

Sociology 364

Handout on Computing Sample Sizes

A. Sample Size Required for Estimating the Population Mean

If we want the “margin of error” to be smaller than some value B , with a probability of at least $1 - \alpha$, the appropriate sample size is obtained as follows

$$n = s^2 \left(\frac{z_{\alpha/2}}{B} \right)^2$$

Derivation:

$$B = z_{\alpha/2} \left(\frac{s}{\sqrt{n}} \right) \quad (1)$$

Another name for B is the “margin of error”

$$\sqrt{n} = z_{\alpha/2} \left(\frac{s}{B} \right) \quad (2)$$

Rearrange the terms

$$n = s^2 \left(\frac{z_{\alpha/2}}{B} \right)^2 \quad (3)$$

Square each side

B. Appropriate Sample size to estimate p (See Agresti and Finlay, p 107, for derivation)

Similarly, assuming $\pi = 0.50$ (which allows for a conservative estimate of the standard error), the appropriate sample size n to estimate a population proportion with probability $1 - \alpha$ is found as follows

$$n = .25 \left(\frac{z_{\alpha/2}}{B} \right)^2$$

Examples

Problem 34 (p. 118), Agresti and Finlay.

Step 1: State the Formula

Since, the problem involves calculating the appropriate sample size to calculate a *population proportion*, the appropriate formula is

$$n = s^2 \left(\frac{z_{\alpha/2}}{B} \right)^2$$

Step 2: Find the Necessary Values

- a. We are told that the requisite probability is 0.95, thus $1 - \alpha = 0.95$ and $z_{\alpha/2} = z_{0.025} = 1.96$.
- b. The allowed margin of error B is given as 5 acres.
- c. The standard deviation σ is also given as 50.

Step 3: Substitute these values into the formula:

$$\begin{aligned} n &= 50^2 \left(\frac{1.96}{5} \right)^2 \\ &= 384 \end{aligned}$$

Step 4: Clearly State Your Conclusion

For example: "In order to estimate the mean acreage of farms in Brazil to within 5 acres, with a probability of 0.95, we would need to draw a sample of size 384." In other words. if we repeatedly drew samples of size 384, our estimate of farm size would be accurate -- give or take (+/-) 5 acres -- 95 percent of the time.