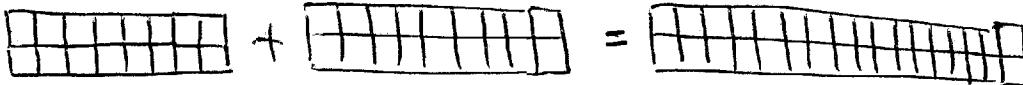
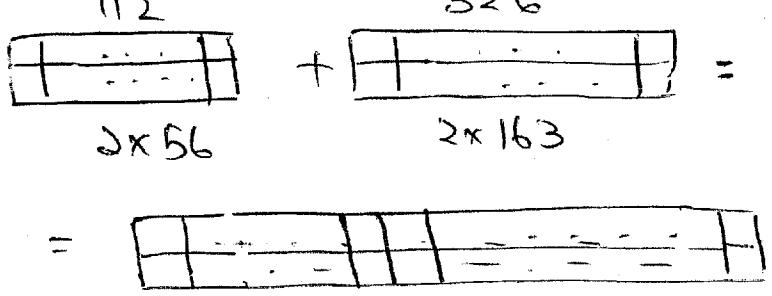


$$1) \quad 16 + 18 = 34$$

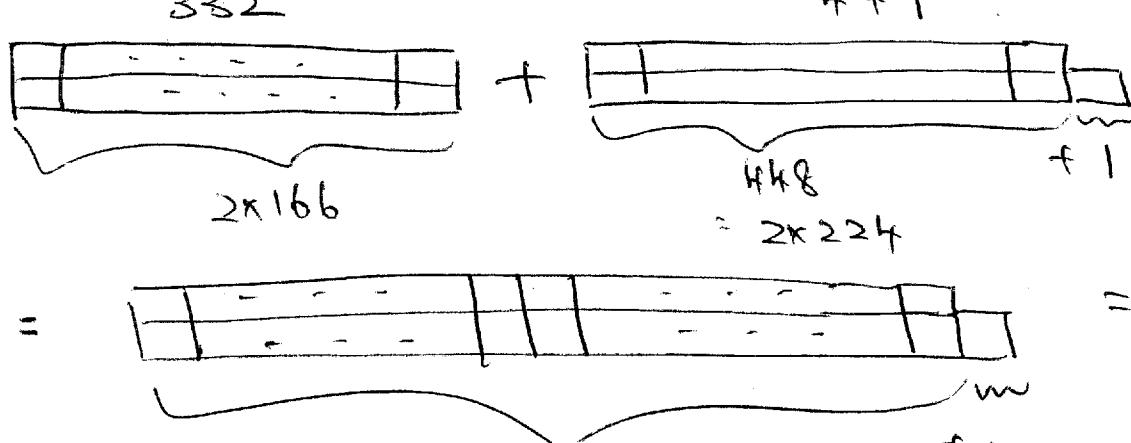
16      + 18      = 34  
  
 2x8      2x9      2x17

$$112 + 326 = 438$$

112      + 326      = 438  
  
 2x56      2x163      2x219

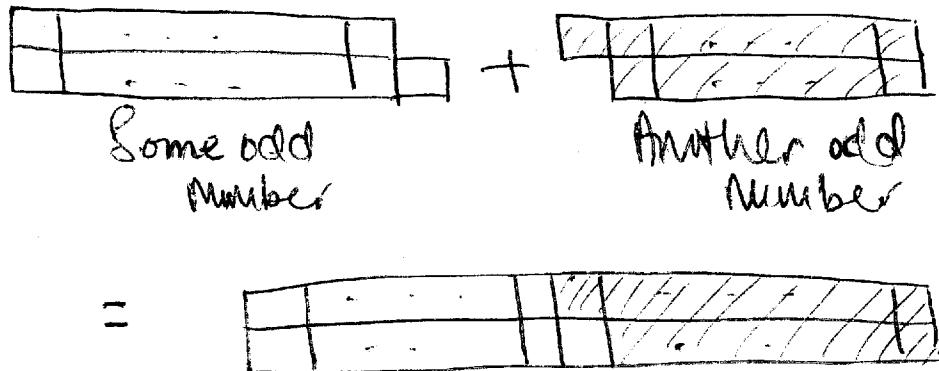
$$2) \quad 332 + 449 = 781$$

$$\begin{array}{r}
 332 \\
 + 449 \\
 \hline
 781
 \end{array}$$

  
 2x166      2x224      2x390

4(a)

$$\begin{array}{r}
 \text{Some odd} \\
 \text{Number} \\
 + \text{Another odd} \\
 \text{Number} \\
 \hline
 \end{array}$$



Total is even!

4(b) Represent two odd numbers by  $2k+1$  and  $2m+1$ ,  
where  $k$  and  $m$  are whole numbers.

Then  $(2k+1) + (2m+1)$

$$= 2k+2m+1+1 \quad \text{Addition property}$$

$$= 2(k+m)+2 \quad \text{distributive property}$$

$$= 2(k+m+1) \quad \text{distributive property}$$

which is an even number.

5) Take any whole number  $A$  and divide it by 2.

By Quotient - Remainder Theorem (p35),

$$A = 2q+r \quad \text{where } 0 \leq r < 2.$$

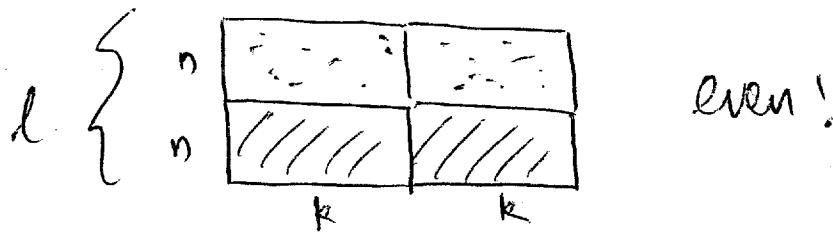
Since  $r$  must be a whole number,  $r$  has  
only two choices : 0 or 1

If  $r = 0$ , then  $A = 2q$  which means  $A$  is even.

If  $r = 1$ , then  $A = 2q+1$  which means  $A$  is odd.

6) (a) Let the two even numbers be  $2k$  and  $2n (=l)$

picture proof

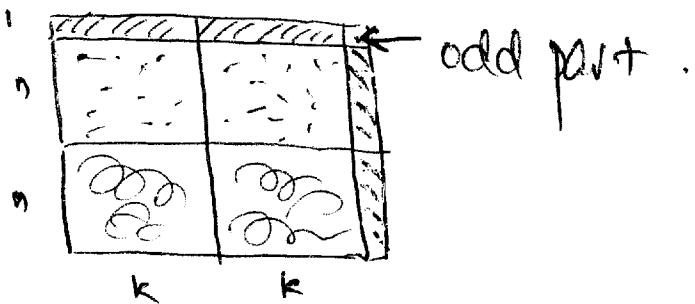


Algebraic Proof :

The product of an even no.  $2k$  with a no.  $l$  is:  $2k \cdot l = 2(kl)$  by the associative property of multiplication, and  $2(kl)$  is twice a whole number, so it is even.

(c) Let the two odd numbers be  $2k+1$  and  $2n+1$ .

picture proof



algebraic proof

$$\begin{aligned}
 (2k+1)(2n+1) &= 2k(2n+1) + 1(2n+1) \\
 &\stackrel{\text{distributive property}}{=} 2(2kn) + 2k + 2n + 1 \\
 &\stackrel{\text{distributive property}}{=} 2\underline{(2kn + k+n)} + 1 \quad \text{which is odd!} \\
 &\stackrel{\text{distributive property}}{=} 2(2kn + k+n) + 1
 \end{aligned}$$

7)(a) Suppose A is even. Then  $A = 2m$   
where m is a whole number.

If B is even, then  $B = 2k$  where k is  
also a whole number

$$\begin{aligned}A+B &= 2m+2k \\&= 2(m+k) \text{ (distributive property)}\end{aligned}$$

which is even.

(b) Suppose A is even. Then  $A = 2m$   
where m is a whole number.

If A+B is even, then  $A+B = 2l$   
where l is also a whole number.

$$\begin{aligned}B &= (A+B) - A \\&= 2l - 2m \\&= 2(l-m) \text{ distributive property}\end{aligned}$$

which is even