

 **crispin lover**  
@hog\_mild


Mean Girls implies the existence of  
Median Girls, Mode Girls, and Range  
Girls

11:44 AM · 2021-02-09 · Twitter for iPhone

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## My Frozen Dinner: Another LOM e.g.



- Pork chops (pork -> nominal)
- Size of the chop (medium? -> ordinal)
- Number of corn kernels (interval, discrete)
- Amount of potatoes (interval, continuous)

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Where we are in the semester...

#	Date	Read (5th)	Due	Area	Lecture Topic	Lab #	Lab Assignment	T Lab	R Lab
1	Tue Aug 26	1.1 to 1.4		Overview	Welcome & Orientation				
2	Thu Aug 28	1.1 to 1.4		Overview	Basic Terms				
3	Tue Sep 2	2.1 & 2.5			Measurement Issues	1	Levels / Age 3x	1	
4	Thu Sep 4	3.1			Data Reduction	2	Means & SD	1, 2	
5	Tue Sep 8	3.1			Display & Analysis of Data	3	Four 3x3	3, 4	
6	Thu Sep 11	3.2 & 3.5			Central Tendency	4	GI		3, 4
7	Tue Sep 15	3.1 & 3.4			Dispersion	5	Dispersion	5, 6	
8	Thu Sep 18	3.7			Indices & Data Cleaning	6	Music Index	5, 6	
9	Tue Sep 23	4.2			Probability & Z Scores	7	Standardizing Scores	6, 7	
10	Thu Sep 25	4.3			Z & Pz	8	Table A	7, 8	
11	Tue Sep 30	3.6 & 5.1		HW2	Parameters & Pt Estimation	9	Distances	8, 9	
12	Thu Oct 2	2.2 to 2.4 & 4.3			Sampling (Issues, Methods, Effects)	10	Sampling	9, 10	
13	Tue Oct 7	4.4 to 4.6			The Central Limit Theorem	11-EC	CI: World (EC)	10, 11*	
14	Thu Oct 9	5.3			Confidence Intervals	12	CI for Intervals	11*, 12	
15	Tue Oct 14			HW3	CI for Proportions	13	CI for Proportions	12, 13	
16	Thu Oct 16	6.1 & 6.4			Hypothesis Testing & Zs	14	Writing Hypotheses	13, 14	
17	Tue Oct 21	6.4			Hypothesis Testing for Large ns	15	Two Tests	14, 15	
18	Thu Oct 23	6.3 & 6.8		HW4	The "t" test, for small ns	16	GI & Test Ages	15, 16	
19	Tue Oct 28				Sample Size Estimation	17	Estimating n Needed	16, 17	
20	Thu Oct 30	7.1, 7.3, & 10.1			Differences in Means	18	Comparing Means	17, 18	
21	Tue Nov 4	7.2		HW5	Differences in Proportions	19	Comparing Proportions	18, 19	
22	Thu Nov 6	12.1			Analysis of Variance	20, 21-EC	ANOVA (+ MODEL EC)	19, 20, 21	
23	Tue Nov 13	9.4 & 9.5			Scatterplots & Correlation	22	Grade Correlations	22	
24	Thu Nov 18	8.1 to 9.3		HW6	Regression	23	Regression Lab	20, 21*, 22, 23	
25	Tue Nov 20	10.2 & 11.1			Multiple Regression	24-EC	Multiple Reg (EC)	23, 24*	
26	Thu Nov 25	8.1		HW7	Crosstabulations	25	TBA (any)	24*, 25	
27	Tue Dec 2	8.2 & p 233			Dependence	26, 27-EC	TBA (SCU) (& 27-EC)	26, 27*	
28	Thu Dec 4	pp 230 to 243		HW8	Association	28-EC	Measures of Assoc (EC)	25, 26, 27*, 28	
29	Tue Dec 9				(no lecture - work session only)				
30	Thu Dec 11				(no lecture - work session only)				
31	Tue Dec 16			HW9	(no meetings - deadline only - exam, final)				

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## Administrative Notes

- **Labs/Grades OTW**
  - L1 back now
  - L2 & HW1 coming by Friday
  - PDF updated & PR emails out on Friday
- **Check portal asap to make sure**
  - added classes have been added,
  - dropped classes have been dropped,
  - and no surprises found ☺
- **Check grading sheet for**
  - Codename & Grades (esp. attendance) okay?
  - Still missing two Intake Forms & 2 headshots

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# CENTRAL TENDENCY

SOC424 – Statistics w/ Dr. Ellis Godard

## Means, Medians, & Modes – oh, my!

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## Outline for Today

- **Overview of Course Direction** (4 parts)
- **Central Tendency**
  - Concept: What's typical?
  - Measures: options, formulas, examples, & choices
  - CT in SPSS: Demonstrations & Trials
- **Lab Exercise:** Describe some data

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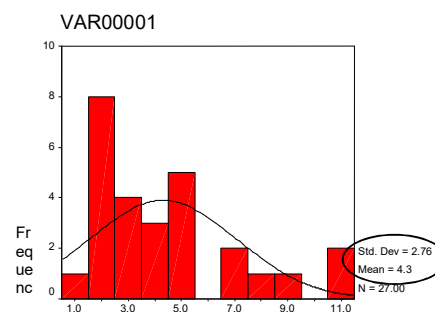
## Toward Bivariate Inference...

- Want to make inferences about a population based on data from sample
  - Estimate the parameters from the statistics
  - For example, population mean from sample mean
    - "Mu" from "Ybar"
- Start w/ sample (i.e. descriptive) statistics
  - How to summarize your data
- Build towards discussion of parameters
  - Then will be ready for *bivariate* statistics

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## You've already seen 1 of each...



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## Course Direction

We'll look at statistics in this order:

- **Descriptive** statistics for **univariate** data
  - **Inferential** statistics for **univariate** data
- then ....*
- **Descriptions** of **bivariate** relationships
  - **Inferences** from **bivariate** relationships

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## 3 Measures of Central Tendency

- **Mode**
  - most frequently occurring value
- **Median**
  - middle value, when cases ordered by value
- **Mean:**
  - arithmetic average, "center of gravity"

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## Univariate Descriptive Statistics

- **Central tendency**
  - Where is the data centered?
  - What's the typical value?
  - Do different kinds of centers differ?
- **Dispersion**
  - How are the data spread out?
    - Widely? Narrowly?
    - Highly concentrated or very dispersed?
- You've seen 1 of each already...

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## What's New & What Isn't

- You learned those stats in 5<sup>th</sup> grade (maybe 4<sup>th</sup>? 6<sup>th</sup>)
- But I recognize that **there are new things** about them now
  - **Opening a dataset** (FILE>OPEN>DATA)
  - **Getting those stats from SPSS**
    - Always check 6: mean, median, mode, quartiles, std dev, & range
  - **Choosing variables** (nominal, ordinal, & interval)
    - Don't use the Measure column – look @ the Values column
  - **Choosing which statistic to use for which variable**
    - Guidance throughout (and again @ the end of) this lecture
  - **Putting them in a meaningful sentence**
    - Not for a mathematician – for a relative, boss, neighbor, etc.
    - Reporting & Interpreting them – not just the number; what's it *mean*?
    - Describe the sample / Summarize the data

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## About Modes...

- = the most frequently occurring score
- Any level of measurement *might* have one
  - Could be *no* mode (equal distribution)
  - Could be *more* than one (bimodal, tri-, etc)
    - But don't go overboard – looking for **concentrations**
- = the *least* you can say about center
  - Might not even be center – could be 1 end
  - Doesn't utilize differences among values
  - Ignores all non-modal values
- In a *symmetrical* (more soon) distribution:  
mean = median = mode

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## Properties of Medians...

- can use for ordinal data
  - *must* be at *least* ordinal level data
  - positional measure
    - 50% above, 50% below – like a percentile ranking
- does not use all information from the data
  - generally not affected by outliers
- inference procedures are difficult
  - cannot be manipulated algebraically

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## About Medians...

- Proportional measure
  - Score that falls in the middle *when they're ranked by magnitude*
  - 50<sup>th</sup> percentile, ½ above and ½ below
  - Cumulative percentage shows it – find the first value w/ cum % > 50
- It's a value, not a case
  - Of {0, 3, 7, 8, 8}, it's 7
  - If Larry had a value of 7, the median is 7, not Larry
  - The *third case* is in the middle, & the *value* of that case is 7, *not* 3
  - Of {3, 4, 7, 8, 8} it's still 7, the value of the 3<sup>rd</sup> case, *not* 3
- It's the value of the middle case, when they're in order
  - In {8, 7, 3, 0, 7}, it's still 7

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## About Means (Notation Intro.)

- $\mu$  = "Mu" = population mean
- $\hat{Y}$  = "Yhat" = estimate of a value
- $\bar{Y}$  = "Ybar" = sample mean
  - sum over each case (until you reach end) & divide by sample size
  - Just a simple "average"
    - "Average" sometimes used w/ non-interval data
    - Only interval data has a mathematical average

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## About Medians...

- If  $n$  = odd, there is a unique median {0,3,7,8,8}
  - Rank scores, find *value* of the middle case (NOT the middle value)
  - If there are 5 cases, median case is  $(5+1)/2 = 3^{\text{rd}}$  and the *value* of that case is 7 (not 3!)
- If even number of cases - e.g. {0,7,8,8}
  - Some say to average the middle two positions
    - Average of value at position  $(n/2)$  and the next one:  $(n/2) + ((n/2)+1)/2$
  - But that's weird... no case had a value of 7.5; how could there be a median that doesn't even exist?
  - Better to report both ("median of 7 to 8"), though usually they'll be the same (because you'll have 100s or 1000s of cases)

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## Basics of Statistical Notation

- $N$  = population size;  $n$  = sample size
- $Y_i$  = each particular case
  - Individual person, school, church, etc.
  - *Not* the sample, but a single element of it
- $Y_1$  = 1<sup>st</sup> case
- $Y_n$  = last case
- $\Sigma$  = summation

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## Properties of Means...

- Uses all data/scores
- Manipulated algebraically easily
  - so lends itself to statistical inference procedures
- Must have interval data
  - Can't add and divide meaningfully if not equidistant
- Affected by outliers (extreme values)
  - like a fulcrum – center of gravity of data
- Best computed for bell-shaped distributions
  - not as good if bimodal or heavily skewed

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## Comparisons w/ Descriptives

- Imagine these three variables:
  - Preferred network
    - That's nominal – no mean or median
  - Amount of time spent online
    - If the values are "some", "lots", "too much", that's ordinal – no mean
  - Number of friends
    - If that's an actual count, we can average them
- Using the appropriate measure of central tendency, we could compare two different samples, or subgroups...

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## Weighted Means

- Imagine separate means, for 2 groups
  - e.g. avg hats owned by 5 girls and 50 boys
  - Can't just average averages
  - But girls' hats avg = total girls hats / 5, and boys' hats = total boys hats / 50
  - So if you multiply each group's avg, by # in that group, you can reverse engineer the separate totals
  - And adding the two separate totals, is like adding all of the individual scores w/o having them
- So, variation: weighted average
  - overall mean for combined set of samples
  - weight by # cases in each set
 
$$(N1Ybar1 + N2Ybar2 \dots) / (n1 + n2 \dots)$$
  - $(5*girlsavg + 50*boysavg) / (5+50)$

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## Comparisons w/ Descriptives

Social Media Use by Men				
	Mean	Median	Mode	Dispersion
Preferred network	x	x	LinkedIn	53% (variation ratio)
Amount of time	x	"Some"	"None"	2 (range)
Number of friends	267.4	163	29	8.35 (std. dev) or 86 (IQR)

Social Media Use by Women				
	Mean	Median	Mode	Dispersion
Preferred network	x	x	Instagram	62% (variation ratio)
Amount of time	x	"Some"	"Tons"	2 (range)
Number of friends	345.2	119	42	11.72 (std. dev) or 112 (IQR)

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## Non-Computer Examples

- Find the median of:
  - {black, black, white, Asian, white}
- Find the mode and median of:
  - {4, 6, 12, 7, 10, 3, 4}
- Find median of:
  - {4, 6, 12, 10, 3, 4}
- Find mean, median, & mode for
  - {2, 2, 7, 8, 3, 2, 11, 13, 9}
- More?
- Find the mean, median, & mode for
  - {7, 6, 10, 7, 5, 9, 3, 7, 5, 13}

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## 3 Measures of Central Tendency

	Formula	Appropriate if...
Mean	Simple average (the sum of all the values, divided by the number of values) $\bar{Y} = \frac{\sum_{i=1}^n Y_i}{n}$	interval (unless heavily skewed); is not meaningful for nominal, & arguably not for ordinals – just interval variables!
Median	If even number of cases, the median case (not value) is the (n/2)th case. Otherwise, it is the [(n+1)/2]th case	Interval (if skewed); ordinal (unless mode is a majority?) – nominals don't have a middle
Mode	Highest (relative) frequency	Esp. nominal (no other choice) but any (?)

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## Means or Medians for Interval?

- If a distribution is symmetric, mean = median
  - If distribution is normal, mean = median = mode
- If a distribution is skewed, the mean is in the direction of the skew from the median
  - If skewed to right, mean is higher than median
  - If skewed to left, mean is lower than median
- Distribution = like seesaw for the median
  - Add more on one end, it may slide in that direction
- But like magnets for the mean
  - Any addition anywhere pulls mean that direction

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## HW Hints / Clarifications

- **“Report”** includes giving the actual value
  - not just the number e.g. 1 for gender, but *which gender*
- **“Interpret”** means making sense of it
  - Not just 12.4 for # of years of educ, but “some college, on avg”
- Summarize clearly
  - State in terms of the sample
- Make full use of the CT measure
  - Describe the typical case
- Mode is not “most” – just most *common*
  - “most” implies well above a majority (>50%), but mode could be 8%

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## Criteria for Selection

**What makes a measure of central tendency (or dispersion) “appropriate”? (in order of importance)**

1. **Scale of measurement** – no medians or means for nominal data; don’t trust means for ordinal data;
2. **Shape of distribution** – for skewed interval data, mean + median say different things; which helps most?
3. **Robustness** – Here, a statistic is “robust” if it resists sampling deviations. The mean is fairly robust, but the median is less misleading if there are scraggly tails
4. **Efficiency** – use highest level of precision appropriate for level of measurement (modes are least precise; means most)
5. **When in doubt, use more than one** – may need to triangulate center—pinpoint using multiple measures

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## Lab Exercise

- Get GSS2018-trimmed.sav from Canvas - 745 variables
- Pick 3 variables, 1 @ each Level of Measurement (N, O, & I)
  - To determine LOM, use the Values column and/or frequency distributions and/or the actual survey – but do NOT use the “Measure” column in SPSS
  - In the Values column, any variable might have missings (97, 98, 99?) but *only* nominal and ordinal variables need other labels (intervals values *are* labels)
- Get *all* measures of central tendency for each, & print
  - When getting a frequency distribution, Click “Statistics” then click Mean, Median, and Mode
- Write at least a sentence about each variable:
  - Be clear about what each variable *measures*
    - It may look like a math class, but we’re doing sociology
  - Report *appropriate* measure(s) of central tendency
    - Do not *report* (write about) all of them. Use criteria outlined above.
    - Do not simply report the choice (e.g. mean) or the value (e.g. 3); use the statistics to describe the sample (e.g. mostly female, highly educated, mostly happy with the class)

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## Last point about estimates...

- **“Y-bar”** is mean of a sample
  - vs **“Mu”** (the population mean)
  - Anything w/ a  $\hat{\phantom{x}}$  is an estimate
- e.g. **“Y-hat”** is an estimate of **“Mu”**
  - not the only way to estimate it, nor the best
  - just the easiest; it’s a “point estimate”
- **Doesn’t take into account dispersion**
  - Sampling theory allows us to consider disp.
  - Will delve into that next lecture... but first...

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