

Exercises - Chapter 1

Scientific Notation

A) $x = 299,750,000$

$$x = 2.9979 \times 10^8$$

Enter $a, k = 2.9979, 8$

B) $x = 0.51$

$$x = 5.1 \times 10^{-1}$$

Enter $a, k = 5.1, -1$

C) $4.0 \times 10^3 + 4 \times 10^2$

→ Put both numbers on the same power of 10

$$4.0 \times 10^3 + 0.4 \times 10^3 = 4.4 \times 10^3$$

Enter $a, k = 4.4, 3$

D)
$$x = \frac{(6.67 \times 10^{-11})(5.97 \times 10^{24})}{(6.38 \times 10^6)^2}$$

Collect the powers of 10

$$x = \frac{(6.67)(5.97)}{(6.38)^2} \times \left(\frac{10^{-11} 10^{24}}{10^{12}} \right)$$

$$x = (0.97827) \times (10) = 9.78 \quad \text{3 significant figures}$$

Enter $a, k = 9.78, 0$

Converting Units

$$A) \quad x = 631.1 \text{ inch} \times \left(\frac{2.54 \text{ cm}}{1 \text{ inch}} \right) = 1602.994 \text{ cm}$$

Report 3 significant figures $x = 1.60 \times 10^3 \text{ cm}$

$$x = 1,600$$

B) This requires two conversions

$$R = 1.971 \times 10^7 \text{ yards} \times \left(\frac{3 \text{ ft}}{1 \text{ yard}} \right) \times \left(\frac{1 \text{ mile}}{5280 \text{ ft}} \right)$$

$$R = 11.198 \text{ miles}$$

Report 4 significant figures $R = 11.20 \text{ miles}$

$$C) \quad v = 1 \frac{\text{mile}}{\text{hour}} \times \left(\frac{1609 \text{ m}}{\text{mile}} \right) \times \left(\frac{1 \text{ hour}}{3600 \text{ s}} \right)$$

$$v = 0.4469 \frac{\text{m}}{\text{s}} = 0.447 \frac{\text{m}}{\text{s}} \quad (\text{to 3 significant figures})$$

2. **Picture the Problem:** This is simply a units conversion problem.

Strategy: Multiply the given number by conversion factors to obtain the desired units.

Solution: (a) Convert the units:
$$70 \mu\text{m} \times \frac{1.0 \times 10^{-6} \text{ m}}{\mu\text{m}} = \boxed{7.0 \times 10^{-5} \text{ m}}$$

(b) Convert the units again:
$$70 \mu\text{m} \times \frac{1.0 \times 10^{-6} \text{ m}}{\mu\text{m}} \times \frac{1 \text{ km}}{1000 \text{ m}} = \boxed{7.0 \times 10^{-8} \text{ km}}$$

Insight: The inside back cover of the textbook has a helpful chart of the metric prefixes.

17. **Picture the Problem:** This is a significant figures question.

Strategy: Follow the given rules regarding the calculation and display of significant figures.

Solution: 1. (a) The leading zeros are not significant: $0.0000 \underline{5} \underline{4}$ has $\boxed{2}$ significant figures

2. (b) The middle zeros are significant: $\underline{3}.\underline{0}\underline{0}\underline{1} \times 10^5$ has $\boxed{4}$ significant figures

Insight: Zeros are the hardest part of determining significant figures. Scientific notation can remove the ambiguity of whether a zero is significant because any trailing zero to the right of the decimal point is significant.

34. **Picture the Problem:** This is a units conversion problem.

Strategy: Multiply the known quantity by appropriate conversion factors to change the units.

Solution: 1. Convert m/s to ft/s:
$$\left(20.0 \frac{\text{m}}{\text{s}}\right) \left(\frac{3.28 \text{ ft}}{\text{m}}\right) = \boxed{65.6 \text{ ft/s}}$$

2. (b) Convert m/s to mi/h:
$$\left(20.0 \frac{\text{m}}{\text{s}}\right) \left(\frac{1 \text{ mi}}{1609 \text{ m}}\right) \left(\frac{3600 \text{ s}}{1 \text{ h}}\right) = \boxed{44.7 \text{ mi/h}}$$

Insight: Conversion factors are conceptually equal to one, even though numerically they often equal something other than one. They are often helpful in displaying a number in a convenient, useful, or easy-to-comprehend fashion.

47. **Picture the Problem:** This is a units conversion problem.

Strategy: Multiply the known quantity by appropriate conversion factors to change the units.

Solution: 1. (a) Convert m/s to mi/h:
$$\left(140 \frac{\text{m}}{\text{s}}\right) \left(\frac{1 \text{ mi}}{1609 \text{ m}}\right) \left(\frac{3600 \text{ s}}{1 \text{ h}}\right) = \boxed{310 \frac{\text{mi}}{\text{h}}}$$

2. (b) Convert m/s to m/ms:
$$\left(140 \frac{\text{m}}{\text{s}}\right) \left(\frac{1 \times 10^{-3} \text{ s}}{1 \text{ ms}}\right) = 0.14 \frac{\text{m}}{\text{ms}} \times 5.0 \text{ ms} = \boxed{0.70 \text{ m}}$$

Insight: Conversion factors are conceptually equal to one, even though numerically they often equal something other than one. They are often helpful in displaying a number in a convenient, useful, or easy-to-comprehend fashion.