Math 140 Introductory Statistics

Next test on March 27th

Health care in America

About 30% of young American adults ages 19 to 29 don't have health insurance.

Suppose you take a random sample of ten American adults in this age group.

What is the probability that at least one of them doesn't have health insurance?

Take ten people, probability at least ONE does not have h.I?

P(at least one DOES NOT have h.i) + P(all have it) = 1

This means, by moving over P(all have it) to the other side

P(at least one DOES NOT have health insurance) =

1 - P(all have it)

P(at least one DOES NOT have health insurance) =

1 - P(all have it) =

1 - P(1st has it AND 2nd has it AND .. 10th has it)

P(at least one DOES NOT have health insurance) =

1 - P(all have it) =

1 - P(1st has it AND 2nd has it AND .. 10th has it) =

1 - P(1st has it) * P(2nd has it)... *P(10th has it)

Since they are independent

P(at least one DOES NOT have health insurance) =

1 - P(all have it) =

1 - P(1st has it AND 2nd has it AND .. 10th has it) =

1 - P(1st has it) * P(2nd has it)... *P(10th has it) =

1 - 0.7 * 0.7 * 0.7 ... *0.7

ten times =

1 - (0.7) 10

= 0.972

2 of her kids died of sudden infant death syndrome Assume these are independent events and calculate

P(baby 1 died AND baby 2 dies)

Assuming P(baby dies) = 1/8500

If the events were independent

P(baby 1 died AND baby 2 dies) = P(baby 1 died) * P(baby 2 died | baby 1 died) = P(baby 1 died) * P(baby 2 died) = $\frac{1}{8500} * \frac{1}{8500}$

1 in 70 million

In the UK there are only about 200,000 second births per year

She was sentenced to life in prison

The Royal Statistical Society of the UK argued that two babies dying in the same family <u>ARE NOT</u> independent

and concluded that the previous analysis does not apply.

P(baby 1 died and baby 2 dies) = P(baby 1 died) * P(baby2 died | baby 1 died) = 1/8500 * 1/100

This translates to one or two per year for the UK data

Sally Clark was released from prison

She died after 4 years.

Her family says she never recovered from the miscarriage of justice.

6.1 Probability distributions Probability distribution = Possible outcomes of a chance process

The probability distribution allows us to find probabilities for any outcome

We have three ways of specifying a population:

List of all (individual) units
 Frequency Table
 Relative Frequency or Proportion Table

Mean? SD?

List of units

Number	Туре	Value x	x - µ
1	Penny	1¢	-3
2	Penny	1¢	-3
3	Penny	1¢	-3
4	Penny	1¢	-3
5	Penny	1¢	-3
6	Nickel	5¢	1
7	Nickel	<mark>5</mark> ¢	1
8	Nickel	5¢	1
9	Dime	10 ¢	6
10	Dime	10 ¢	6
	Total = 10 coins	Sum = 40 cents	

$$\mu = \text{population mean} = \frac{\sum x}{n}$$
$$\mu = \frac{1+1+1+1+1+5+5+5+10+10}{10} = 4$$

List of units

Number	Туре	Value x	x - µ
1	Penny	1¢	-3
2	Penny	1¢	-3
3	Penny	1¢	-3
4	Penny	1¢	-3
5	Penny	1¢	-3
6	Nickel	5¢	1
7	Nickel	<mark>5</mark> ¢	1
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9	Dime	10 ¢	6
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	Total = 10 coins	Sum = 40 cents	

$$\mu = ext{population mean} = rac{\sum x}{n}$$
 $\mu = rac{1+1+1+1+1+5+5+5+10+10}{10} = 4$

$$\sigma_n = \text{SD} = \sqrt{\frac{\sum (x - \mu)^2}{n}}$$
$$\sigma_n = \sqrt{\frac{9 + 9 + 9 + 9 + 9 + 1 + 1 + 1 + 36 + 36}{10}} = \sigma_n = \sqrt{\frac{120}{10}} = \sqrt{12} \approx 3.4641$$

Make list from data

				Secor	nd Die		
		1	2	3	4	5	6
First Die	1	1, 1	1, 2	1,3	1,4	1, 5	1,6
	2	2,1	2,2	2,3	2,4	2,5	2,6
	3	3,1	3,2	3,3	3,4	3,5	3,6
FIRST DIE	4	4, 1	4, 2	4, 3	4,4	4,5	4,6
	5	5,1	5,2	5,3	5,4	5,5	5,6
	6	6,1	6, 2	6,3	1, 4 2, 4 3, 4 4, 4 5, 4 6, 4	6,5	6,6

Construct the probability distribution for1) The sum of the two dice2) The larger number on the two dice

List for the Sum of the data

				Secor	nd Die		
		1			4		
First Die	1	1, 1	1, 2	1, 3	1,4	1, 5	1,6
	2	2,1	2,2	2,3	2,4	2,5	2,6
	3	3,1	3,2	3,3	3,4	3,5	3,6
	4	4, 1	4, 2	4, 3	4,4	4,5	4,6
	5	1, 1 2, 1 3, 1 4, 1 5, 1	5,2	5,3	5,4	5,5	5,6
	6	6,1	6, 2	6, 3	6,4	6,5	6,6

Possibilities Sum = 2 Sum = 3 Probability (1,1) 1/36 (1,2) or (2,1) 2/36

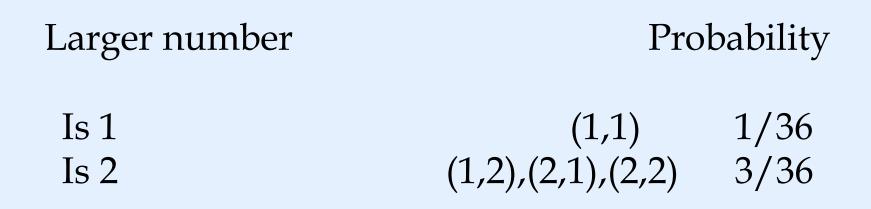
You do the rest

List for the Sum of the data

If we add them we should always get 1, since this represents all possibilities

1/36 2/36
2/36
3/36
4/36
5/36
6/36
5/36
4/36
3/36
2/36
1/36
1

Do also for larger number



You do the rest

Do also for larger number

Larger Number, x	Probability, p
1	1/36
2	3/36
3	5/36
4	7/36
5	9/36
6	11/36
Total	1

We can calculate

Probability that the sum of number is 3 = 2/36Probability that the larger number is 3 = 5/36Etc etc

What we get after tossing the dice is a random variable depends on chance - may change from trial to trial

We call it X. For example, if we care for the SUM of numbers

> P(X=3) = 2/36 = 1/18P(X=7) = 6/36 = 1/6

Lung Cancer Cases	Proportion
Smoking responsible	0.87
Smoking not responsible	0.13

Suppose two lung cancer patients are randomly selected What is the probability distribution of X- the number of patients with lung cancer caused by smoking

Smoking and Lung cancer For 2 sick people, either smoking was cause of disease or not

4 possibilities

Not caused by smoking Not caused by smoking Caused by smoking Caused by smoking Not caused by smoking Caused by smoking Not caused by smoking Caused by smoking

Recall

P(A and B) = P(A) P(B | A) =P(B) P(A | B)

Are the lung cancer events on separate patients independent?

Recall

$$P(A \text{ and } B) = P(A) P(B | A) =$$
$$P(B) P(A | B)$$

Are the lung cancer events on separate patients independent? Yes! P(A and B) = P(A) P(B)

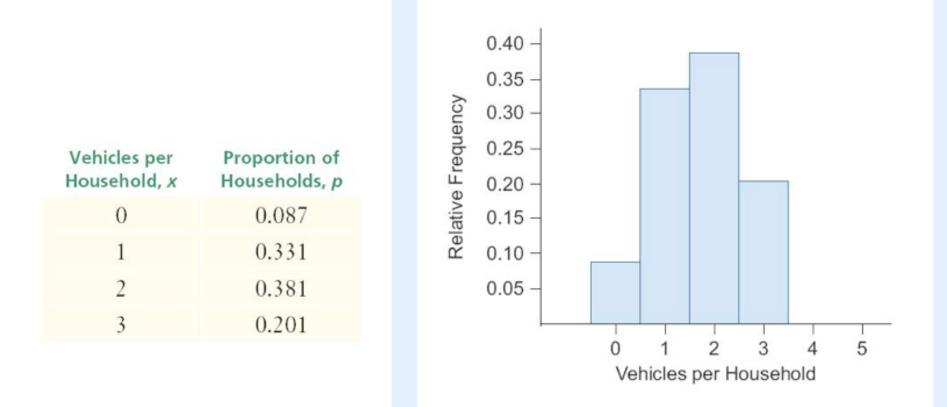
Not caused by smoking Not caused by smoking P=0.13 P= 0.13 Independent events

P(both patients had cancer not caused by smoking) = $0.13*0.13 = 0.0169 \sim \text{less than } 2\%$

Number Caused by Smoking, <i>x</i>	Probability, p
0	
1	
2	

You fill it out

Number Caused by Smoking, <i>x</i>	Probability, p
0	0.0169
1	0.1131 + 0.1131 = 0.2262
2	0.7569



What is the probability that a home will have two or more cars? (Assume no one has 4)

Vehicles per Household, <i>x</i>	Proportion of Households, p
0	0.087
1	0.331
2	0.381
3	0.201

What is the probability that a home will have two or more cars?

P(X=2) = 0.381 + 0.201 = 0.582

How about calculating the probability That two randomly selected homes have NO cars?

P(two randomly selected homes have NO cars) =

P(1st 0 cars) * P(2nd 0 cars | 1st 0 cars)=

Independent events =

P(1st 0 cars) * P(2nd 0 cars) = 0.087 * 0.087 = 0.008

Less than 1%

Vehicles per Household, <i>x</i>	Proportion of Households, p
0	0.087
1	0.331
2	0.381
3	0.201

P(exactly one car in a duplex) = Take two homes, one has a car, the other has zero cars

= P(1 car in 1st house AND 0 cars in 2nd house OR 0 cars in first house AND 1 car in 2nd house)

A = 1 car in 1st house AND 0 cars in 2nd house B = 0 cars in 1st house AND 1 car in 2nd house

A = 1 car in 1st house AND 0 cars in 2nd house B = 0 cars in 1st house AND 1 car in 2nd house

These are disjoined!

Recall P(A or B) = P(A) + P(B) - P(A and B)Here P(A and B) = 0They are disjoined

P(1 car in 1st house AND 0 cars in 2nd house OR 0 cars in first house AND 1 car in 2nd house)

= P (1 car in 1st house AND 0 cars in 2nd house) + P (0 cars in first house AND 1 car in 2nd house) P(1 car in 1st house AND 0 cars in 2nd house OR 0 cars in first house AND 1 car in 2nd house)

= P (1 car in 1st house AND 0 cars in 2nd house) + P (0 cars in first house AND 1 car in 2nd house) (disjoined)

> P(1 car) * P(0 cars) + P(0 cars) * P(1 car) (independent)

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0.331 * 0.087 + 0.087 * 0.331 = 0.058

Make the full chart for duplexes

Total Number of Vehicles, x	Probability, p
0	
1	0.058
2	
3	
4	
5	
6	

Make the full chart for duplexes

Total Number of Vehicles, x	Probability, p
0	0.008
1	0.058
2	0.176
3	0.287
4	0.278
5	0.153
6	0.040

Practice and hk

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P1, P2, P3, E1, E2, E3, E5, E4, E6, E7

Try E2 first

6 computers, 3 are broken, you get to sample only 2

Find P(X=0), P(X=1), P(X=2) X= number of sampled computers that are broken