# Math 140 <br> Introductory Statistics 

Lecture notes and homework
www.csun.edu/~dorsogna
and then click under Math 140

## Data from Tables

## Variables - columns

Characteristics of each case
Allows us to see the variability
Cases - rows Subjects and objects of statistical investigation

| Row | Job Title | Pay | Seniority | Round | Age |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | EngClerk | H | 1.5 | 6 | 25 |
| 3 | EngTech | H | 12.4 | 6 | 38 |
| 4 | Chemist | S | 36.8 | 1 | 69 |
| $\ldots$ |  |  |  |  |  |
| $\ldots$ |  |  |  |  |  |

Cases $=$ individual Westvaco employees Variables = Job title, pay, layoff round

## Data for hourly workers

| Row | Job Title | Age |
| :--- | :--- | :--- |
| 1 | Eng Clerk | 25 |
| 2 | Eng Tech II | 38 |
| 3 | Eng Tech II | 56 |
| 4 | Secretary | 48 |
| 5 | Eng Tech II | 53 |
| 6 | Eng Tech II | 55 |
| 7 | Eng Tech II | 59 |
| 8 | Parts Crib Attendant | 22 |
| 9 | Eng Tech II | 55 |
| 10 | Eng Tech II | 64 |
| 11 | Technical Secretary | 55 |
| 12 | Eng Tech II | 55 |
| 13 | Eng Tech II | 33 |
| 14 | Eng Tech II | 35 |

## Comparing dot plots


1.3) At the end of round 6 - laid off (blue), retained (red)

## Let's use other information

## Round by Round




Keep on going

## Salaried workers

## Summary Tables

## Laid off?

|  Yes No Total \% Yes <br>      <br> Under     <br> 50     | Yes |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- |
|  | No |  |  |  |  |
|  |  |  |  |  |  |

## Summary Tables

## Laid off?

|  |  | Yes | No | Total | \% Yes |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Under <br> $50 ?$ | Yes | 6 | 10 |  |  |
|  | No | 12 | 8 |  |  |
|  |  |  |  |  |  |

## Summary Tables

Laid off?

|  |  | Yes | No | Total |
| :--- | :--- | :--- | :--- | :--- |
| Under Yes <br> $50 ?$ | Yes | 6 | 10 | 16 |
|  | No | 12 | 8 | 20 |
|  |  |  |  |  |
| Total | 18 | 18 | 36 |  |

## Summary Tables

## Laid off?

| Under 40 ? |  | Yes | No | Total | \% Yes |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Yes | 4 | 5 | 9 | 44\% |
|  | No | 14 | 13 | 27 | 52\% |
|  | Total | 18 | 18 | 36 | 50\% |

1.What proportion of workers of age 50 or older were laid off? Were not laid off?
2. Same question with under 50
3. What proportion of laid off workers were age 50 or older? Were age 50 or lower?
4. Same question with retained workers
5. What proportions should be compared ?
6. Repeat for 1-4 for age 40 as a cutoff.

What table is best to argue with in a court of law?

## Overall:

# Exploratory work tells us that MAYBE <br> Older workers were laid off more likely than older ones. 

Are the patterns consistent with no discrimination occurring?

Does the company have some explaining to do at least?

## Summary Statistic

## Let's use some 'condensed' quantity from this data



## Summary Statistic

## Average age of those who lost job at round 2

$$
\text { Average }=\frac{(55+55+64)}{3}=58 \text { years }
$$

|  |  |  |  |  | 0 | 0 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 20 | 25 | 30 | 35 | 40 | 45 | 50 | 55 | 60 | 65 |

Hourly workers laid off at round 2 (blue)

## Summary Statistic

## Average age of all workers at round 2?



## Summary Statistic

## Average age of all workers at round 2?

46.4


## Thoughts?

The average age of all workers is 46.4 The average age of laid off workers is 58 The average age of retained workers is 41.4

What does this really mean?

## Can it be attributed to chance? <br> After all we have only 10 people!

What if I had changed the 64 year old with the 25 year old?

Would there have been discrimination?

## Laid off are 55, 55, 25

The average age of all workers is 46.4 The average age of laid off workers is 45 The average age of retained workers is 47

What does this really mean?

## Can it be attributed to chance? <br> After all we have only 10 people!

What if I had changed the 64 year old with the 25 year old?

Would there have been discrimination?

## For your entertainment

Calculate average ages (retained and laid off) by exchanging the 64 year old person with the 25 year old person

## For your entertainment

Calculate average ages (retained and laid off) by exchanging the 64 year old person with the 25 year old person

## But there are many other possibilities!

Why did we choose the 25 year old?
If it were by chance, any exchange should be valid!

## Hk

- E9 problems b/c
- E15
- E16
- E20
- E23 problems a/c/d
- Read chapter 1

