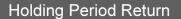


#### 5.1 RATES OF RETURN



$$HPR = \frac{P_1 - P_0 + D_1}{P_0}$$

 $P_0$  = Beginning Price  $P_1$  = Ending Price  $D_1$  = Cash Dividend

# Rates of Return: Single Period Example

Ending Price = 24 Beginning Price = 20 Dividend = 1

HPR = ( 24 - 20 + 1 )/ ( 20) = 25%

#### Measuring Investment Returns Over Multiple Periods

- May need to measure how a fund performed over a preceding five-year period
- Return measurement is more ambiguous in this case

# Rates of Return: Multiple Period Example Text (Page 128)

# Returns Using Arithmetic and Geometric Averaging

<u>Arithmetic</u>

$$\begin{split} r_a &= (r_1 + r_2 + r_3 + \dots r_n) \ / \ n \\ r_a &= (.10 + .25 - .20 + .25) \ / \ 4 \\ &= .10 \ or \ 10\% \\ \hline \frac{Geometric}{r_g = \{[(1+r_1) \ (1+r_2) \ \dots \ (1+r_n)]\}^{1/n} - 1 \\ r_g &= \{[(1.1) \ (1.25) \ (.8) \ (1.25)]\}^{1/4} - 1 \\ &= \ (1.5150)^{1/4} - 1 = .0829 = \ 8.29\% \end{split}$$

### **Dollar Weighted Returns**

<u>Internal Rate of Return (IRR)</u> - the discount rate that results in present value of the future cash flows being equal to the investment amount

- Considers changes in investment
- Initial Investment is an outflow
- Ending value is considered as an inflow
- Additional investment is a negative flow
- Reduced investment is a positive flow

	lar Weigl Fext Exa			•	8)
Net CFs \$ (mil)	<u>1</u> - 0.1 -0				
$1.0 = \frac{-0.1}{1 + IRR} +$	$-\frac{-0.5}{\left(1+IRR\right)^2}+$	0.8 (1+ <i>IRI</i>	$\overline{R}$ ) <sup>3</sup> + $\overline{(1)}$	$\frac{1.0}{+IRR)^4}$	= 4.17%

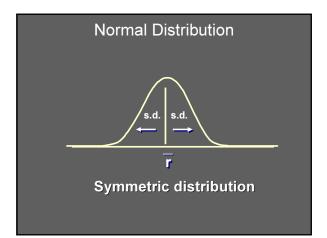
### **Quoting Conventions**

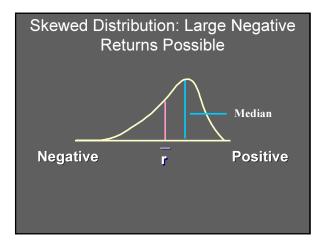
APR = annual percentage rate (periods in year) X (rate for period) EAR = effective annual rate ( 1+ rate for period)<sup>Periods per yr</sup> - 1 *Example: monthly return of 1%* APR = 1% X 12 = 12% EAR = (1.01)<sup>12</sup> - 1 = 12.68%

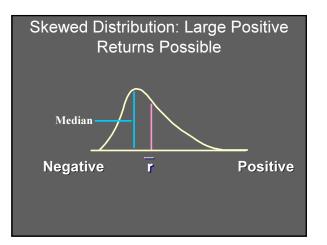
## Scenario Analysis and Probability Distributions

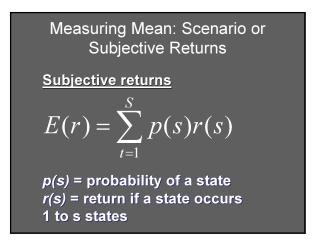
- 1) Mean: most likely value
- 2) Variance or standard deviation
- 3) Skewness
- \* If a distribution is approximately normal, the distribution is described by characteristics 1 and 2

#### 5.2 RISK AND RISK PREMIUMS

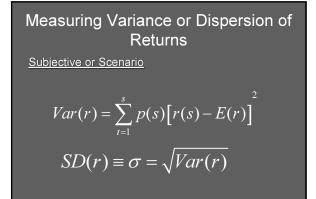








	_		_
		ple: Subjective Distributions	or
State Prob.	of State r	in State	
1	.1	05	
2	.2	.05	
2 3	.4	.15	
4	.2	.25	
5	.1	.35	
		2)(.05)+ (.1)(.35)	
E(r) = .1	5 or 15%		



# Measuring Variance or Dispersion of Returns

Using Our Example:

Var =[(.1)(-.05-.15)2+(.2)(.05- .15)2...+ .1(.35-.15)2] Var= .01199 S.D.= [ .01199] 1/2 = .1095 or 10.95%

#### **Risk Premiums and Risk Aversion**

Degree to which investors are willing to commit funds

Risk aversion

If T-Bill denotes the risk-free rate, r<sub>f</sub>, and variance, σ<sup>2</sup><sub>p</sub>, denotes volatility of returns then:
 The risk premium of a portfolio is:

 $E(r_P)-r_f$ 

# **Risk Premiums and Risk Aversion**

To quantify the degree of risk aversion with parameter A:

$$E(r_p) - r_f = \frac{1}{2} A \sigma_p^2$$
  
= Or:  
$$A = \frac{E(r_p) - r_f}{\frac{1}{2} \sigma_p^2}$$

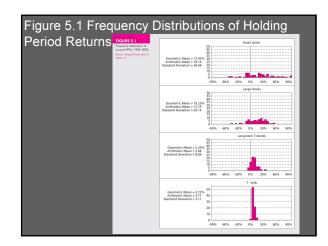
# The Sharpe (Reward-to-Volatility) Measure $S = \frac{\text{portfolio risk premium}}{\text{standard deviation of portfolio excess return}}$ $= \frac{E(r_p) - r_f}{\sigma_p}$

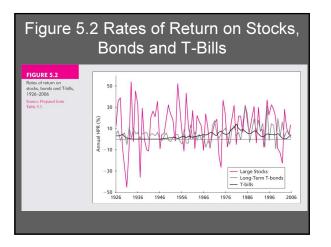
5.3 THE HISTORICAL RECORD

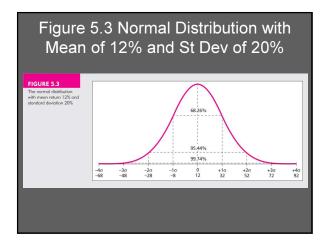
## Annual Holding Period Returns From Table 5.3 of Text

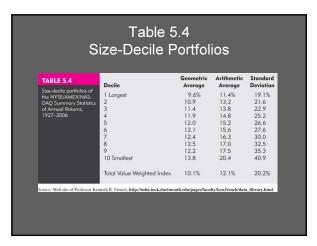
	Geom.	Arith.	Stan.
<u>Series</u>	Mean%	Mean%	<u>Dev.%</u>
World Stk	9.80	11.32	18.05
US Lg Stk	10.23	12.19	20.14
US Sm Stk	12.43	18.14	36.93
Wor Bonds	5.80	6.17	9.05
LT Treas.	5.35	5.64	8.06
T-Bills	3.72	3.77	3.11
Inflation	3.04	3.13	4.27

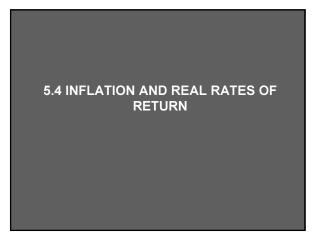
Annual Holding From Ta			
	Risk	Stan.	Sharpe
<u>Series</u>	Prem.	Dev.%	<u>Measure</u>
World Stk	7.56	18.37	0.41
US Lg Stk	8.42	20.42	0.41
US Sm Stk	14.37	37.53	0.38
Wor Bonds	2.40	8.92	0.27
LT Treas	1.88	7.87	0.24











#### Real vs. Nominal Rates

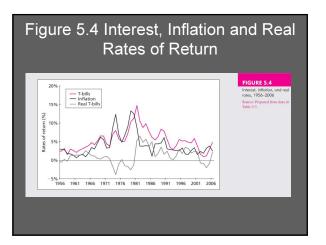
Fisher effect: Approximation nominal rate = real rate + inflation premium R = r + i or r = R - iExample r = 3%, i = 6%R = 9% = 3% + 6% or 3% = 9% - 6%

## Real vs. Nominal Rates

Fisher effect:

2.83%

$$1 + r = \frac{1 + R}{1 + i}$$
 or:  
 $r = \frac{R - i}{1 + i}$   
 $r = (9\% - 6\%) / (1.06)$ 





# Allocating Capital

 Possible to split investment funds between safe and risky assets
 Risk free asset: proxy; T-bills
 Risky asset: stock (or a portfolio)

# Allocating Capital

#### Issues

- Examine risk/ return tradeoff
- Demonstrate how different degrees of risk aversion will affect allocations between risky and risk free assets

#### The Risky Asset: Text Example (Page 143)

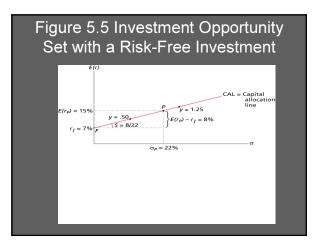
Total portfolio value	=	\$300,000
Risk-free value	=	90,000
Risky (Vanguard and Fidelity)	=	210,000
Vanguard (V) = 54%		
Fidelity (F) = 46%		

# The Risky Asset: Text Example (Page 143)

$y = \frac{210,000}{300,000}$	
$1 - y = \frac{90,00}{300,00}$	$\frac{10}{00} = 0.3$ (risk-free assets)
Vanguard	113,400/300,000 = 0.378
Fidelity	96,600/300,000 = 0.322
Portfolio <i>P</i>	210,000/300,000 = 0.700
<u>Risk-Free Assets F</u>	90,000/300,000 = 0.300
Portfolio C	300,000/300,000 = 1.000

Calculating the E Text Example	
r <sub>f</sub> = 7%	σ <sub>rf</sub> = 0%
E(r <sub>p</sub> ) = 15%	σ <sub>p</sub> = 22%
y = % in p	(1-y) = % in r <sub>f</sub>

Expected Returns for Combinations  $E(r_c) = yE(r_p) + (1 - y)r_f$   $r_c = \text{complete or combined portfolio}$ For example, y = .75  $E(r_c) = .75(.15) + .25(.07)$  = .13 or 13%



Variance on the Possible Combined Portfolios Since  $\sigma_{r_r} = 0$ , then  $\sigma_c = y \sigma_p$  Combinations Without Leverage If y = .75, then  $\sigma_c = .75(.22) = .165$  or 16.5% If y = 1  $\sigma_c = 1(.22) = .22$  or 22% If y = 0  $\sigma_c = 0(.22) = .00$  or 0%

# Using Leverage with Capital Allocation Line

Borrow at the Risk-Free Rate and invest in stock Using 50% Leverage  $r_c = (-.5) (.07) + (1.5) (.15) = .19$ 

 $\sigma_{c}$  = (1.5) (.22) = .33

# Risk Aversion and Allocation

- Greater levels of risk aversion lead to larger proportions of the risk free rate
- Lower levels of risk aversion lead to larger proportions of the portfolio of risky assets
- Willingness to accept high levels of risk for high levels of returns would result in leveraged combinations

5.6 PASSIVE STRATEGIES AND THE CAPITAL MARKET LINE

#### Table 5.5 Average Rates of Return, Standard Deviation and Reward to Variability

TABLE 5.5		Excess R	eturn (%)	
Average excess rate of		Average	SD	Sharpe Ratio
return, standard devia-	1926-1946	8.36	27.98	0.30
tions and the reward-to-	1947-1966	12.72	18.05	0.70
volatility ratio of large	1967-1986	4.14	17.44	0.24
common stocks over	1987-2006	8.47	16.22	0.52
one-month bills over 1926–2006 and various subperiods	1926-2006	8.42	20.42	0.41
ource: Data in Table 5.3.			_	_
ource: Data in Table 5.3.				
ource: Data in Table 5.3.				
eurce: Data in Table 5.3.				
ource: Data in Table 5.3,				

#### Costs and Benefits of Passive Investing

- Active strategy entails costs
- Free-rider benefit
- Involves investment in two passive portfolios
  - Short-term T-bills
  - Fund of common stocks that mimics a broad market index