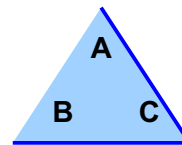


SYMMETRIES: A **symmetry** is a rigid transformation of a figure **onto itself**.

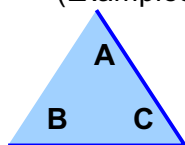
For example, an equilateral triangle ABC may be:

- rotated 120° (so that A→B, B→C and C→A) $[[(A,B,C)]]$
 - rotated 240° (A→C, B→A and C→B). $[[(A,C,B)]]$
- (Examples of *point symmetry* or *rotational symmetry*)

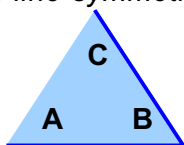


The triangle may also be:

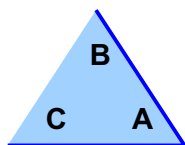
- reflected through the altitude from A ... A stays put, B→C, C→B ... (A) (BC)
 - reflected through the altitude from B $[[(B) (A,C)]]$
 - reflected through the altitude from C. $[[(C) (A,B)]]$
- (Examples of *line symmetry*)



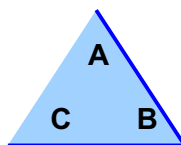
I
Rotate 360°
(identity)
(A)(B)(C)



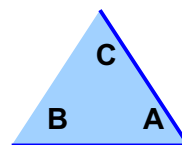
σ_1
Rotate 120°
(ABC)



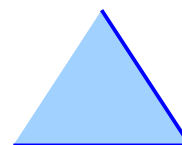
σ_2
Rotate 240°
(ACB)



ρ_1
Flip over
altitude A
(A) (BC)



ρ_2
Flip over
altitude B
(B)(AC)



ρ_3
Flip over
altitude C
() ()

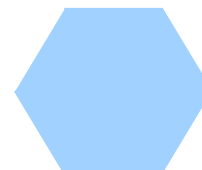
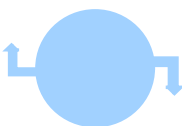
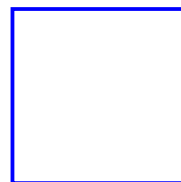
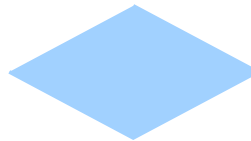
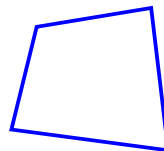
Together with the 360° rotational symmetry (which is tantamount to leaving the figure alone!), which every figure has, these symmetries form "the symmetry group of an equilateral triangle".

- The letter **A** has *line* symmetry. Draw the line of reflection, or line of symmetry.
- The letter **B** also has *line* symmetry. Check out these: **C D E F Z**
- Do any of these letters have *rotational* symmetry?

A B C D E F G H I J K L M
N O P Q R S T U V W X Y Z

- Find all the symmetries of each of the following:

- isosceles triangle region
- scalene quadrilateral
- isosceles trapezoid region
- parallelogram region
- rhombus region
- square
- regular hexagon region
- circular region
- the figure at right ↗



- Add one square to this figure so that it will have one line & no rotational symmetry.
- Add one square to this figure so that it will have one rotational & no line symmetry.

