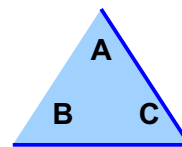


**SYMMETRIES:** A **symmetry** is a rigid transformation of a figure **onto itself**.

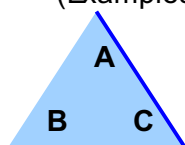
For example, an equilateral triangle ABC may be:

- rotated  $120^\circ$  (so that A→B, B→C and C→A)  $[[ (A,B,C) ]]$
  - rotated  $240^\circ$  (A→C, B→A and C→B).  $[[ (A,C,B) ]]$
- (Examples of *point symmetry* or *rotational symmetry*)



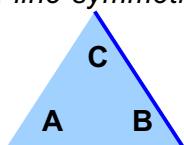
The triangle may also be:

- reflected through the altitude from A ... A stays put, B→C, C→B ... (A) (BC)
  - reflected through the altitude from B  $[[ (B) (A,C) ]]$
  - reflected through the altitude from C.  $[[ (C) (A,B) ]]$
- (Examples of *line symmetry*)



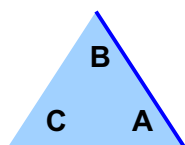
I

Rotate  $360^\circ$   
(identity)  
(A)(B)(C)



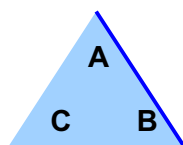
$\sigma_1$

Rotate  $120^\circ$   
(ABC)



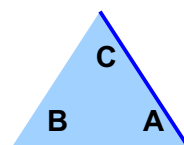
$\sigma_2$

Rotate  $240^\circ$   
(ACB)



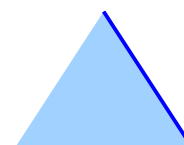
$\rho_1$

Flip over  
altitude A  
(A) (BC)



$\rho_2$

Flip over  
altitude B  
(B)(AC)



$\rho_3$

Flip over  
altitude C  
( ) ( )

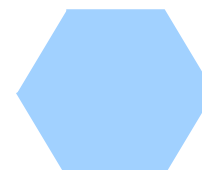
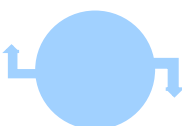
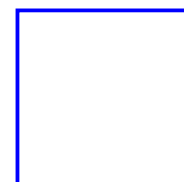
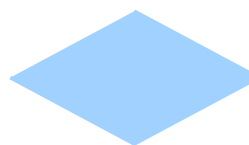
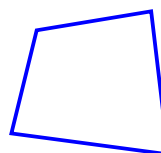
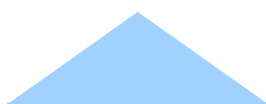
Together with the  $360^\circ$  rotational symmetry (which is tantamount to leaving the figure alone!), which every figure has, these symmetries form "the symmetry group of an equilateral triangle".

1. The letter **A** has *line* symmetry. Draw the line of reflection, or line of symmetry.
2. The letter **B** also has *line* symmetry. Check out these: **C D E F Z**
3. Do any of these letters have *rotational* symmetry?

A B C D E F G H I J K L M  
N O P Q R S T U V W X Y Z

4. Find all the symmetries of each of the following:

- a. isosceles triangle region
- b. scalene quadrilateral
- c. isosceles trapezoid region
- d. parallelogram region
- e. rhombus region
- f. square
- g. regular hexagon region
- h. circular region
- i. the figure at right ↗



5. Name a figure that has TRANSLATIONAL SYMMETRY!
6. Add one square to this figure so that it will have one line & no rotational symmetry.  
Add one square to this figure so that it will have one rotational & no line symmetry.

