

M 225 Test 2 B

Name_____

(1 point)

SHOW YOUR WORK FOR FULL CREDIT!

Problem	Max. Points	Your Points
1-10	10	
11	10	
12	6	
13	6	
14	5	
15	12	
16	4	
17	6	
18	6	
19	3	
20	3	
21	3	
22	6	
23	9	
Total	100	

Multiple choice questions (1 point each)

1. A correct interpretation of the statement “The probability that a child delivered in a certain hospital is a girl is 0.50” would be which one of the following?
- a. In the next two births at that hospital, there will be exactly one boy and one girl.
 - b. To make sure that a couple has two girls and two boys at that hospital, they only need to have four children.
 - c. A computer simulation of 100 births for that hospital would produce exactly 50 girls and 50 boys.
 - ☒ d. Over a long period of time, there will be equal proportions of boys and girls born at that hospital.
2. From a computer simulation of rolling a fair die ten times, the following data were collected on the showing face: 5 1 5 1 6 2 5 3 5 1
What is a correct conclusion to make about the next ten rolls of the same die?

- ☒ a. Each face has exactly the same probability of being rolled.
- b. The probability of rolling a 5 is greater than the probability of rolling anything else.
- c. We will see exactly three faces showing a 1 since it is what we saw in the first experiment.
- d. The probability of rolling a 4 is 0, and therefore we will not roll it in the next ten rolls.

3. If a couple has three children, let X represent the number of girls. What is the probability that the couple does NOT have girls for all three children?

X	0	1	2	3
$P(X)$	1/8	3/8	3/8	1/8

- ☒ c. 1/8
- d. 3/8
- e. $1/8 + 1/8 = 2/8$
- f. $1/8 + 3/8 = 4/8$

4. Three students work independently on a homework problem. The probability that the first student solves the problem is 0.95. The probability that the second student solves the problem is 0.85. The probability that the third student solves the problem is 0.80.
What is the probability that all are able to solve the problem?

- ☒ a. $(0.95)(0.85)(0.80)$
- b. $0.95 + 0.85 + 0.80$
- c. $1 - (0.95)(0.85)(0.80)$
- d. 0.80

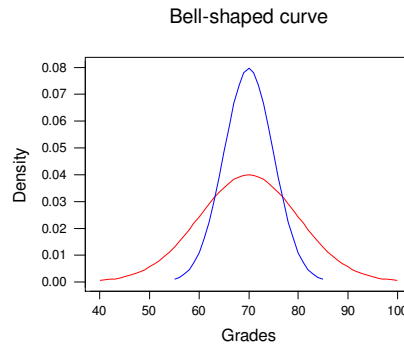
5. A telemarketing firm in Los Angeles uses a device that dials residential telephone numbers in the city at random. Of the first 100 numbers dialed, 48% are unlisted. This is not surprising because 52% of all Los Angeles residential phones are unlisted.
- a. the 48% is a parameter, and the 52% is a statistic
 - ☒ b. the 48% is a statistic, and the 52% is a parameter
 - c. both the 52% and the 48% are parameters
 - d. both the 52% and the 48% are statistics

6. A manufacturing company takes a sample of $n = 100$ bolts from their production line. X is the number of bolts that are found defective in the sample. It is known that the probability of a bolt being defective is 0.003.
Does X have a binomial distribution?
- ☒ a. Yes.
 - b. No, because there is not a fixed number of observations.
 - c. No, because the observations are not all independent.
 - d. No, because there are more than two possible outcomes for each observation.
 - e. No, because the probability of success for each observation is not the same.
7. A survey-taker asks the age of each person in a random sample of 20 people. X is the age for the individuals.
Does X have a binomial distribution?
- a. Yes.
 - ☒ b. No, because there are more than two possible outcomes for each observation.
 - c. No, because there is not a fixed number of observations.
 - d. No, because the observations are not all independent.
8. A fair die is rolled and the number of dots on the top face is noted. X is the number of times we have to roll in order to have the face of the die show a 2.
Does X have a binomial distribution?
- a. Yes.
 - ☒ b. No, because there is not a fixed number of observations.
 - c. No, because the observations are not all independent.
 - d. No, because there are more than two possible outcomes for each observation.
 - e. No, because the probability of success for each observation is not the same.
9. Suppose that for a randomly selected high school student who has taken a college entrance exam, the probability of scoring above a 650 is 0.30. A random sample of $n = 9$ students was selected. What are the mean μ and standard deviation σ of the number of students in the sample who have scores above 650?
- a. $\mu = (9)(0.3) = 2.7$, $\sigma = 0.30$
 - b. $\mu = 3$, $\sigma = (9)(0.3)$
 - c. $\mu = (9)(0.3) = 2.7$, $\sigma = \sqrt{(9)(0.7)(0.3)}$
 - ☒ d. $\mu = (9)(0.3) = 2.7$, $\sigma = (9)(0.7)(0.3)$
10. Which one of these pairs of events is a pair of disjoint (mutually exclusive) events?
- a. has been in a foreign country; has never ridden on a train
 - b. owns a piano; owns a violin
 - ☒ c. has never been married; has divorced
 - d. has brown hair; has blue eyes

11. TRUE or FALSE (1 point each)

T **F** If two events are mutually exclusive (disjoint), they don't have outcomes in common.

T **F** These two normal curves have the same means, but different standard deviations.



T **F** The probability that a person has a certain disease is 0.04. Then the probability that two randomly selected persons do NOT have the disease is $1 - 0.04^2$.

T **F** The Standard Normal Distribution has mean 1 and standard deviation 0.

T **F** For a normal distribution the z-score is 0 if the corresponding x-value is equal to zero.

T **F** In a binomial experiment p represents the probability of failure.

T **F** The area under any normal curve is 1.

T **F** When the z-score of a data value is 1.8, that means that the data value is 1.8 standard deviations above the mean.

T **F** An appropriate notation for the fraction of a sample of American adults who received at least one speeding ticket last year is \hat{p} .

T **F** An appropriate notation for the mean distance traveled in a year by all of the truck drivers is \bar{x} .

12. (6 points) You roll two fair six-sided dice. Find the probability for each event:

a. Event A: the sum of the two numbers is 9

Sum of 9: 3,6; 6,3; 4,5; 5,4. So the probability is 4/36

b. Event B: the sum is 8 or getting doubles

Sum of 8: 2,6; 6,2; 3,5; 5,3; 4,4. Doubles: 1,1; 2,2; 3,3; 4,4; 5,5; 6,6

Since the outcome 4,4 was counted twice, the probability is $5/36 + 6/36 - 1/36 = 10/36$

13. (6 points) Identify the sample space.

- a. Gender of two children born to a couple.

$$S=\{GG, GB, BG, BB\}$$

- b. You have three coins, a quarter (Q), a dime (D), and a nickel (N) in your pocket. You randomly one coin, and then without replacing it you select another coin.

$$S=\{QD, QN, DQ, DN, NQ, ND\}$$

14. (5 points) Decide whether the random variable X is discrete or continuous:

- a. X represents the number of highway fatalities in one week in LA county. **Discrete**
- b. X represents the length of time it takes to get to work **Continuous**
- c. X represents the volume of blood drawn for a blood test. **Continuous**
- d. X represents the number of books sold per semester at a university book store. **Discrete**
- e. X represents the weight of a chemical compound. **Continuous**

15. (12 points) During one season, the Los Angeles Dodgers had won 41 and lost 37 games. The breakdown by whether the game was played during the day or at night is shown in the following table. If you select a game randomly

		Won the Game?		
		Yes	No	Total
Time of Game	Day	11	10	21
	Night	30	27	57
	Total	41	37	78

- a. what is the probability that the team had not won that game?

$$37/78$$

- b. what is the probability that the team had won that game and played at during the day?

$$11/78$$

- c. what is the probability that the team had won that game given that they played at night?

$$30/57$$

- d. what is the probability that the team played during the night given that they lost?

$$27/37$$

- e. what is the probability that the team had not won that game given that they played during the day?

10/21

- f. Are the events “Played during the day” and “Did not win the game” independent? Explain using the given probabilities.

Two events A and B are independent if $P(A \text{ and } B) = P(A) \cdot P(B)$

In this case, we need to check whether $P(\text{Played during the day and Did not win the game})$ equals to $P(\text{Played during the day}) \cdot P(\text{Did not win the game})$

$P(\text{Played during the day and Did not win the game}) = 10/78 = 0.1282$

$P(\text{Played during the day}) = 21/78$

$P(\text{Did not win the game}) = 37/78$

$(21/78)(37/78) = 0.1277$

Since $P(\text{Played during the day and Did not win the game})$ doesn't equal to $P(\text{Played during the day}) \cdot P(\text{Did not win the game})$, these two events are not independent

However, since they are close, I gave full credit if you concluded (showing your work) that they are independent.

- 16. (4 points) The probability that a statistics student reads the textbook is 0.66. The probability a student does the homework is 0.76. The probability that a student reads the book and does the homework is 0.51.**

If a student is randomly selected, what is the probability that the student reads the book or does the homework?

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B) = 0.66 + 0.76 - 0.51 = 0.91$$

- 17. (6 points) A printing company's bookbinding machine has a probability of 0.018 of producing a defective book. This machine is used to bind three books.**

- a. Find the probability that all three books are defective.

$$(0.018)(0.018)(0.018) = 5.832 \times 10^{-6}$$

- b. Find the probability that none of the three books are defective.

$$(1 - 0.018)(1 - 0.018)(1 - 0.018) = 0.9470$$

18. (6 points) A sociologist surveyed the households in a small town. The random variable represents the number of dependent children per household.

X	0	1	2	3	4
P(X)	0.07	0.20	0.36		0.13

- a. Find the missing probability value.
Since the probabilities must add up to 1, the missing value must be 0.24.
- b. What is the probability that a randomly selected household has 3 or more dependent children?
3 or 4 children: $0.24 + 0.13 = 0.37$
- c. Find the mean number of dependent children per household.

$$\text{Mean: } 0(0.07) + 1(0.20) + 2(0.36) + 3(0.24) + 4(0.13) = 2.16$$

19. (3 points) From a pool of 10 candidates, the offices of president, vice-president, secretary, and treasurer will be filled. In how many ways can the offices be filled?

$$\text{Order DOES matter here, so it's } {}_{10}P_4 = 5040$$

20. (3 points) Find the number of ways a four-member committee can be chosen from 10 candidates.

$$\text{Order does NOT matter here, so it's } {}_{10}C_4 = 210$$

21. (3 points) In how many distinguishable ways can the letters in the word STATISTICS?

$$\begin{aligned} &10 \text{ letters in the word, S repeats 3 times, T repeats 3 times, and I repeats twice:} \\ &(10!)/(3!)(3!)(2!) = 50400 \end{aligned}$$

22. (6 points) 76% of men consider themselves basketball fans. You randomly select 3 men and ask each if he considers himself a basketball fan.

- a. Verify that the experiment is a binomial experiment.

n is fixed ($n = 3$), the trials are independent, the probability that a man is a basketball fan is constant, and there are only two possible outcomes (either a fan or not). So it's a binomial experiment.

- b. What is the probability that out of the three men exactly two men consider themselves a basketball fan?

$$P(X = 2) = 0.4159$$

- c. Find the mean and the standard deviation of the distribution.

$$\text{Mean} = np = 3(0.76) = 2.28$$

$$\text{Standard deviation} = \sqrt{np(1-p)} = \sqrt{3(0.76)(1-0.76)} = 0.740$$

- 23. (13 points) The mean total cholesterol levels for men ages 35-44 are normally distributed with mean cholesterol level 205 milligrams per deciliter with a standard deviation of 39.2 milligrams per deciliter. (Don't forget to draw the distribution and shade the area.)**

- a. What is the probability that a randomly selected man in this age group has total cholesterol level below 120 milligrams per deciliter?

$$z = \frac{x - \mu}{\sigma} = \frac{120 - 205}{39.2} = -2.17 \quad \text{probability: 0.015}$$

The probability that a randomly selected man in this age group has total cholesterol level below 120 milligrams per deciliter is about 1.5%.

- b. What is the cholesterol level of men ages 35-44 who are in the top 5% ?

For the top 5%, the z-score is 1.645 (invNorm(0.95))

$$x = z \cdot \sigma + \mu = 1.645(39.2) + 205 = 269.48$$

The cholesterol level of men ages 35-44 in the top 5% is 269.48 milligrams per deciliter or more.