

95% confidence interval for the mean temperature for men.

$$\bar{x} \pm t^* \frac{s}{\sqrt{n}}$$

What is  $t^*$ ?

We need  $n=10$  and 95% confidence

$$t^* = 2.2622$$

$$\bar{x} = 97.88$$

$$s = .5553777$$

$$97.88 \pm (2.2622) \cdot \left( \frac{.5553777}{\sqrt{10}} \right) = \begin{cases} 97.482699 \\ 98.2773008 \end{cases}$$

95% confidence for females

$$\begin{cases} 98.143 \\ 98.897 \end{cases}$$

Identify the test (circle one):

1. Significance test for one proportion (1-PropZTest)
2. Significance test for the difference of two proportions (2-PropZTest)
3. Significance test for a mean (T-Test)
4. Significance test for the difference of two means (2-SampTTest)

Data: Significance level  $\alpha = .05$

Other: (depending on the test, circle and give the necessary values)

$$p_0 = \underline{\hspace{2cm}} \quad \hat{p} = \underline{\hspace{2cm}} \quad \bar{x} = \textcircled{1050}$$

$$\mu_0 = \textcircled{1015} \quad \hat{p}_1 = \underline{\hspace{2cm}} \quad \bar{x}_1 = \underline{\hspace{2cm}}$$

$$n = \textcircled{64} \quad \hat{p}_2 = \underline{\hspace{2cm}} \quad \bar{x}_2 = \underline{\hspace{2cm}}$$

$$n_1 = \underline{\hspace{2cm}} \quad x_1 = \underline{\hspace{2cm}} \quad s = \textcircled{150}$$

$$n_2 = \underline{\hspace{2cm}} \quad x_2 = \underline{\hspace{2cm}} \quad s_1 = \underline{\hspace{2cm}}$$

$$x = \underline{\hspace{2cm}} \quad s_2 = \underline{\hspace{2cm}}$$

Check the conditions:

1. The sample was obtained at random.
2. The sample size  $n = 64$  is big enough (greater than 40)
3.  $10n = 640 <$  total number of students at this particular university

State the hypotheses:

$$H_0: M = M_0$$

$$H_a: M > M_0$$

where (circle and describe in words the appropriate symbol(s):  $p, p_1, p_2, \mu, \mu_1, \mu_2$ )

$M$  = true mean number of hours students study every week.

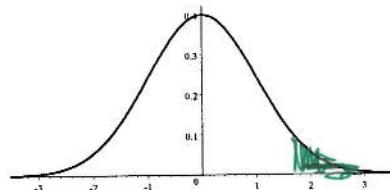
Compute the test statistic,  $p$ -value, and label and complete the sketch:

Test statistic: 
$$t = \frac{\bar{x} - M_0}{S/\sqrt{n}} = \underline{1.86666}$$

formula

$$P\text{-value} = \underline{.0333016}$$

Is the sample significant? Yes  
Yes/No



Conclusions:

(Circle one) We reject/don't reject the null hypothesis.

Explain in context.

Because the  $P\text{-Value} = .0333016 < .05$ , we rejected the null hypothesis in favor of the alternate. If the mean number of hours of study time per week was 1015 minutes, then it would be unlikely (probability 3.33%) to get a sample of 64 random students with a larger mean than 1050. So we have evidence to assert that indeed the average study time per week is larger than 1015.

Identify the test (circle one):

1. Significance test for one proportion (1-PropZTest)
2. Significance test for the difference of two proportions (2-PropZTest)
3. Significance test for a mean (T-Test)
4. Significance test for the difference of two means (2-SampTTest)

Data: Significance level  $\alpha = .05$

Other: (depending on the test, circle and give the necessary values)

$$p_0 = \underline{\hspace{2cm}} \quad \hat{p} = \underline{\hspace{2cm}} \quad \bar{x} = \underline{\hspace{2cm}} 92.9286$$

$$\mu_0 = \underline{\hspace{2cm}} 93 \quad \hat{p}_1 = \underline{\hspace{2cm}} \quad \bar{x}_1 = \underline{\hspace{2cm}}$$

$$n = \underline{\hspace{2cm}} 15 \quad \hat{p}_2 = \underline{\hspace{2cm}} \quad \bar{x}_2 = \underline{\hspace{2cm}}$$

$$n_1 = \underline{\hspace{2cm}} \quad x_1 = \underline{\hspace{2cm}} \quad s = \underline{\hspace{2cm}} 111.8587$$

$$n_2 = \underline{\hspace{2cm}} \quad x_2 = \underline{\hspace{2cm}} \quad s_1 = \underline{\hspace{2cm}}$$

$$x = \underline{\hspace{2cm}} \quad s_2 = \underline{\hspace{2cm}}$$

Check the conditions:

1. Measurements were obtained at random times and places.
2. The data looks normally distributed except for an outlier. We'll do the test with and without the outlier.
- 3.

$10n = 150 <$  total number of measurements from earth to sun (infinitely many)

State the hypotheses:

$$H_0: M = M_0$$

$$H_a: M \neq M_0$$

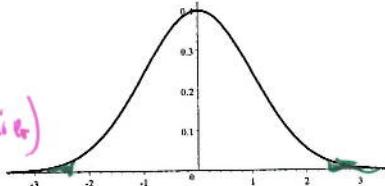
where (circle and describe in words the appropriate symbol(s):  $p, p_1, p_2, \mu, \mu_1, \mu_2$ )

$M = \text{the average distance from the earth to the sun.}$

Compute the test statistic,  $p$ -value, and label and complete the sketch:

Test statistic:  $t = \frac{\bar{x} - M_0}{s/\sqrt{n}} = \frac{-2.469836}{-6.2792}$

$P\text{-value} = .0269928$  (.0000203) (without the outlier)



Is the sample significant? Yes  
Yes/No

Conclusions:

(Circle one) We  reject/don't reject the null hypothesis.

Explain in context.

Because  $P\text{-Value} = .02699 < .05$  we reject the null hypothesis in favor of the alternate.

If the average distance from the earth to the sun was 93 million miles, then it would be unlikely (probability 2.69%) to get a sample of

15 measurements as extreme or more than the one we analyzed.

Furthermore, if we remove the outlier<sup>1</sup> of 93.28, then the probability becomes .00283%. So we have ample evidence to assert that the A.U. is not equal to 93 million miles.

Identify the test (circle one):

1. Significance test for one proportion (1-PropZTest)
2. Significance test for the difference of two proportions (2-PropZTest)
3. Significance test for a mean (T-Test)
4. Significance test for the difference of two means (2-SampTTest)

Data: Significance level  $\alpha = .05$

Other: (depending on the test, circle and give the necessary values)

$$p_0 = \underline{\hspace{2cm}} \quad \hat{p} = \underline{\hspace{2cm}} \quad \bar{x} = \underline{\hspace{2cm}} 43.3$$

$$\mu_0 = \underline{\hspace{2cm}} 42 \quad \hat{p}_1 = \underline{\hspace{2cm}} \quad \bar{x}_1 = \underline{\hspace{2cm}}$$

$$n = \underline{\hspace{2cm}} 40 \quad \hat{p}_2 = \underline{\hspace{2cm}} \quad \bar{x}_2 = \underline{\hspace{2cm}}$$

$$n_1 = \underline{\hspace{2cm}} \quad x_1 = \underline{\hspace{2cm}} \quad s = \underline{\hspace{2cm}} 5.06$$

$$n_2 = \underline{\hspace{2cm}} \quad x_2 = \underline{\hspace{2cm}} \quad s_1 = \underline{\hspace{2cm}}$$

$$x = \underline{\hspace{2cm}} \quad s_2 = \underline{\hspace{2cm}}$$

Check the conditions:

1. The sample is not a random sample, we'll proceed but be very wary of our results.

2. The sample size  $n=40$  is big enough

3.  $10n = 100 < \text{total number of owners of 2007 Honda Civic Hybrid}$

State the hypotheses:

$$H_0: \mu = \mu_0$$

$$H_a: \mu > \mu_0$$

where (circle and describe in words the appropriate symbol(s):  $p, p_1, p_2, \mu, \mu_1, \mu_2$ )

$\mu$  = true average mpg for 2007 Honda Civic Hybrid Cars that their owners would report.

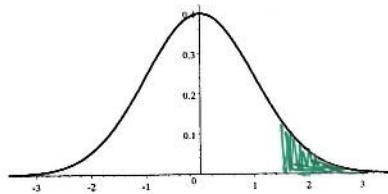
Compute the test statistic, p-value, and label and complete the sketch:

Test statistic: 
$$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}} = \underline{1.6249}$$

formula

P-value = .0561

Is the sample significant? No  
Yes/No



Conclusions:

(Circle one) We reject/don't reject the null hypothesis.

Explain in context.

Because P-Value = .0561 > .05 we don't reject the null hypothesis. If the average mpg the owners would report is 42mpg then it is likely to get a sample of 40 owners with  $\bar{x} = 43.3$  and  $s = 5.06$  or more extreme (Probability of this is 5.61%)

So we have no evidence to assert that the actual mpg the owners would report is larger than 42.

95% confidence interval for

"bottom" - "mid depth"

$$(\bar{x}_1 - \bar{x}_2) \pm t^* \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

$$n_1 = 10$$

$$\bar{x}_1 = ? 6.04$$

$$s_1 = ? 1.579$$

$$t^* = ?$$

$$n_2 = 10$$

$$\bar{x}_2 = ? 5.05$$

$$s_2 = ? 1.103$$

$$(-.3009, 2.2809)$$

$$[\text{~~~~~} \overbrace{\text{~~~~~}}^{M_1 - M_2} \text{~~~~~}]$$



$M_1$  = true average aldrin at the bottom

$M_2$  = true average aldrin at mid-depth