

## Special Cases for Translation

CONSTRUCTION	TRANSLATION
neither p nor q not either p or q both p and q are not not p and not q	$\sim(p \vee q)$ or $\sim p \cdot \sim q$
not both p and q not p or not q	$\sim(p \cdot q)$ or $\sim p \vee \sim q$
p or q but not both	$(p \vee q) \cdot \sim(p \cdot q)$
p unless q	$p \vee q$ or $\sim q \supset p$ or $\sim p \supset q$
if p then q if p, q p only if q p is sufficient for q p implies q	$p \supset q$
p if q p is necessary for q p is implied by q	$q \supset p$

For transformation of the conjunction and disjunction, see DeMorgan's Theorem:

$$\begin{aligned} \sim(p \cdot q) &\equiv (\sim p \vee \sim q) \\ \sim(p \vee q) &\equiv (\sim p \cdot \sim q) \end{aligned}$$

For transformation of the conditional, see Contraposition:

$$(p \supset q) \equiv (\sim q \supset \sim p)$$

Exclusive disjunction  $(p \vee q) \cdot \sim(p \cdot q)$

Inclusive disjunction  $(p \vee q) \cdot (p \cdot q)$