - 0.615 -> positive relationship

SOC364 @ CSUN - Ellis Godard

30

## The Idea Behind "Gamma" ( $\gamma$ )

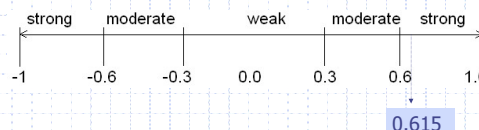
- ◆ Compares *most* pairs of cases in the sample
- ◆ **Focuses on those concordant w/ relationship**
  - (those that show that higher values on one variable are associated with higher values on the other one)
- ◆ **and those discordant w/ a relationship**
  - (the reverse of or at *discord* with a positive relationship – a higher value on one variable but lower on the other)
- ◆  $\text{Gamma} = (C - D) / (C + D)$ 
  - the difference, as a fraction of the combination

SOC364 @ CSUN - Ellis Godard

28

## Interpreting Gamma 2: Strength

- ◆ Weak relationship if 0 to .3 (or 0 to -.3)
- ◆ Moderate if 0.3 to .6 (or -.3 to -.6)
- ◆ Strong if 0.6 to 1 (or -.6 to -1)



SOC364 @ CSUN - Ellis Godard

31

Admin Review Chi-square PREs Choices Summary

## Disadvantage of Gamma

- ◆ Does not take into account tied pairs
  - Therefore overstates strength – it might suggest a perfect positive association (+1) with only one concordant pair:  

$$(C-D)/(C+D) = (1-0)/(1+0) = 1$$
  - **Somer's D** takes ties into account  

$$= (C-D) / (\text{all tied pairs})$$
- ◆ Assumes that a higher value is "more"...

SOC364 @ CSUN - Ellis Godard 32

Admin Review Chi-square PREs Choices Summary

## 5 key PRE Measures, esp 2...

- ◆ **Gamma** (8.5, p.223) –  

$$(\text{Concordant} - \text{Discordant}) / (\text{Concordant} + \text{Discordant})$$
- ◆ **Somer's D**  

$$(\text{concordant} - \text{discordant}) / \text{all ties}$$
- ◆ **Goodman & Kruskal's tau b** (8.4, p.224)
  - based on row marginals
- ◆ **G&K's tau c**
  - based on column marginals
- ◆ **Lambda**
  - nominal only, based on modal category
  - Must use if *either* variable is nominal

SOC497 @ CSUN w/ Ellis Godard 35

Admin Review Chi-square PREs Choices Summary

## What's the variable's *valence*?

- ◆ Gamma assumes a higher *value* means a higher value *label*
  - E.g. 1= low ses, 2=middle, 3= high ses
- ◆ If your variable is the reverse, you'll need to *either* recode the variable to reverse the values *or* interpret gamma upside-down (positive as negative, etc)

SOC364 @ CSUN - Ellis Godard 33

Admin Review Chi-square PREs Choices Summary

## Measures to use...

- ◆ Chi-square always, to establish dependence
- ◆ Lambda if *either* variable is nominal *and* has more than 2 categories
  - Also interpret the p-value – can you reject the null (that the lambda is simply 0)?
- ◆ Gamma if *each* variable is either ordinal or dichotomous
  - Also interpret the p-value – can you reject the null (that the gamma is simply 0)?

SOC364 @ CSUN - Ellis Godard 36

Admin Review Chi-square PREs Choices Summary

## Goodman & Kruskal's tau b

- ◆ Like gamma, tau b is asymmetrical
  - Infers a "direction" to the relationship
  - $\chi^2$  is symmetrical – doesn't distinguish between DV & IV (tho column percents *do*)
  - (plain) tau also symmetrical – could use for 2 nominals?
  - Could use tau b for 2 ordinals?
- ◆ Like Lambda, not absolute; relative only
  - below .5ish weaker; above .5ish is stronger

SOC364 @ CSUN - Ellis Godard 34

Admin Review Chi-square PREs Choices Summary

## SPSS (time/interest permitting)

- ◆ Demo: Crosstab w Abortion
  - Two possible explanations: sex & polviews
  - Don't forget:
    - get cell count, column %, chi-square, & gamma or lambda
    - use *Pearson chi-square*, and get Asymp Sig (= p value)
  - Summary table @ board
- ◆ Lab: is the US in Decline?
  - Now you try. ☺
  - Handout and data are on the web
  - Use USDECLINE as the IV (makes more sense!)

SOC497 @ CSUN w/ Ellis Godard 37

Admin Review Chi-square Piles Choices Summary

### 5. Which is the correct choice?

- A. Gamma for 2 nominals  
3%
- B. Lambda for 2 intervals  
6%
- C. Lambda for 1 nominal & 1 ordinal  
81%
- D. Gamma for 1 ordinal & 1 nominal  
8%
- E. Chi-square for one nominal & 1 interval  
3%

SOC497 @ CSUN w/ Ellis Godard

00

Admin Review Chi-square Piles Choices Summary

### Team Scores

Points	424 With?	Points	424 With?
3	Someone else		
2.99	Godard		
2.98	Campbell		
2.67	Bogumil		
2.67	Mavvadat		

SOC497 @ CSUN w/ Ellis Godard

39