

# Math 140

## Introductory Statistics

Math 140 tutoring:  
LIVE OAK 1319

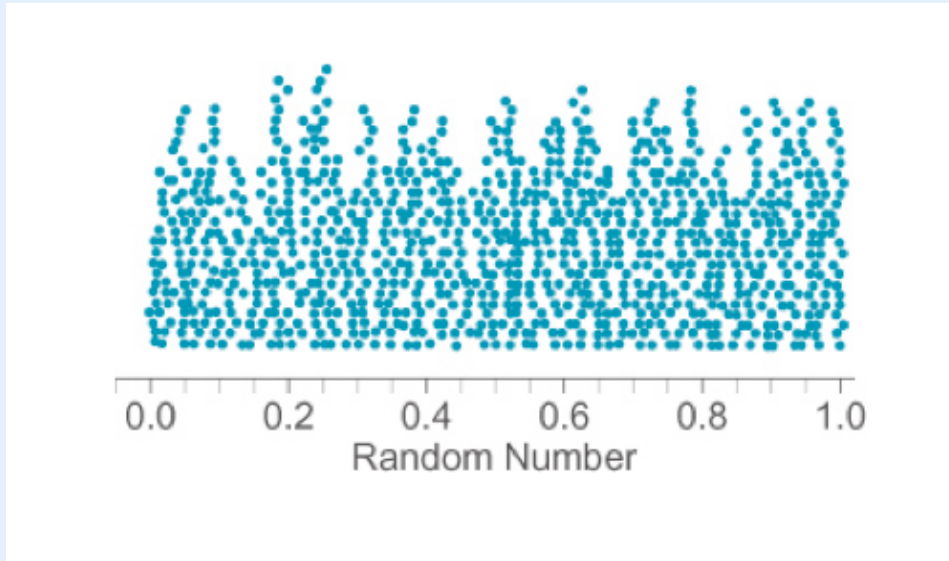
MW 11:30 - 4:30    TTh 3:30-5:30    F 10:30-12:30

General Hours:

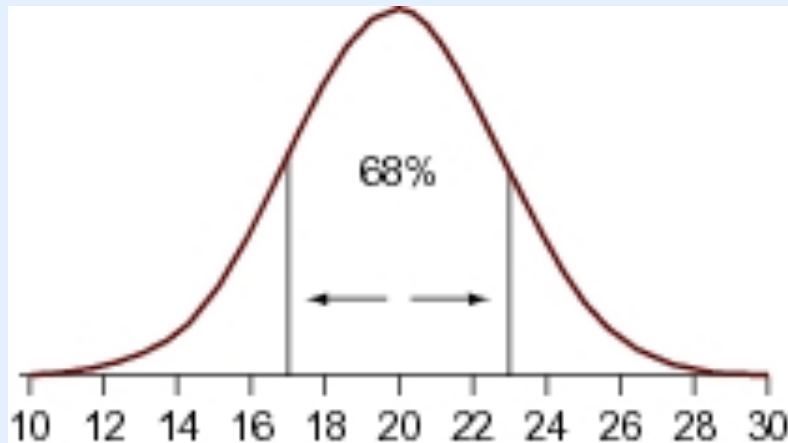
M - Th 10:00 - 5:30    F 10:00 - 3:00

Later: Saturday from 11 to 2.

# Last time

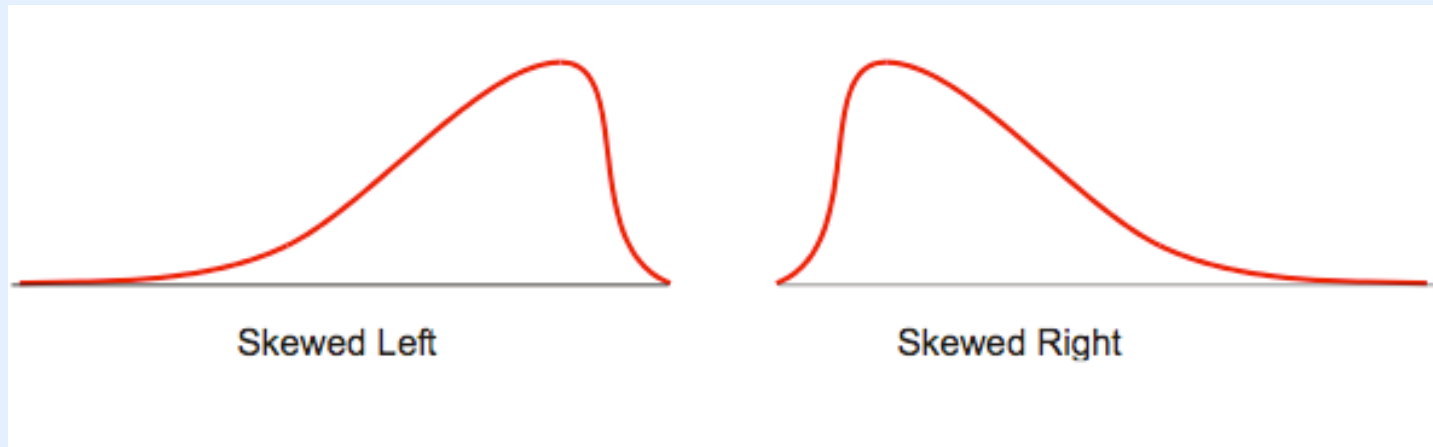


Uniform - rectangular  
distribution



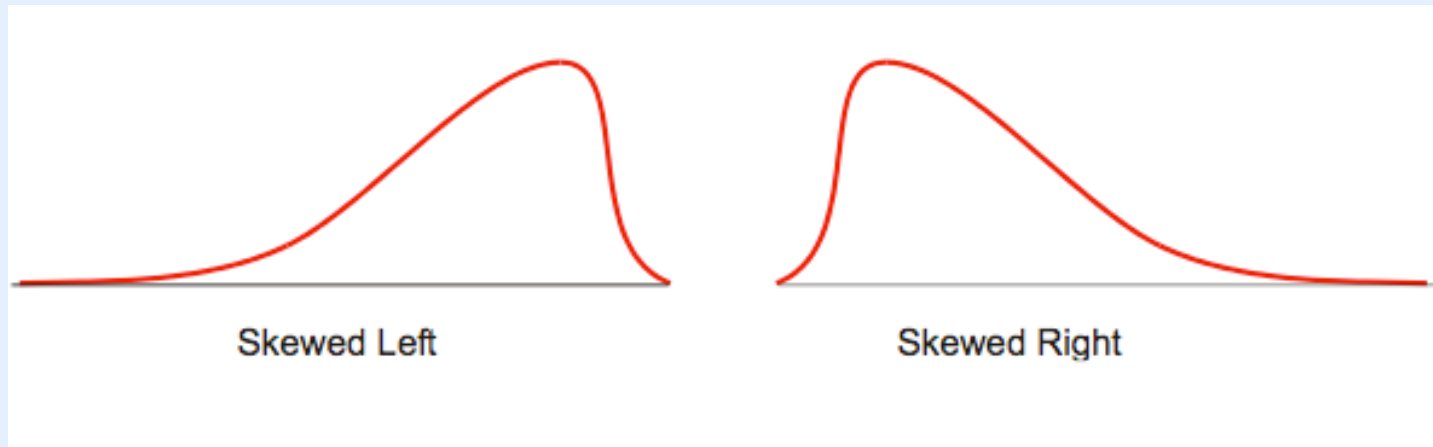
Normal distribution  
mean  
inflection points  
standard deviation

# Skewed distributions



Not symmetric curves  
Data is bunched on one end  
and a tail appears on the other side

# New tools



## Median:

The value of the line dividing the number of values in equal halves

The area (or the number of points) to the left or to the right of the median are equal

# New tools



## Quartiles:

Once you have found the median, look at the left of the distribution and repeat the same procedure.

This new value is called the **lower quartile Q1**

Repeat on the right, and find the **upper quartile Q3**

# Median, lower and upper quartiles

They divide the distribution in quarters.

How much data is contained between Q1 and Q3?

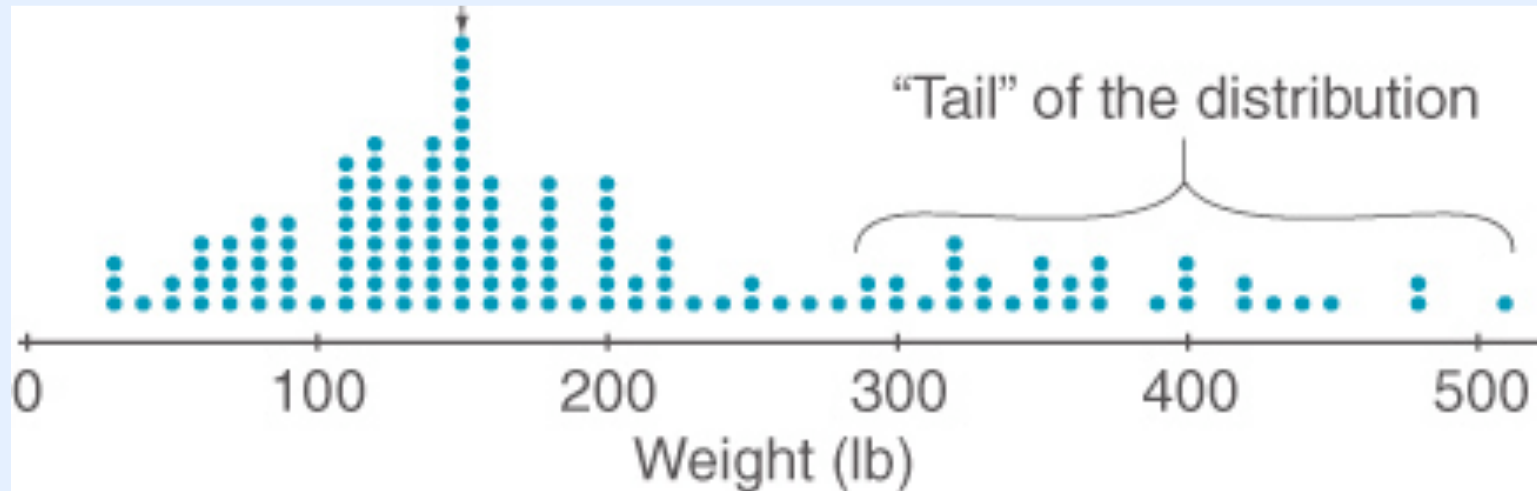
# Median, lower and upper quartiles

They divide the distribution in quarters.

How much data is contained between Q1 and Q3?

50%

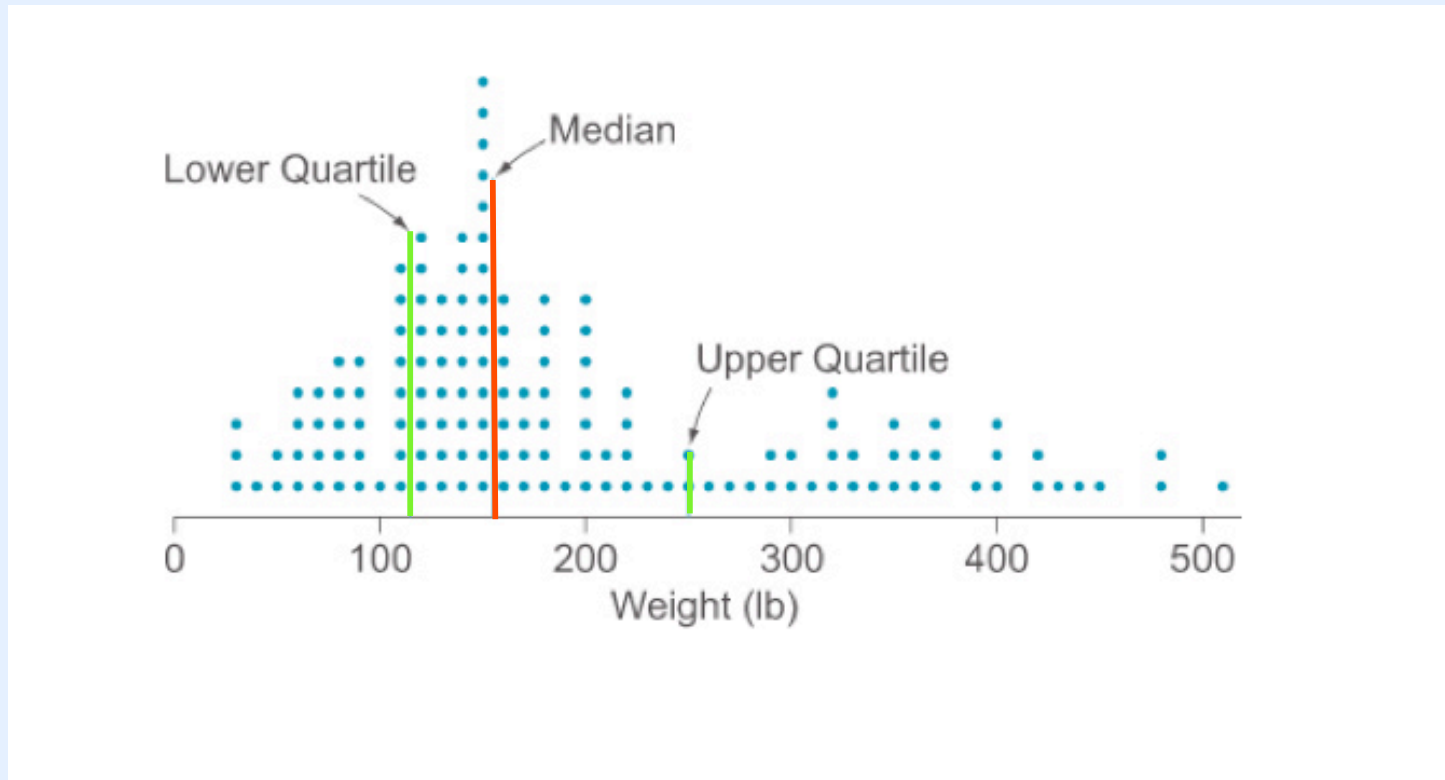
# Example - the weight of bears



Find median, Q1 and Q3



# Example - the weight of bears



Median ~ 155 lb

Q1 ~ 115 lb

Q3 ~ 250 lb

# Outliers, gaps and clusters

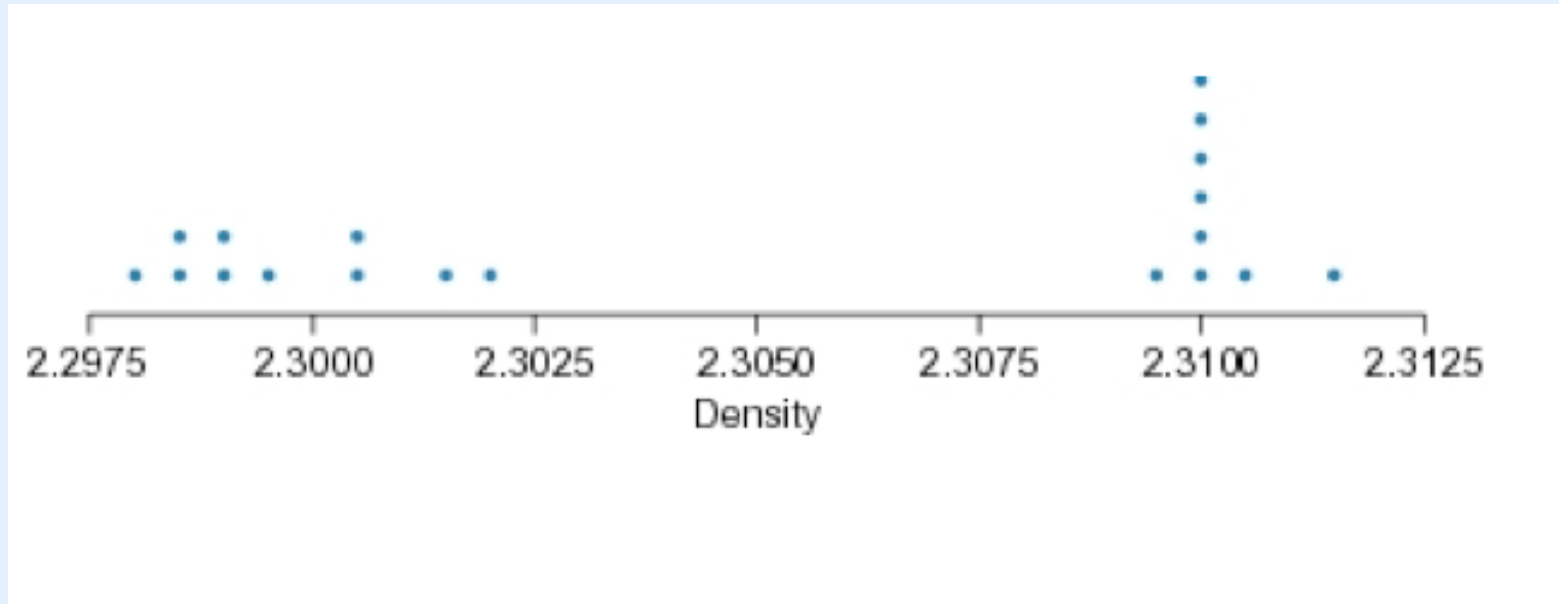
outliers are “special” values that stand out  
when we look at the distribution

mistakes? Just flukes (a really really big bear!)  
sometimes they can lead to interesting discoveries

gaps and clusters

“informal” definitions

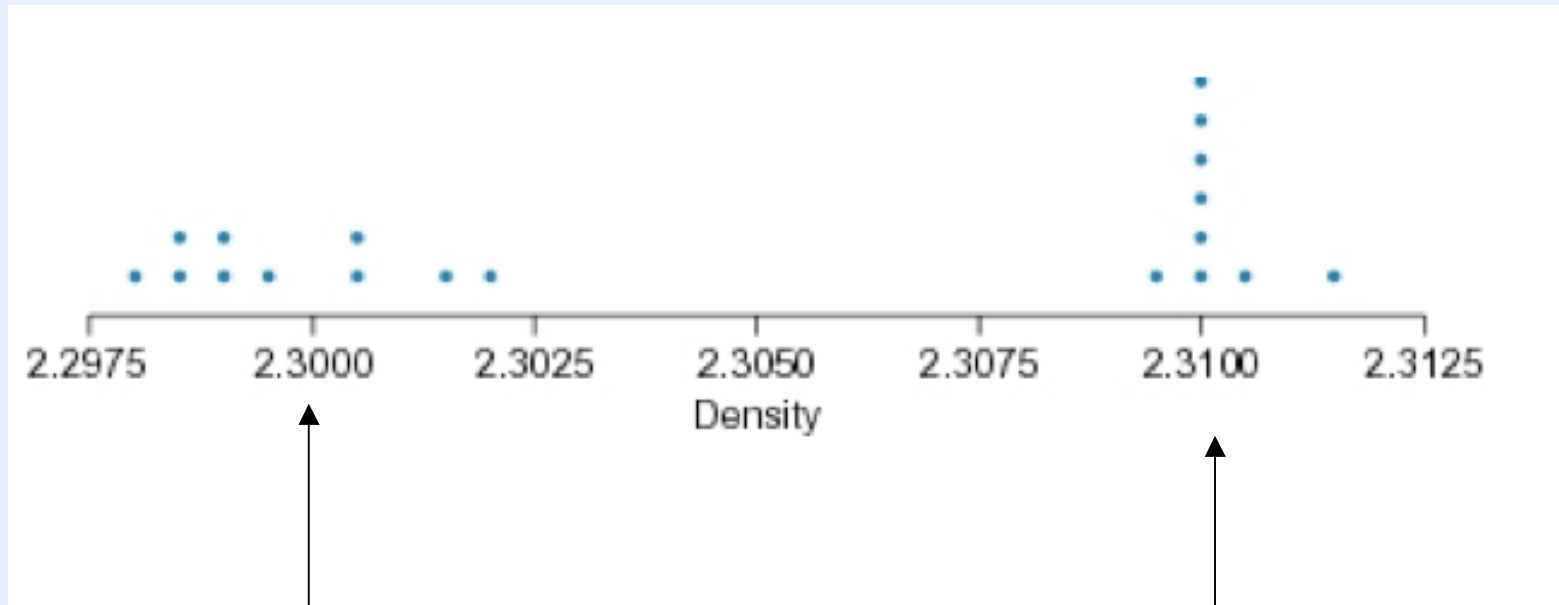
# Outliers, gaps and clusters



Lord Rayleigh's densities of nitrogen

what is different between the two?  
why two clusters?

# Outliers, gaps and clusters

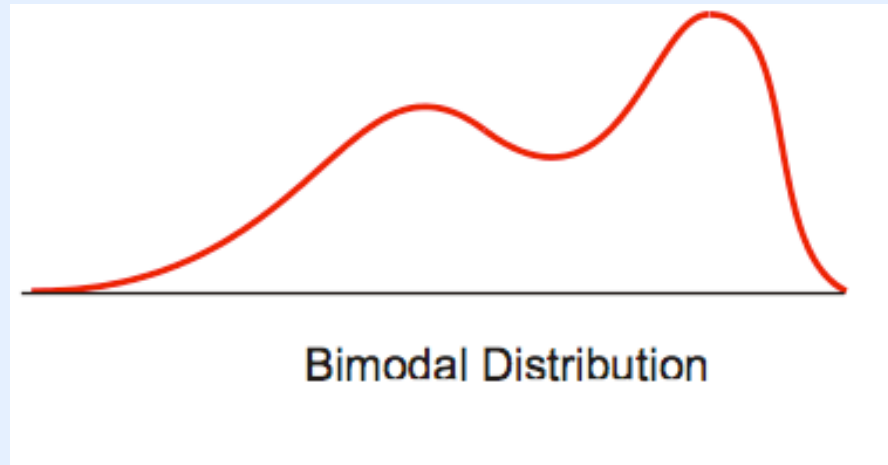


Chemically produced

Atmospheric

There might be something else in the atmosphere!

# Bimodal distributions



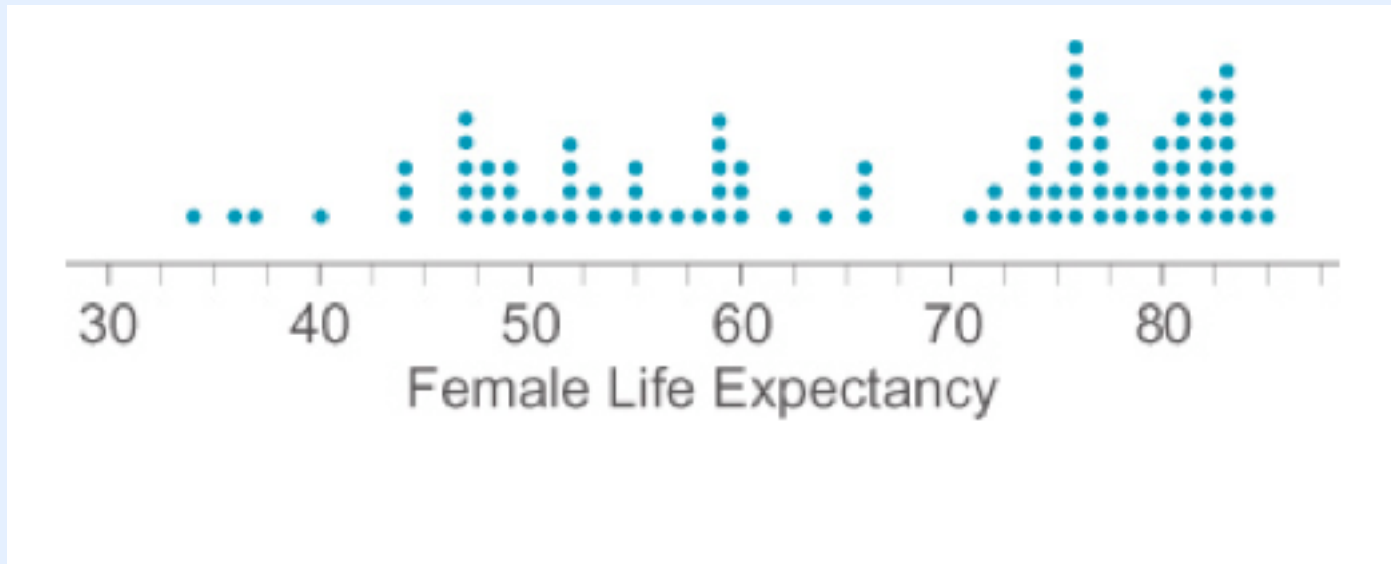
Some distributions have two peaks instead of one

Unimodal (one peak)

Bimodal (two peaks)

Multimodal (many peaks)

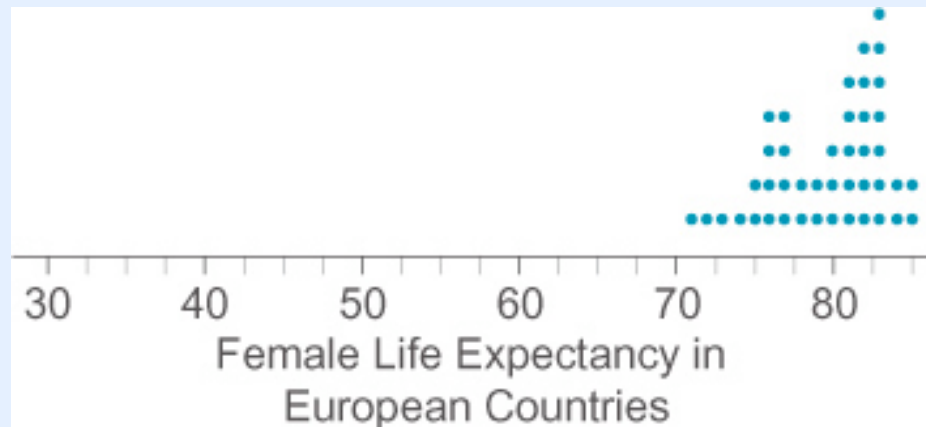
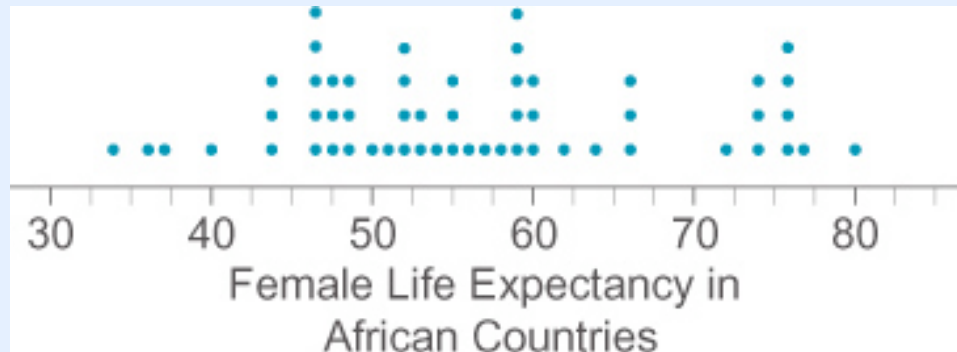
# Example



Bimodal - what to make of this?

is there other info we can use?

# Splitting data



Africa - spread out

Europe - skewed to left

# Quantitative vs. categorical data

Quantitative : data in form of numbers  
that can be compared and  
that can take a large range of values

Categorical : a case can belong to a category or not



How to look at quantitative data?

# 1. Dot plots

Each dot represents a case

Dots may represent more than one case  
(one dot may represent 1000 cases - USA births)

We can use different symbols for different  
Categories of data

# Dot plots work best when

Relatively small number of values to plot

Want to keep track of individuals

Want to see the shape of the distribution

Have one group or a small number of groups that we want to compare

Making plots by hand

## 2. Histograms

Similar to dot plots but where data is grouped

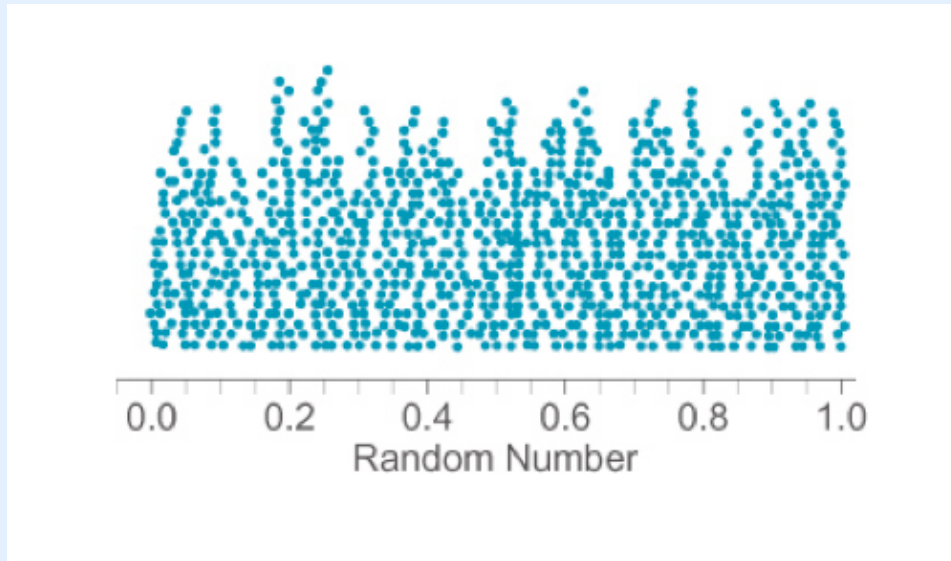
Groups of cases represented as rectangles or bars

The vertical axis gives the number of cases  
(called frequency or count)

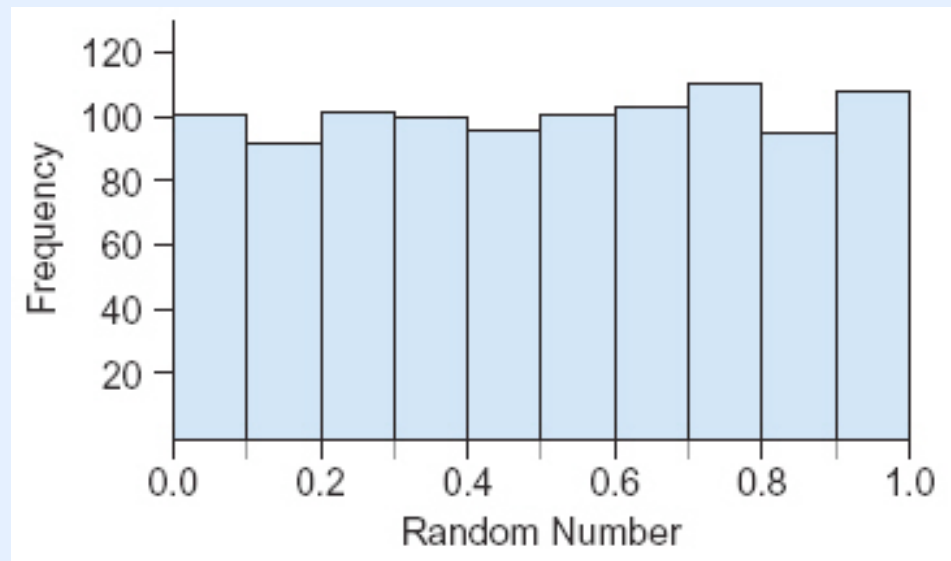
By convention borderline values  
go to the bar on the right.

There is no prescribed number for the width of the bars.

# Random numbers

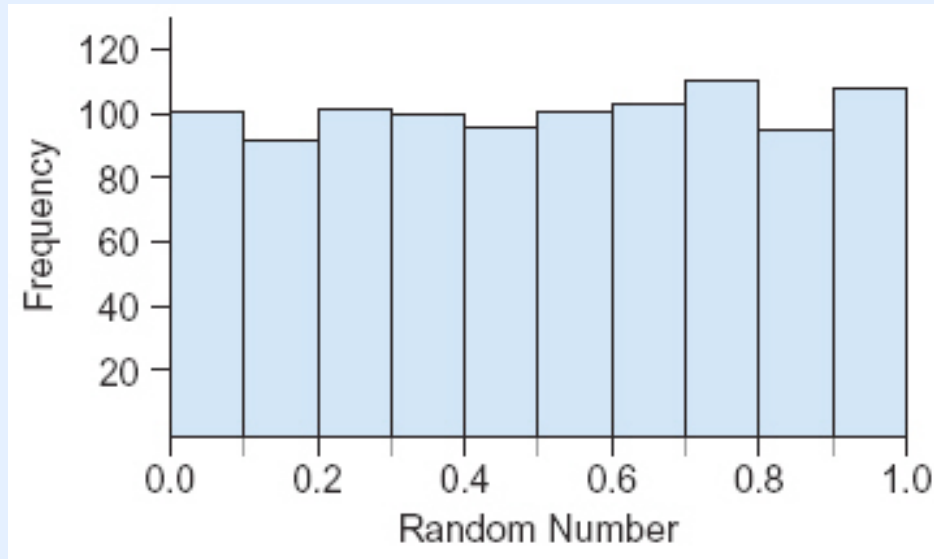


Dot plot



Histogram

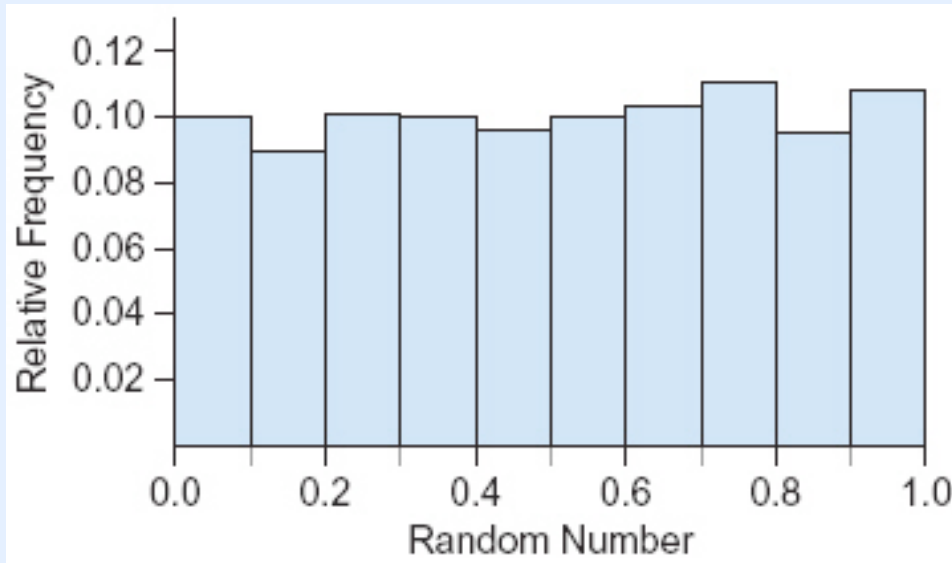
# Histograms



A histogram is like a 'coarse grained' dot plot  
'bins' on the x-axis  
'frequency' on the y-axis

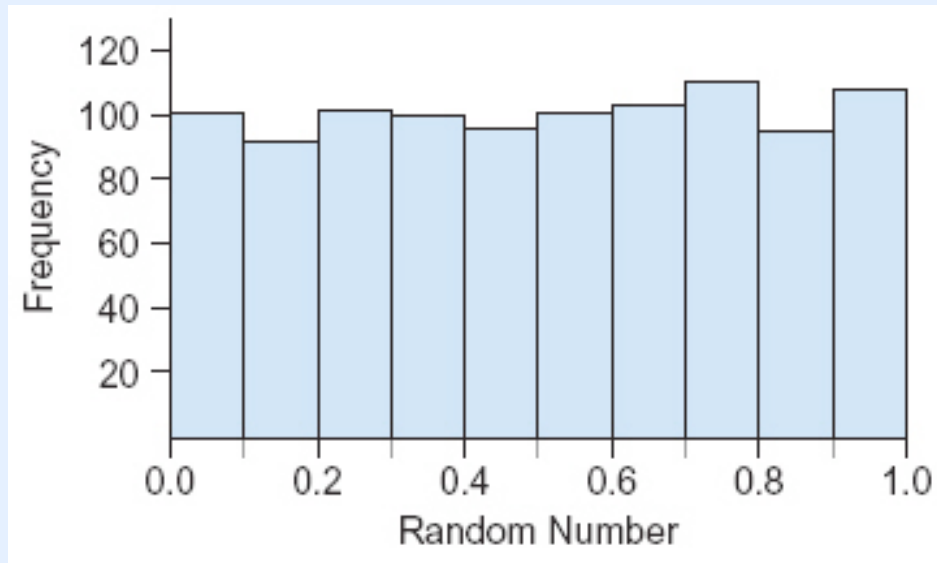
We can choose bin size any way we like

# Relative Frequency

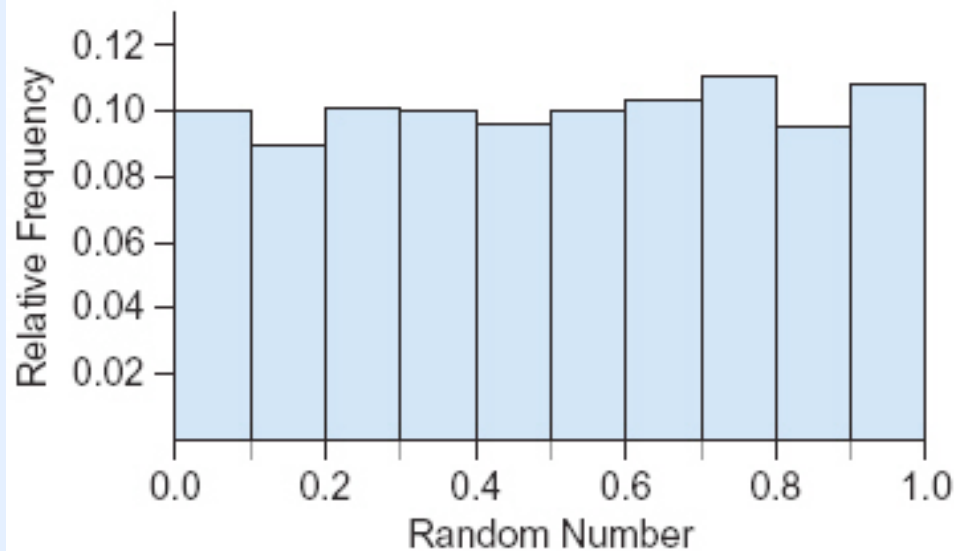


The sum of all heights is one

# Frequency and Relative frequency



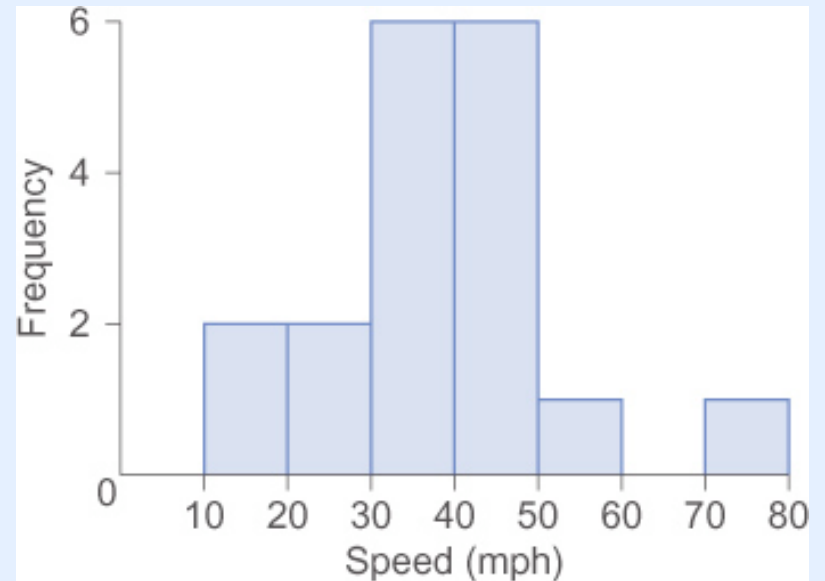
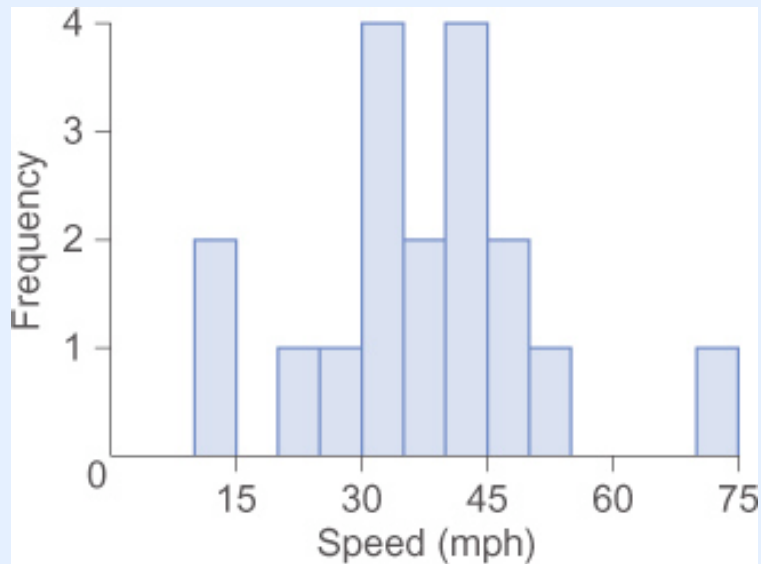
actual occurrences



percent of total  
(in this case  
divide by 1000)



# Different bin choices



Speed of mammal species  
Using two bar widths

**THERE IS NO RIGHT OR WRONG**

# Histograms work best when

Large number of values to plot

Don't need to see individual values exactly

Don't want to see exact shape of distribution

Have one distribution to look at

Use a calculator or computer

# 3. Stemplots

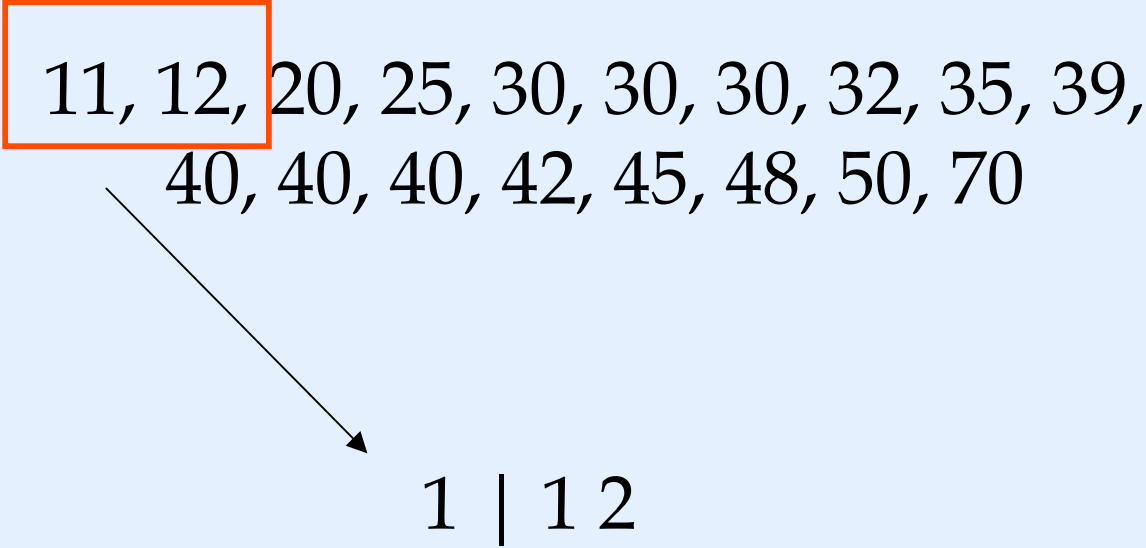
Speeds of mammals (mph)

11, 12, 20, 25, 30, 30, 30, 32, 35, 39,  
40, 40, 40, 42, 45, 48, 50, 70

# 3. Stemplots

Speeds of mammals (mph)

11, 12, 20, 25, 30, 30, 30, 32, 35, 39,  
40, 40, 40, 42, 45, 48, 50, 70



1 | 1 2

# 3. Stemplots

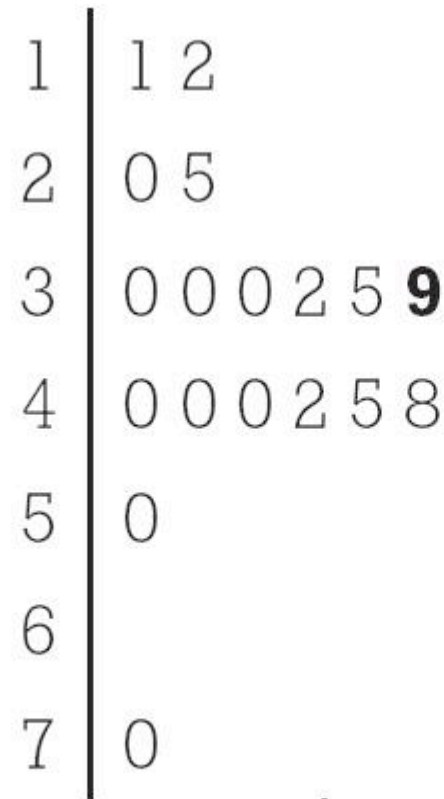
Speeds of mammals (mph)

11, 12, 20, 25, 30, 30, 30, 32, 35, 39,  
40, 40, 40, 42, 45, 48, 50, 70



3 | 0 0 0 2 5 9

# 3. Stemplots



3 | 9 represents 39 mph

# 3. Stemplots

Or stem-and-leaf plots

Numbers on the left are called stems  
(the first digits of the data value)

Numbers on the right are called leaves  
(the last digit of the data value)

# Split stemplots

```
1 | 1 2
•
2 | 0
• 5
3 | 0 0 0 2
• 5 9
4 | 0 0 0 2
• 5 8
5 | 0
•
6 |
•
7 | 0
```

3 | 9 represents 39 mph



# Split stemplots

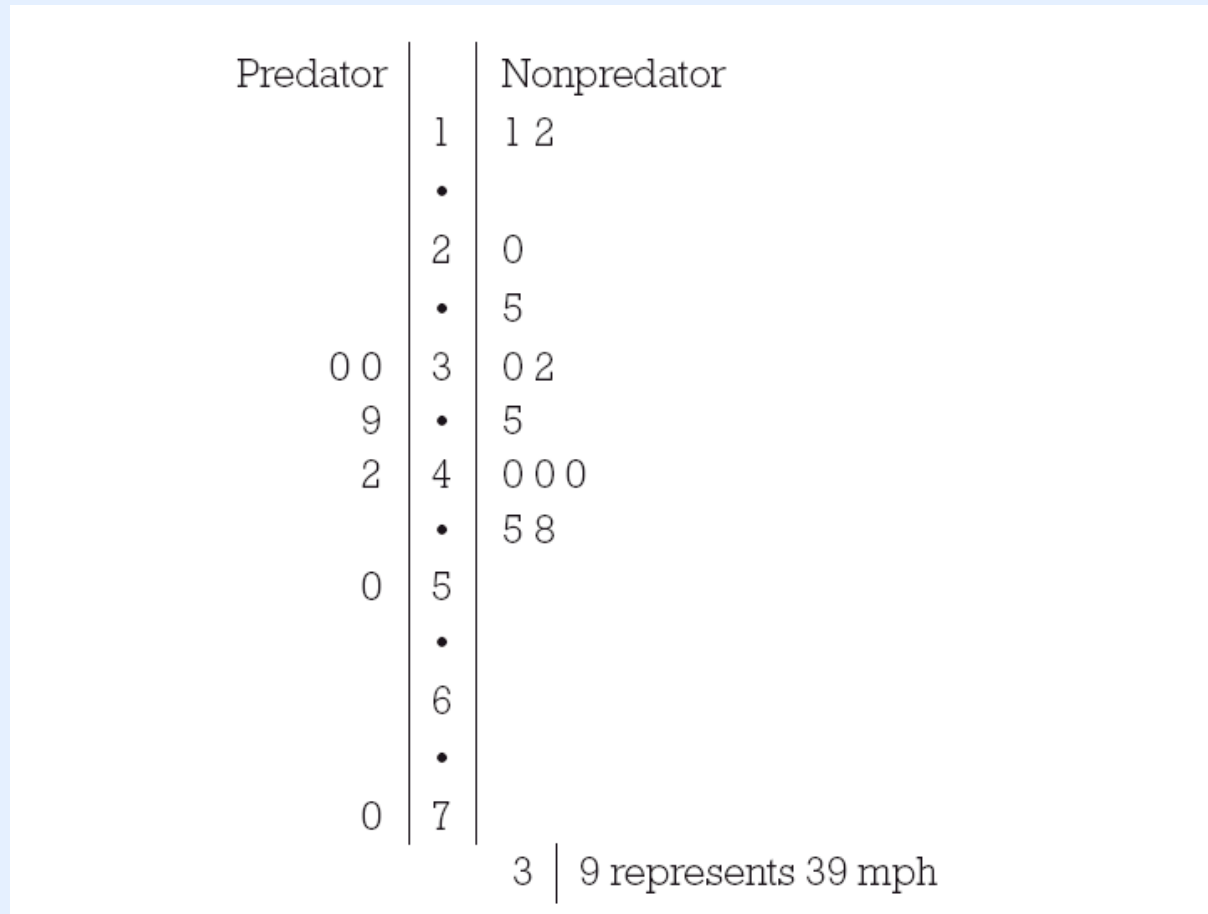
1		1 2
•		
2		0
•		5
3		0 0 0 2
•		5 9
4		0 0 0 2
•		5 8
5		0
•		
6		
•		
7		0

3 | 9 represents 39 mph

The unit digits  
0,1,2,3,4 are associated  
with the first stem and  
they are placed on the first  
line.

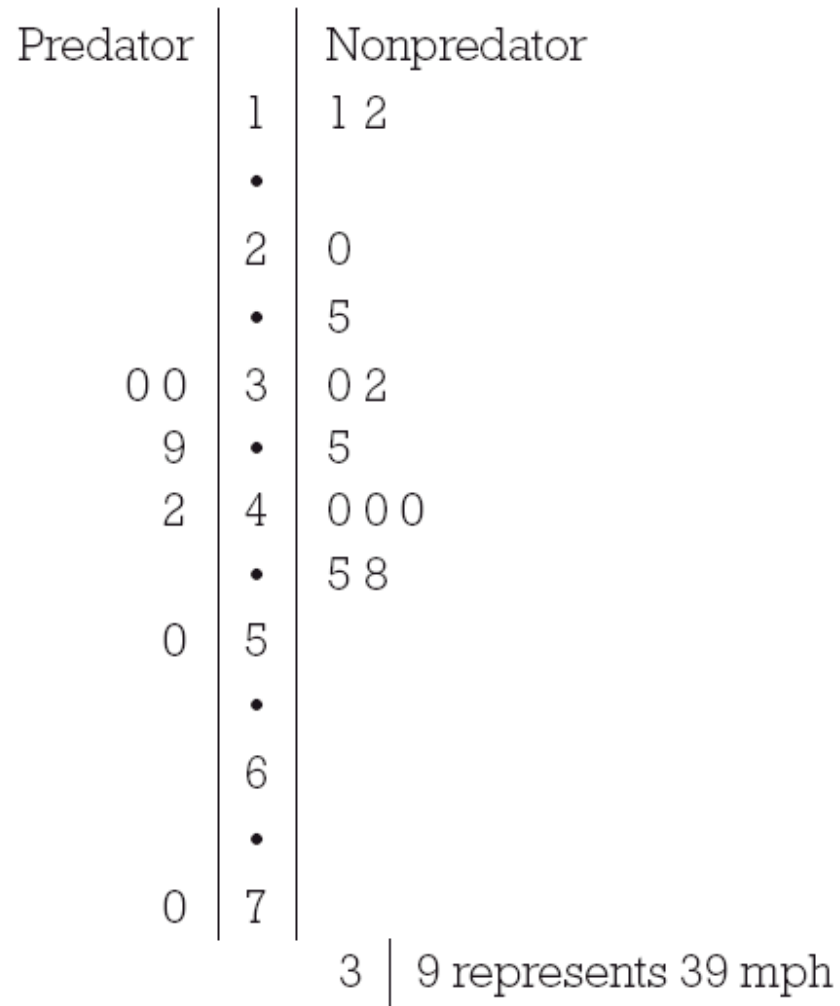
The unit digits 5,6,7,8,9 are  
associated with the second  
stem  
and they are placed on the  
second line.

# Back to back stemplots



The data is differentiated on whether the mammals are predators or non-predators

# Who has the faster speed?



# Calculating medians and quartiles

Stem-and-leaf of Speeds      N = 18  
Leaf Unit = 1.0                      N\* = 21

2	1 12	
2	1	
3	2 0	
4	2 5	Lower quartile = 30
8	3 ①002	Median = 37
(2)	3 5 9	
8	4 000②	Upper quartile = 42
4	4 58	
2	5 0	
1	5	
1	6	
1	6	
1	7 0	

# Stemplots work best when

Small number of values to plot

Want to keep track of individual values  
(at least approximately)

Want to see shape of distribution

Have two or more groups that we want to compare

Hk

Page 45 E16, E17 a/b, E13, E14