

SYNTHETIC DIVISION HOW-TO

Here is a division process: $(2x^3 - x^2 + 2x - 3) \div (x - 1)$

Standard division:

$$\begin{array}{r}
 2x^2 + x + 3 \\
 x - 1 \overline{) 2x^3 - x^2 + 2x - 3} \\
 \underline{2x^3 - 2x^2} \\
 x^2 \\
 \underline{x^2 - x} \\
 3x - 3 \\
 \underline{3x - 3} \\
 0
 \end{array}$$

Bring down the first coefficient.
(Or Add: 2 plus nothing = 2)

Multiply this by c which is 1 here:
 $1 \cdot 2 = 2$

ADD: $-1 + 2 = 1$

Repeat: Multiply the 1 by c (c=1 here)
 $1 \cdot 1 = 1$

and ADD: $2 + 1 = 3$

Repeat: Multiply the 3 by c (c=1 here)
 $1 \cdot 3 = 3$

and ADD: $-3 + 3 = 0$

Synthetic division:

$$\begin{array}{r|rrrr}
 1 & 2 & -1 & 2 & -3 \\
 & 2 & 1 & 3 & 0
 \end{array}$$

Below we are step by step instructions.

$$\begin{array}{r|rrrr}
 1 & 2 & -1 & 2 & -3 \\
 & \downarrow & & & \\
 & 2 & & &
 \end{array}$$

$$\begin{array}{r|rrrr}
 1 & 2 & -1 & 2 & -3 \\
 & & 2 & & \\
 \hline
 & 2 & 1 & &
 \end{array}$$

$$\begin{array}{r|rrrr}
 1 & 2 & -1 & 2 & -3 \\
 & & 2 & & \\
 \hline
 & 2 & 1 & &
 \end{array}$$

$$\begin{array}{r|rrrr}
 1 & 2 & -1 & 2 & -3 \\
 & & 2 & & \\
 \hline
 & 2 & 1 & &
 \end{array}$$

$$\begin{array}{r|rrrr}
 1 & 2 & -1 & 2 & -3 \\
 & & 2 & 1 & \\
 \hline
 & 2 & 1 & 3 &
 \end{array}$$

$$\begin{array}{r|rrrr}
 1 & 2 & -1 & 2 & -3 \\
 & & 2 & 1 & \\
 \hline
 & 2 & 1 & 3 &
 \end{array}$$

$$\begin{array}{r|rrrr}
 1 & 2 & -1 & 2 & -3 \\
 & & 2 & 1 & \\
 \hline
 & 2 & 1 & 3 &
 \end{array}$$

...from which we read the answer:

Quotient is $2x^2 + 1x + 3$ Rem = 0

A side-by-side comparison can be seen at Purplemath.com

There are a number of synthetic divisions in problem #4a of the chapter 5 preview , also posted on the Notices page.